



# Estimation of Surface Fluxes of Carbon, Heat, Moisture and Momentum from Atmospheric Data Assimilation

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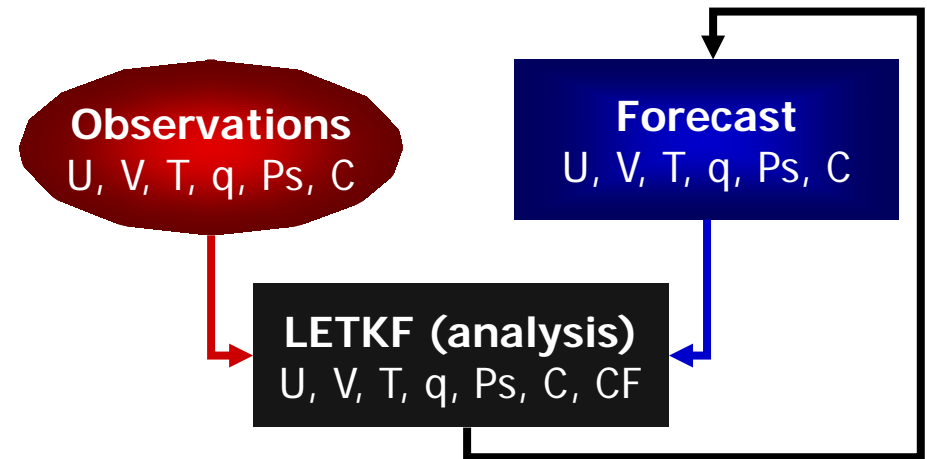
**(재)한국형수치예보모델개발사업단**

- Explore the feasibility of **estimating surface fluxes at the model-grid scale** by assimilating atmospheric variables (U, V, T, q, Ps) and the flux variables **simultaneously**
  - Consider multivariate error covariance in analyzing the flux variables
  - **No *a-priori* information** for the fluxes

# UMD-Berkeley LETKF-C System

$$\mathbf{X}^b = \begin{bmatrix} \mathbf{X} \\ \mathbf{CF} \end{bmatrix}$$

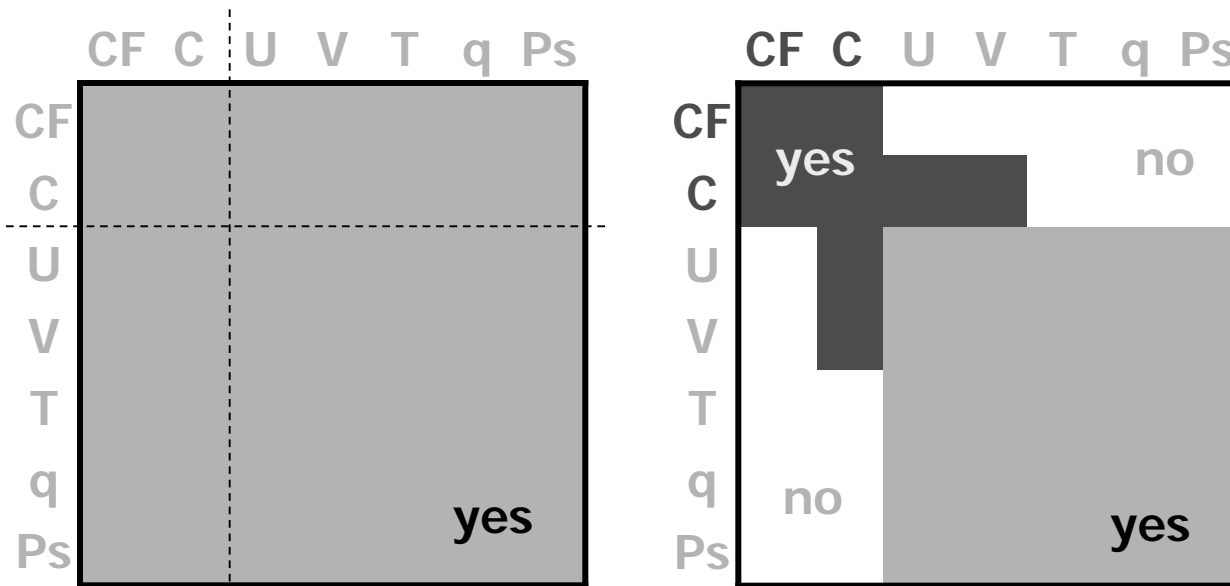
$\mathbf{X}$ : model state vector  
(U, V, T, q, Ps, C)  
 $\mathbf{CF}$ : surface CO<sub>2</sub> flux



