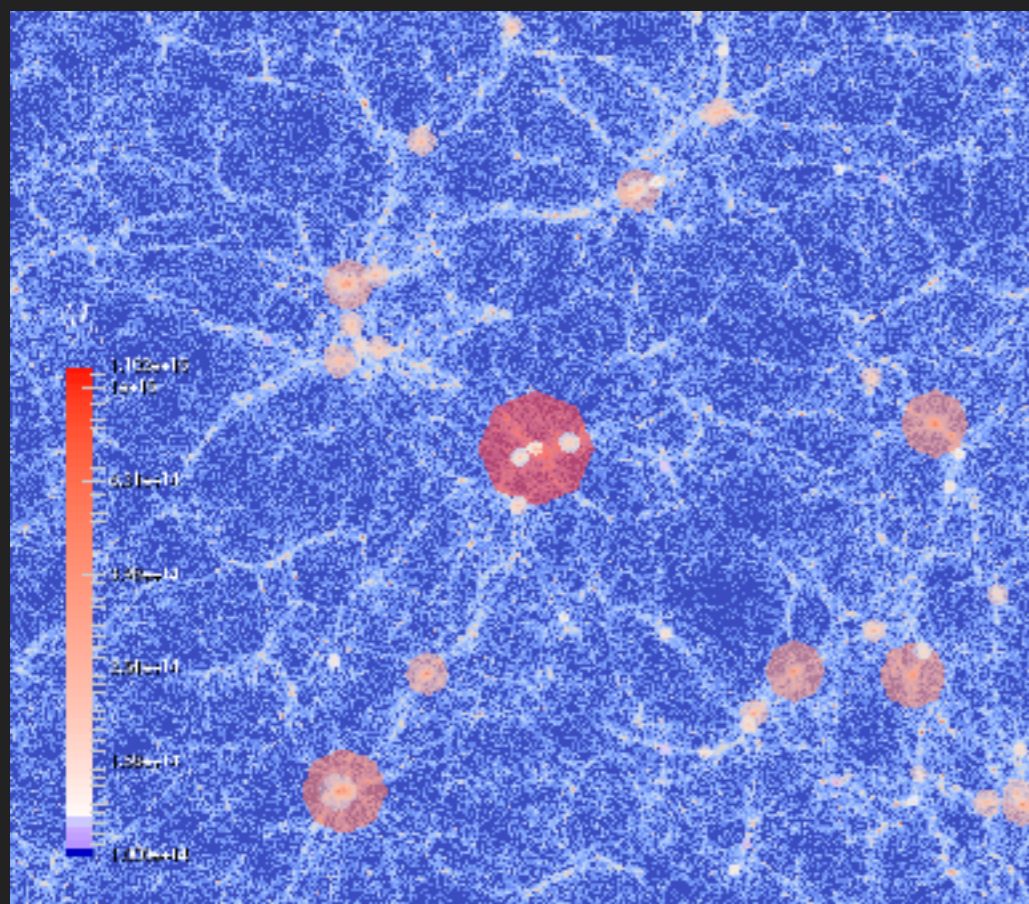


# DARK EMULATOR

## COSMIC LARGE-SCALE STRUCTURES AND PARAMETER ESTIMATION

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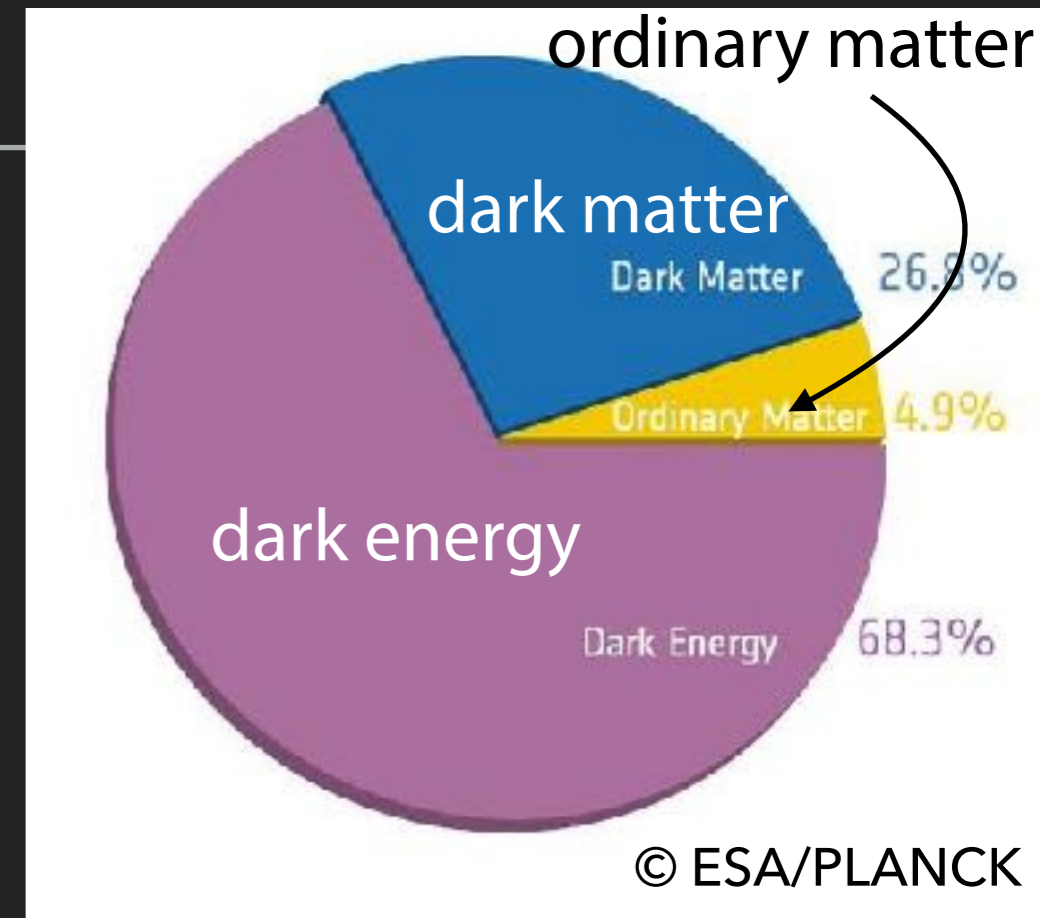
### ▶ Hirosaki U.

Ryuichi Takahashi\*

**BACKGROUND**

# COSMOLOGY: CURRENT STATUS

- ▶ All sorts of observations can be explained by the standard model with only **6 free parameters**
  - ▶ and they are very precisely determined
- ▶ *Dark components* play the major role in the current Universe



Parameter	68 % limits
$\Omega_b h^2$	$0.02225 \pm 0.00016$
$\Omega_c h^2$	$0.1198 \pm 0.0015$
$100\theta_{MC}$	$1.04077 \pm 0.00032$
$\tau$	$0.079 \pm 0.017$
$\ln(10^{10} A_s)$	$3.094 \pm 0.034$
$n_s$	$0.9645 \pm 0.0049$
$H_0$	$67.27 \pm 0.66$
$\Omega_\Lambda$	$0.6844 \pm 0.0091$
Age/Gyr	$13.813 \pm 0.026$

Planck 2015 cosmological params.

baryon density

dark matter density

cosmic geometry (dark energy encoded here)