- **Parameter estimation: state vector augmentation**
  - Append **CF** (surface CO<sub>2</sub> fluxes)
  - Update **CF** as part of the data assimilation process
- **Simultaneous analysis of carbon and meteorological variables**
  - **Multivariate** analysis with **a localization of the variables** (Kang et al., 2011)
  - Update all variables at every six hours

# (1) Localization of Variables

- If **variables in the state vector are not physically correlated** each other, error covariance between those variables can introduce a sampling error into the analysis system



without variable localization Background error covariance matrix with variable localization

- ➔ **Zeroing out** the background error covariance between those variables improves the result of the analysis

(Kang et al., 2011, JGR)

## (2) Inflation Methods

- **Background uncertainty** tends to be **underestimated** with a limited ensemble size due to the imperfection of the model and nonlinearity of the system.
  - Underestimation is more serious **over the observation-rich area**.
  - ➔ EnKF needs “**inflation**”

<b>Multiplicative inflation</b>	<b>Additive inflation</b>
Multiply $(1.0+\alpha)$ to the background variance	Add perturbations to the background/analysis state

- **The choice of inflation parameter**
  - $\alpha$  for the multiplicative inflation
  - Scaling factor for the additive perturbation in additive inflation
  - ➔ *Manual tuning: very expensive or often infeasible!*
- **Adaptive multiplicative inflation**
  - Estimates multiplicative inflation parameter at each grid point at every analysis step adaptively (Anderson, 2009; Miyoshi, 2012)



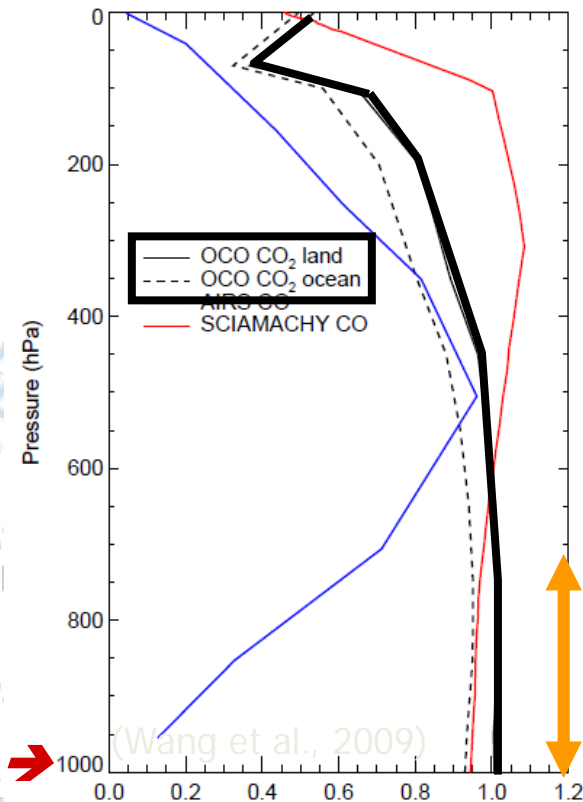
# (3) Vertical Localization

- **Vertical localization** of column mixing CO<sub>2</sub> observation from remote sensing (e.g. GOSAT, OCO-2)
  - Averaging kernel is nearly uniform in the vertical, although **the forcing term** (our ultimate estimate) is **at the surface**
  - We have **localized the column CO<sub>2</sub> data, updating only lower atmospheric CO<sub>2</sub>** rather than a full column of CO<sub>2</sub>

$$\mathbf{y}_i^b = h(\mathbf{x}_{i,k}^b) = \sum_{k=1}^{nlev} a_k S(\mathbf{x}_{i,k}^b)$$

- Calculating innovation based on the averaging kernel

*Forcing is at the surface* →



(Kang et al., 2012)

# Observing System Simulation Experiments

## ■ **Nature run: assumed true state in the experiments**

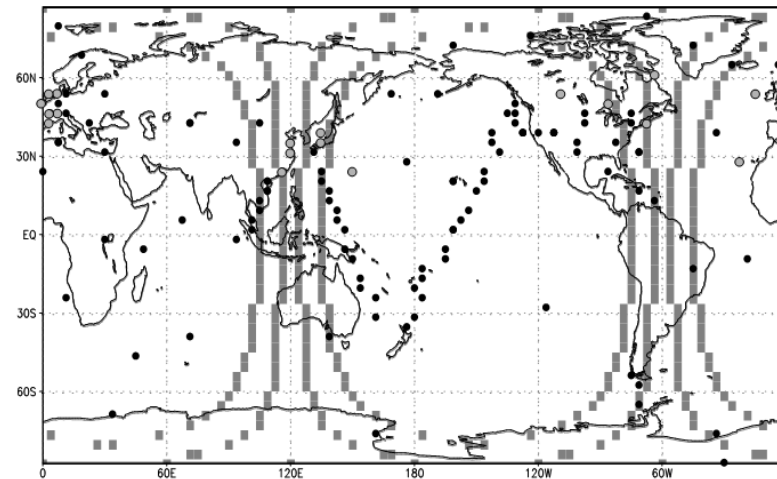
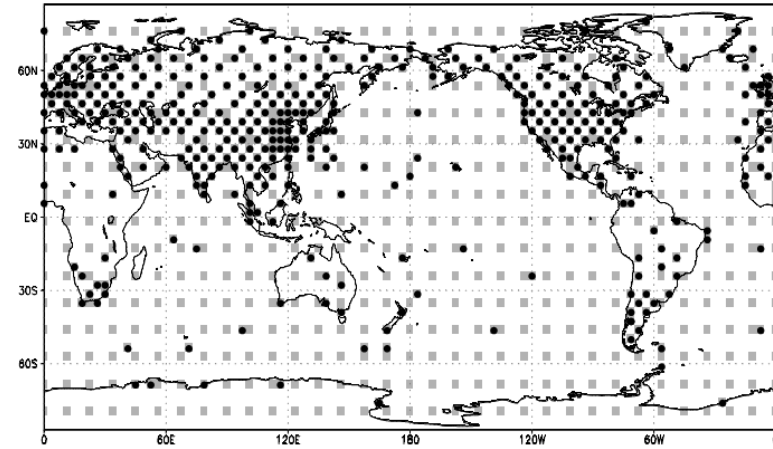
- SPEEDY-C: the modified version of SPEEDY (Molteni, 2003)
  - AGCM with a tracer gas of atmospheric CO<sub>2</sub> (C)
  - Spectral model with T30L7
  - Prognostic variables: U, V, T, q, Ps, C
  - No diurnal cycle
- “True” CO<sub>2</sub> fluxes (true CF)
  - A constant fossil fuel emission (Andres et al., 1996)
  - CASA terrestrial CO<sub>2</sub> fluxes (Gurney et al., 2004)
  - Oceanic CO<sub>2</sub> fluxes (Takahashi et al., 2002)

## ■ **Forecast model**

- SPEEDY-C with persistence forecast of surface CO<sub>2</sub> fluxes (CF)
  - CF is updated only by the data assimilation

# Simulated Observations

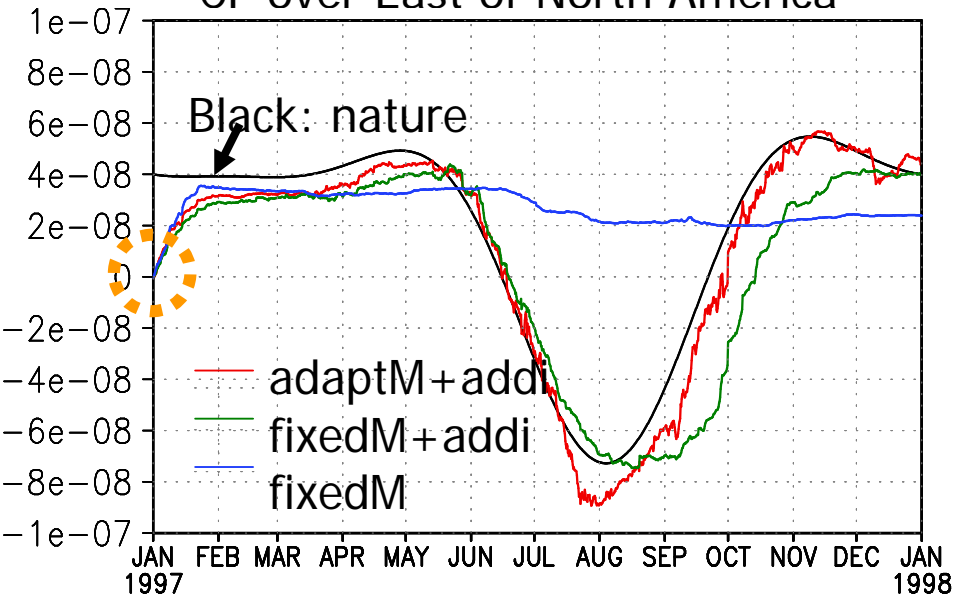
- **Meteorological variables (U, V, T, q, Ps)**
  - Conventional data
    - U, V, T, q: black dots (every 12 hours)
    - Ps: gray boxes (every 6 hours)
- **Atmospheric CO<sub>2</sub> concentrations**
  - in-situ & flask observations
    - Weekly records: black dots (107)
    - Hourly records: gray dots (18)
  - Satellite data from GOSAT
    - GOSAT provides column mixed CO<sub>2</sub> information which has a sensitivity near the surface: gray boxes
- **No direct measurement of surface CO<sub>2</sub> fluxes**