optical depth

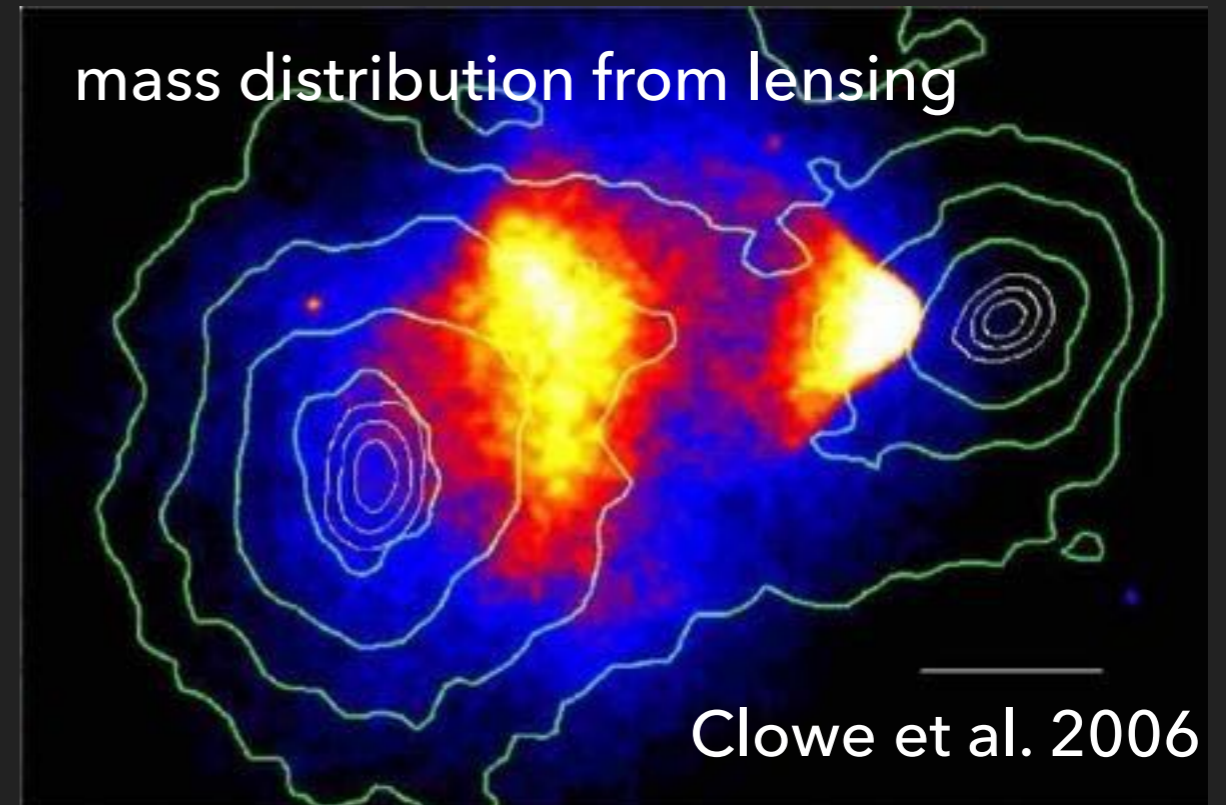
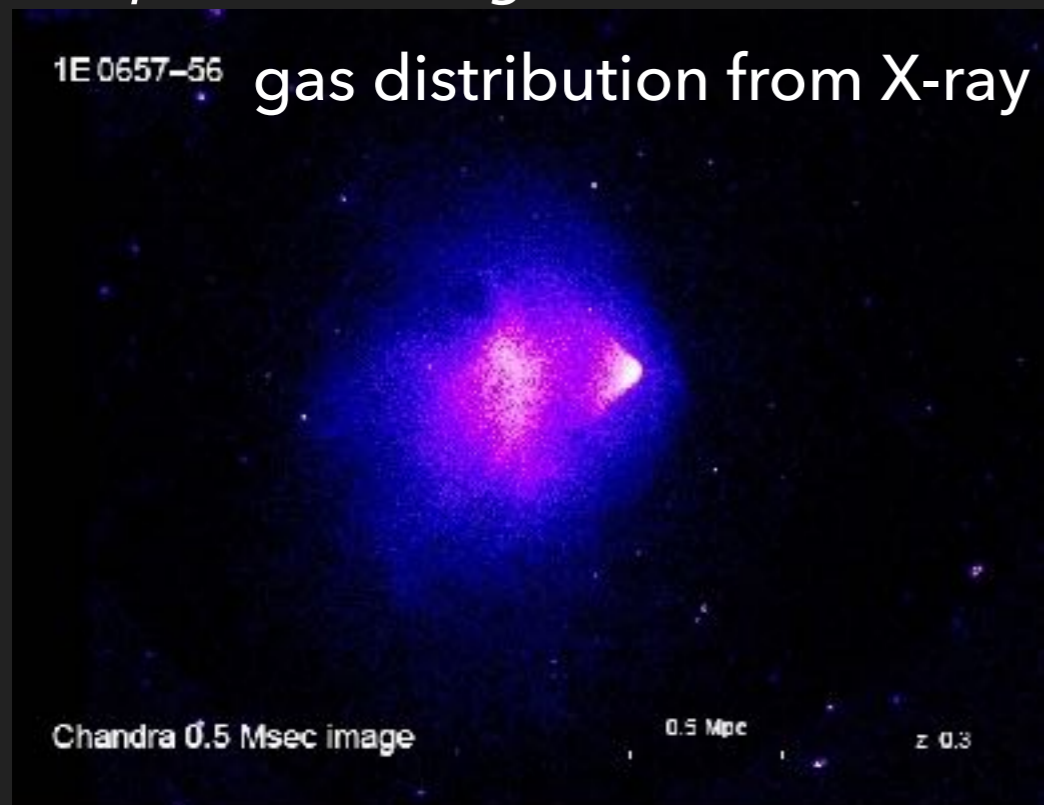