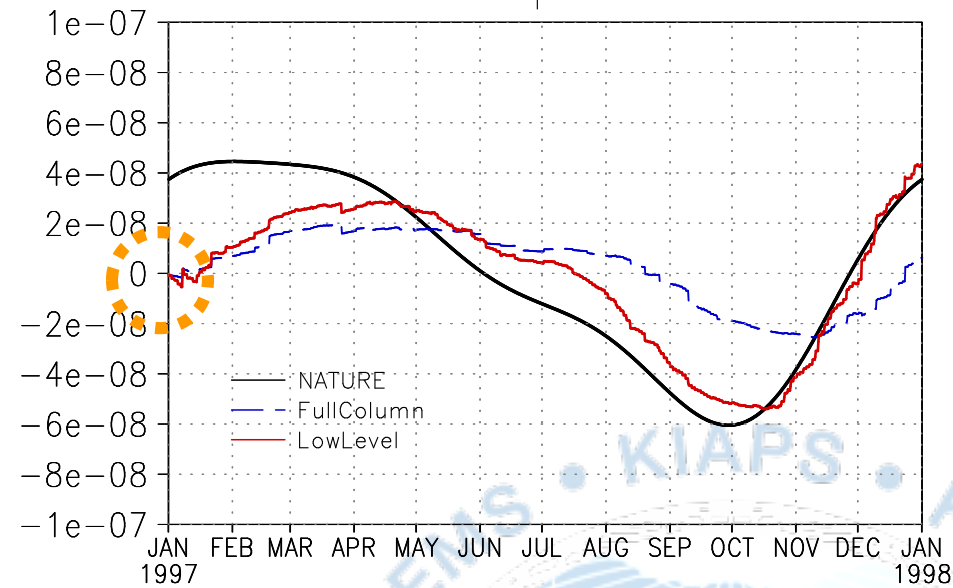
# Results: time series of surface CO<sub>2</sub> fluxes

## CF over East of North America



< observation-rich area >

## CF over N Equatorial Africa



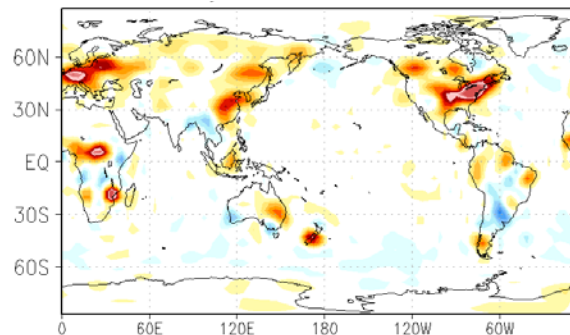
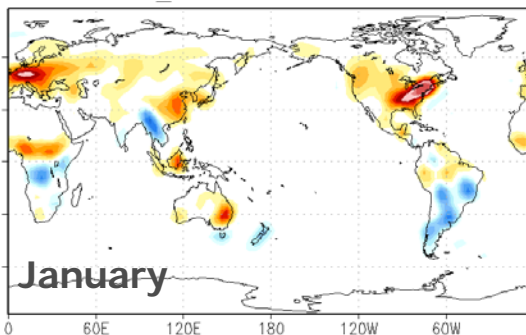
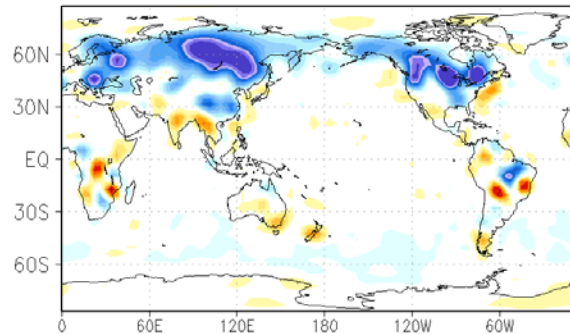
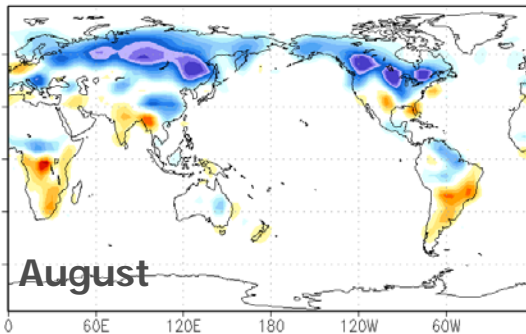
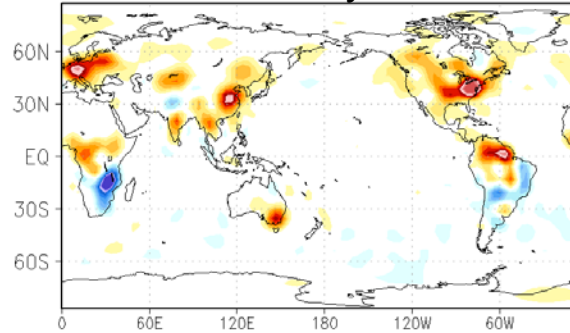
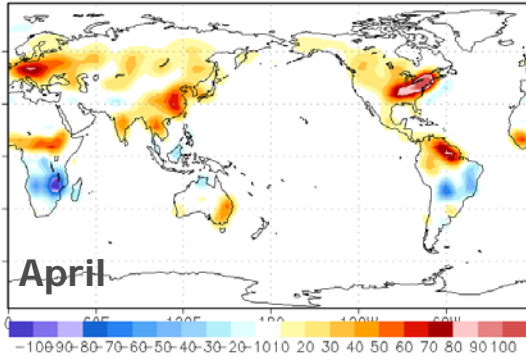
< observation-poor area >