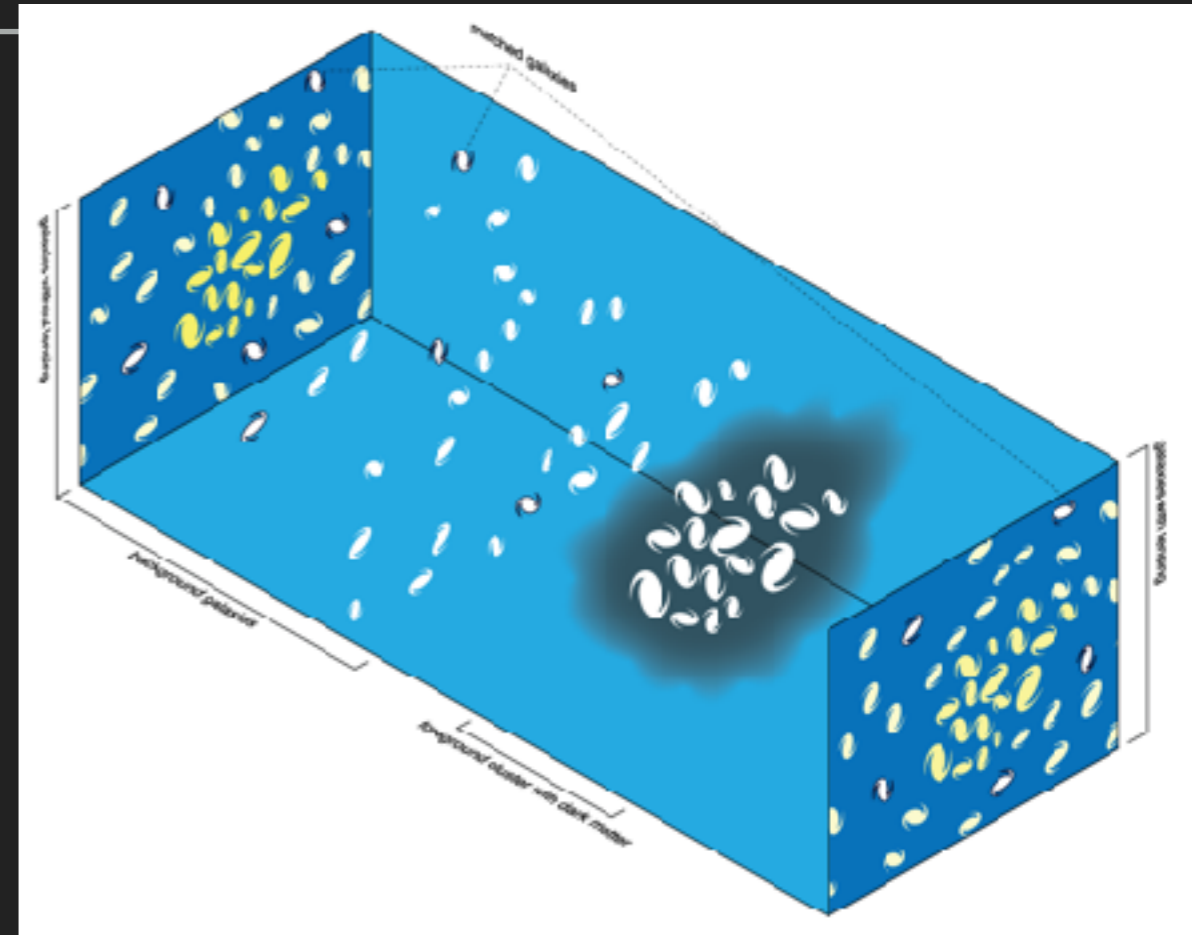
} 2 params for cosmic fluctuations