- Advanced inflation methods prevent ensemble from collapsing over observation rich area
  - Additive & adaptive multiplicative inflations help analysis estimate seasonal change of CF.
- Vertical localization improve the CF estimation over area where satellite data are dominant

# Results: surface CO<sub>2</sub> fluxes in different seasons

A: True fluxes

B: Analysis



**Due to the following techniques:**

- 1) Localization of variables (*Kang et al. 2011*)
- 2) Advanced inflation methods (adaptive multiplicative inflation + additive inflation)
- 3) Vertical localization of column mixing CO<sub>2</sub> data (*Kang et al. 2012*)

**we have estimated surface CO<sub>2</sub> fluxes evolving in time successfully!**

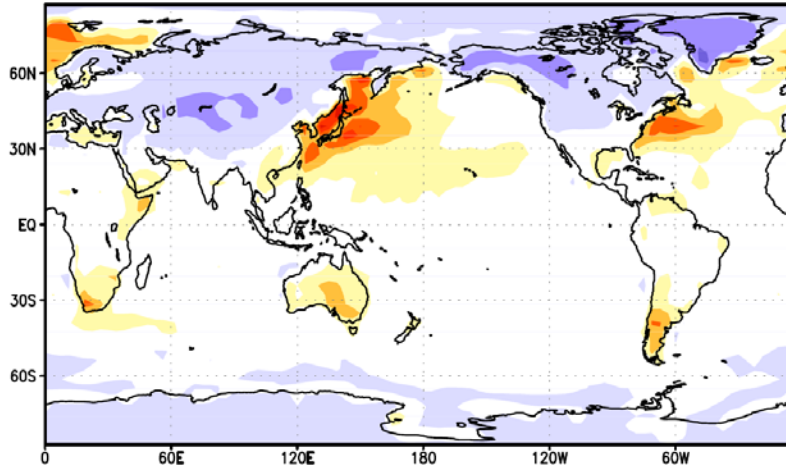
# How about heat/moisture fluxes?

- Can we estimate surface moisture/heat fluxes by assimilating atmospheric moisture/temperature observations? *We can use the same methodology!*
- OSSEs
  - Nature: SPEEDY (perfect model)
  - Forecast model: SPEEDY with **persistence forecast of Sensible/Latent heat fluxes (SHF/LHF)**
  - Simulated observations: conventional observations of (U, V, T, q, Ps) and **AIRS retrievals of (T, q)**
  - Analysis: U, V, T, q, Ps + **SHF & LHF**
- **Fully multivariate data assimilation**
- **Adaptive multiplicative inflation + additive inflation**
- **Initial conditions: random (*no a-priori information*)**