WHAT IS DARK ENERGY?

WHAT IS DARK MATTER?

# DARK MATTER

- ▶ No light emission but **has mass** (i.e., gravitational interaction)
- ▶ indirectly observable through *gravitational lensing*
  - ▶ light path bent by gravity
- ▶ **bullet cluster**
  - ▶ *Chandra X-ray data vs lensing data*
  - ▶ *small cluster coming from the left and past to the right*

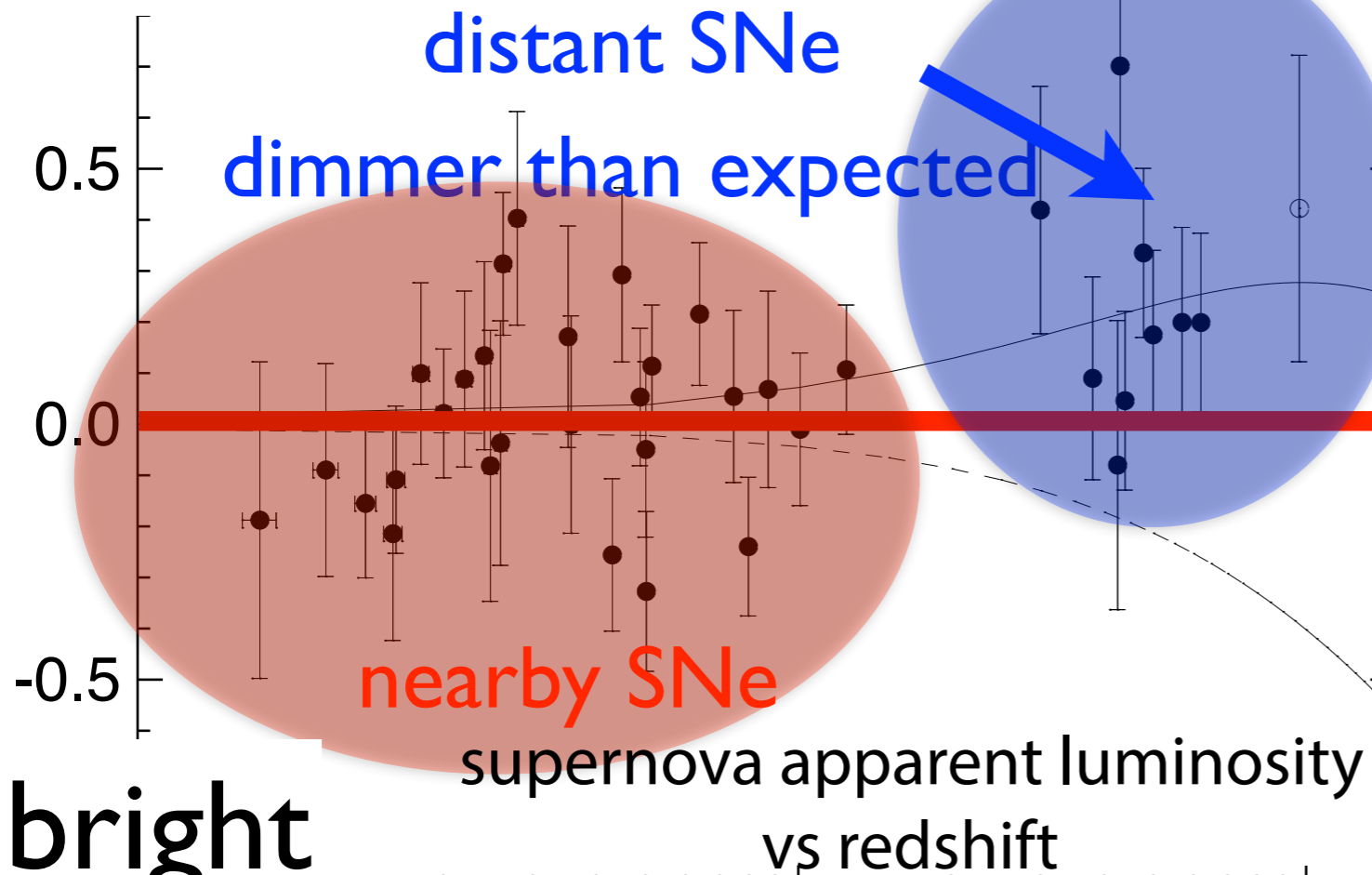


# DARK ENERGY



observation - naive theory

dim



bright

0.01

0.10

1.00

now

redshift

past



Riess (1969-)



Schmidt (1967-)

High-Z Supernova Search Team

Nobel Physics Prize in 2011,  
shared with Perlmutter  
(Supernova Cosmology Project)

***Something is accelerating the expansion!***

# PROBLEM SETTINGS

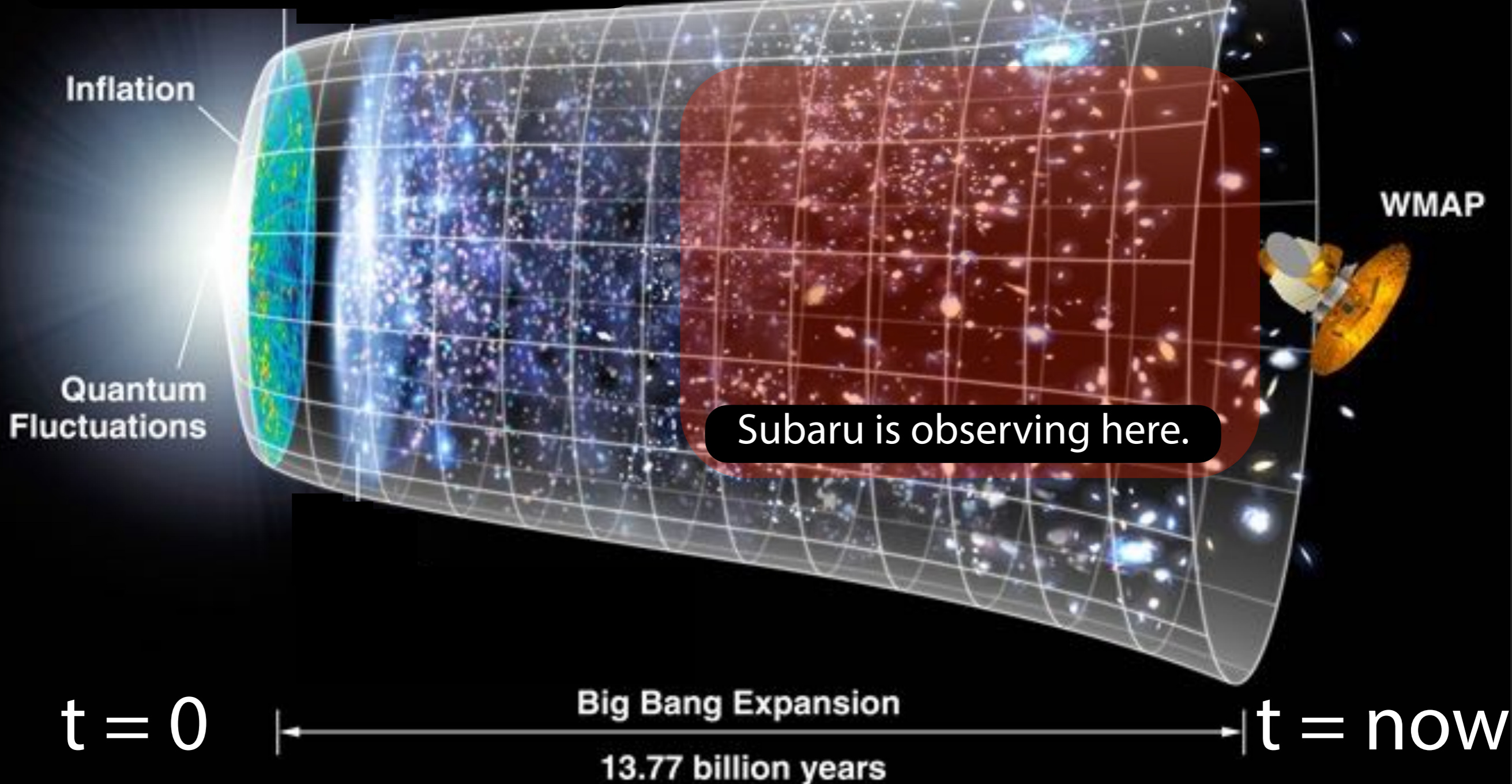
# OBSERVABLE UNIVERSE

©NASA/WMAP

*cosmic microwave background*  
(param. table determined by this)