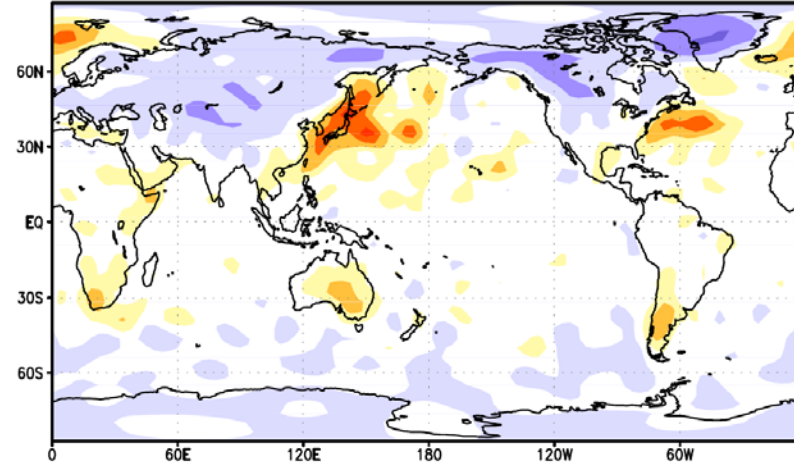


# Results: SHF & LHF (perfect model of WSTR)

True SHF @ end of JAN

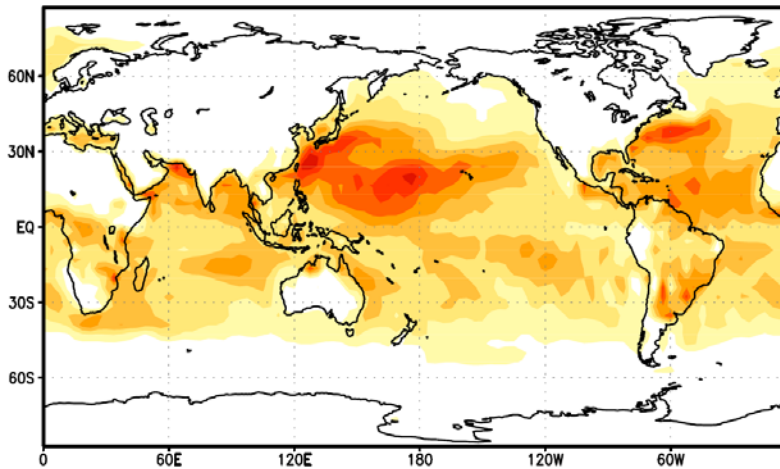


SHF analysis @ end of JAN

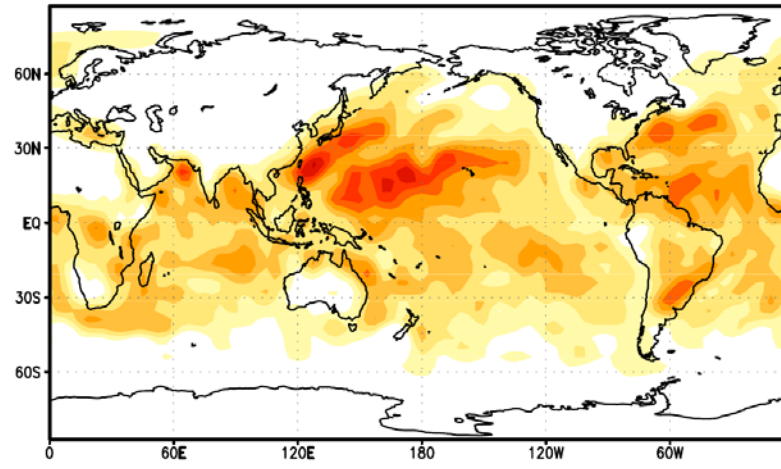


*Estimations converge to the true state just after one month!*

True LHF @ end of JAN



LHF analysis @ end of JAN



# Can we also estimate wind stress?

## ■ OSSEs

- Nature: SPEEDY
- Forecast model: SPEEDY with **persistence forecast of Sensible/Latent heat fluxes (SHF/LHF) and wind stress (USTR, VSTR) [ALL\_FLUXES]**
- Simulated observations: conventional observations of (U, V, T, q, Ps), AIRS retrievals of (T, q), and **ASCAT ocean surface wind observations**
  - **Observation error of ASCAT: 3.5m/s (not as good as AIRS data)**
  - ASCAT covers the global ocean every 12 hours, but little overlapped with AIRS data distribution
- Analysis: U, V, T, q, Ps + **SHF, LHF, USTR, VSTR**

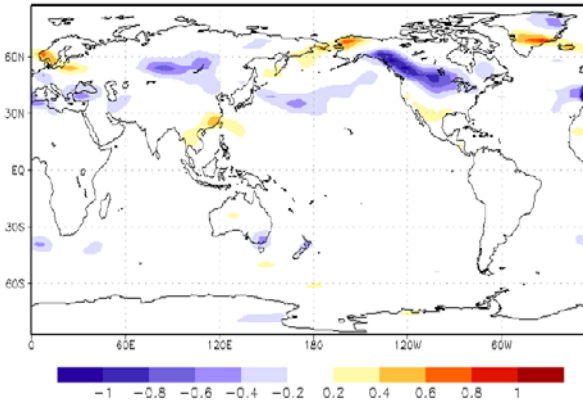
## ■ Fully multivariate data assimilation

## ■ Initial conditions: random (*no a-priori information*)

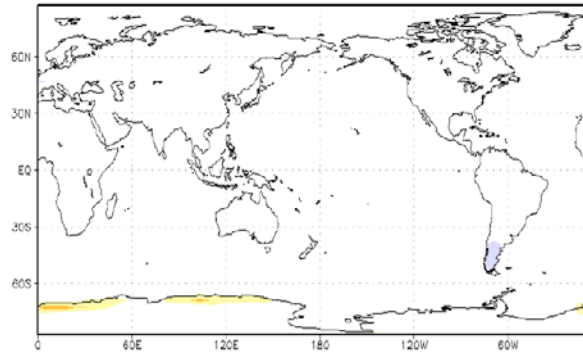


# Result: USTR from [ALL\_FLUXES]

TRUTH\_USTR



Initial USTR

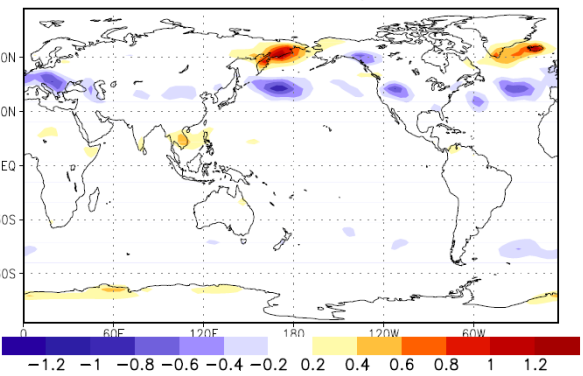


← Initial condition includes no a-priori information of USTR

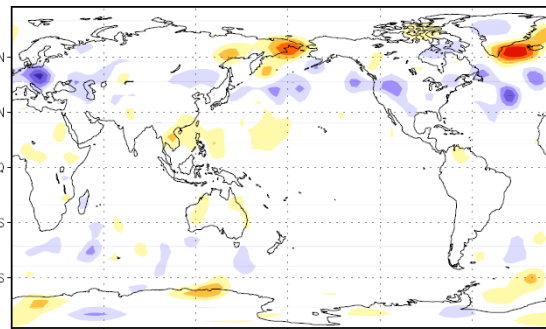
RMSE=1.28e-01

CORR=0.412729

TRUTH\_USTR [N/m<sup>2</sup>]



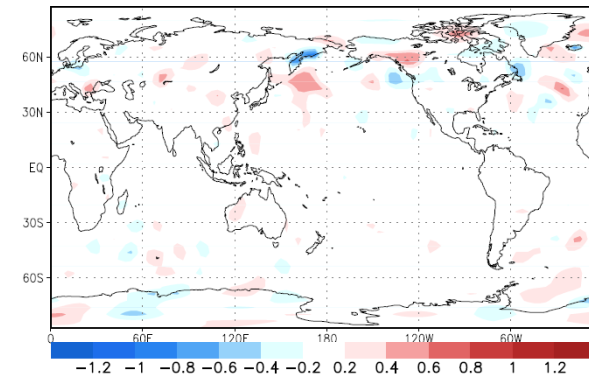
[Analysis: WSTR\_DA]



RMSE=1.33e-01

CORR=0.594041

[Error: WSTR\_DA]

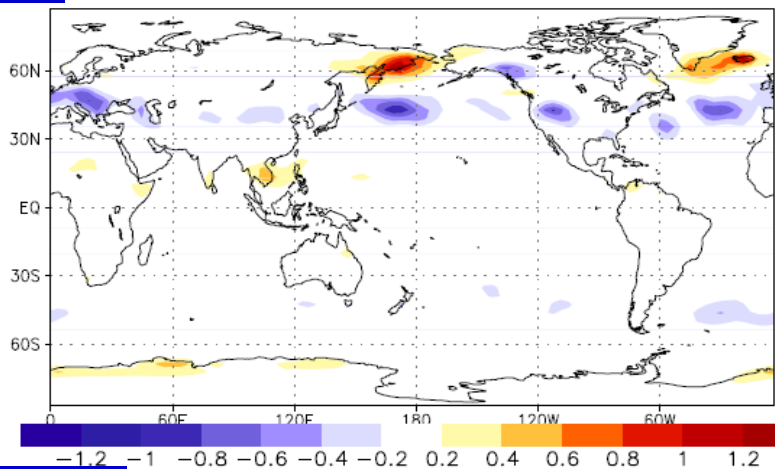


↑ After one month of DA, USTR estimation converges to the true USTR

# Impact of imperfect WSTR on LHF analysis

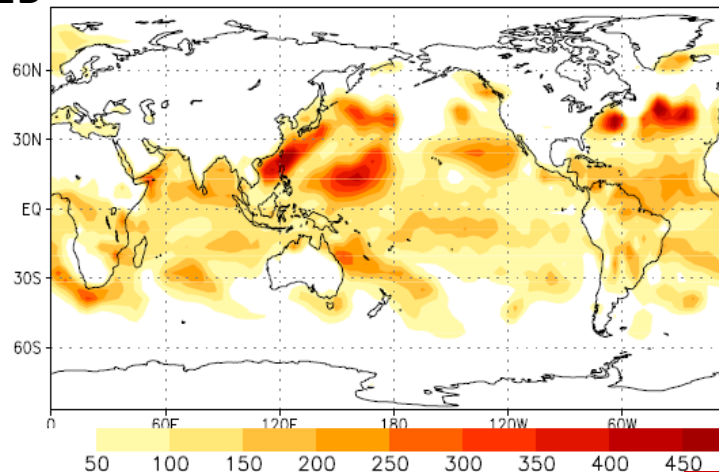
True USTR

TRUTH\_USTR [N/m<sup>2</sup>] 00Z01FEB



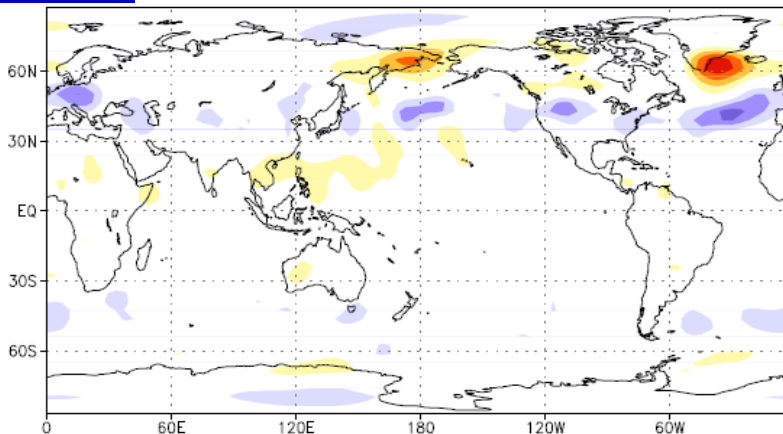
TRUTH\_LHF [W/m<sup>2</sup>]

True LHF



USTR analysis

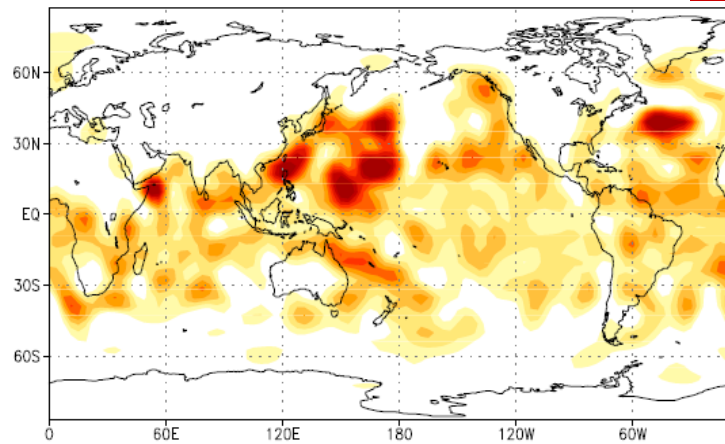
[Analysis: WSTRDA\_FT]



RMSE=1.12e-01

[Analysis: WSTRDA\_FT]

LHF analysis



RMSE=6.30e+01

# Summary and Discussion

- **We succeed in estimating surface CO<sub>2</sub> fluxes with the advanced LETKF-C system, even without *a-priori* information (OSSEs)**
- **With the same methodology, we could estimate surface heat/moisture fluxes!**
  - ➔ After a short spin-up period (~a week), **estimation of SHF and LHF converges very well**, under the perfect model of WSTR
- **We attempt to estimate wind stress (WSTR) within LETKF (without computing it from a physical parameterization of the perfect model) in addition to SHF/LHF estimation**
  - The analysis system still needs further improvement to avoid a negative feedback among WSTR, SHF, LHF, and other prognostic variables due to the imperfect WSTR.
  - Addition of ASCAT data gives fairly good estimation of WSTR