*large scale structure*

Dark Energy  
Accelerated Expansion



# 3K COSMIC MICROWAVE BACKGROUND ANISOTROPY

*"initial condition"* of our Universe @  $t \sim 380$  kyrs

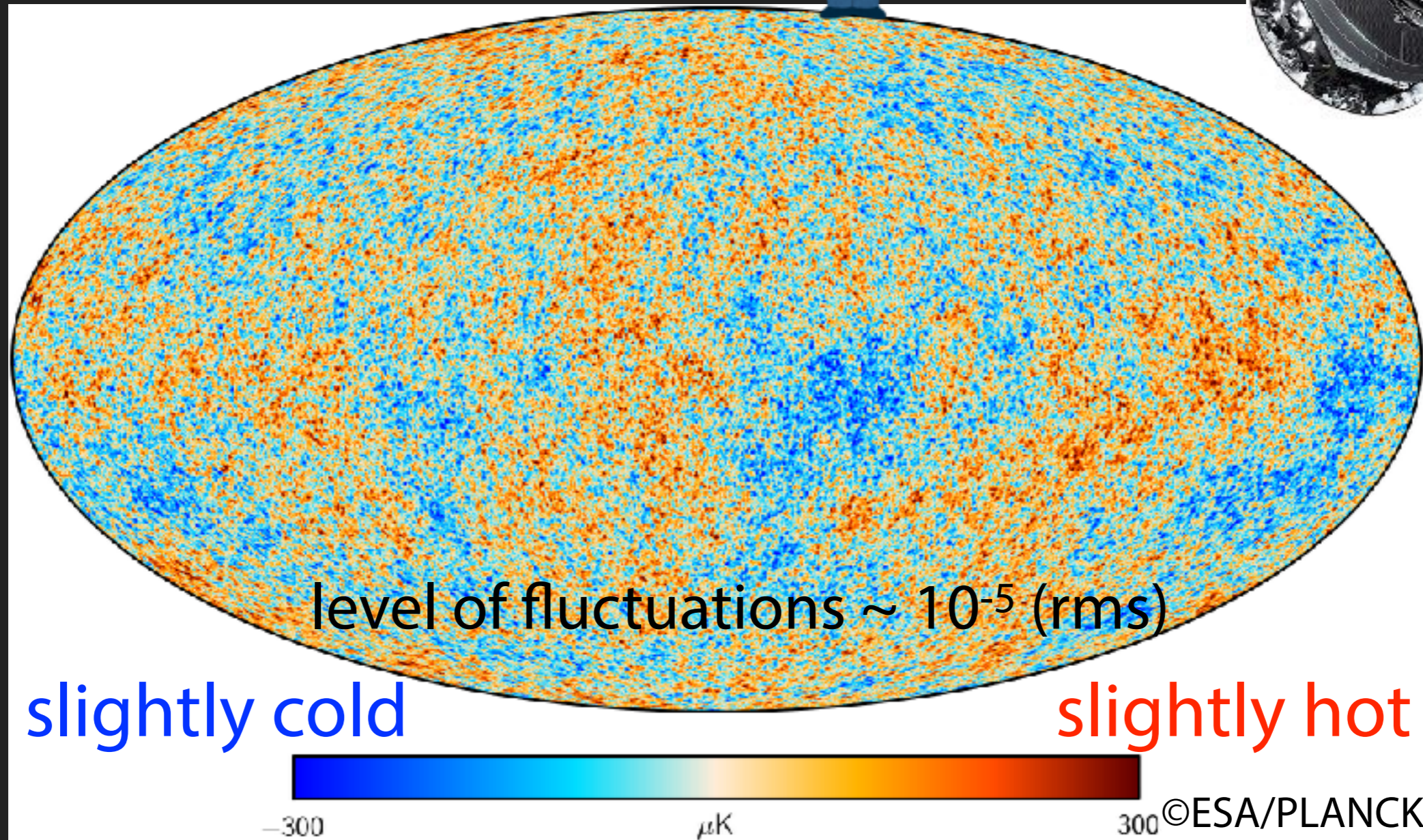
c.f.,  $t_{\text{now}} \sim 14$  Gyrs



7 hours old



30 years old





# COSMIC RANDOM FIELDS

- ▶ Assume *cosmological principle*
  - ▶ no special place
  - ▶ *homogeneity* + *isotropy* (in a statistical sense)

- ▶ consider the “fluctuations”:

$$\delta_A(\mathbf{x}, t) = [A(\mathbf{x}, t) - A(t)]/A(t)$$

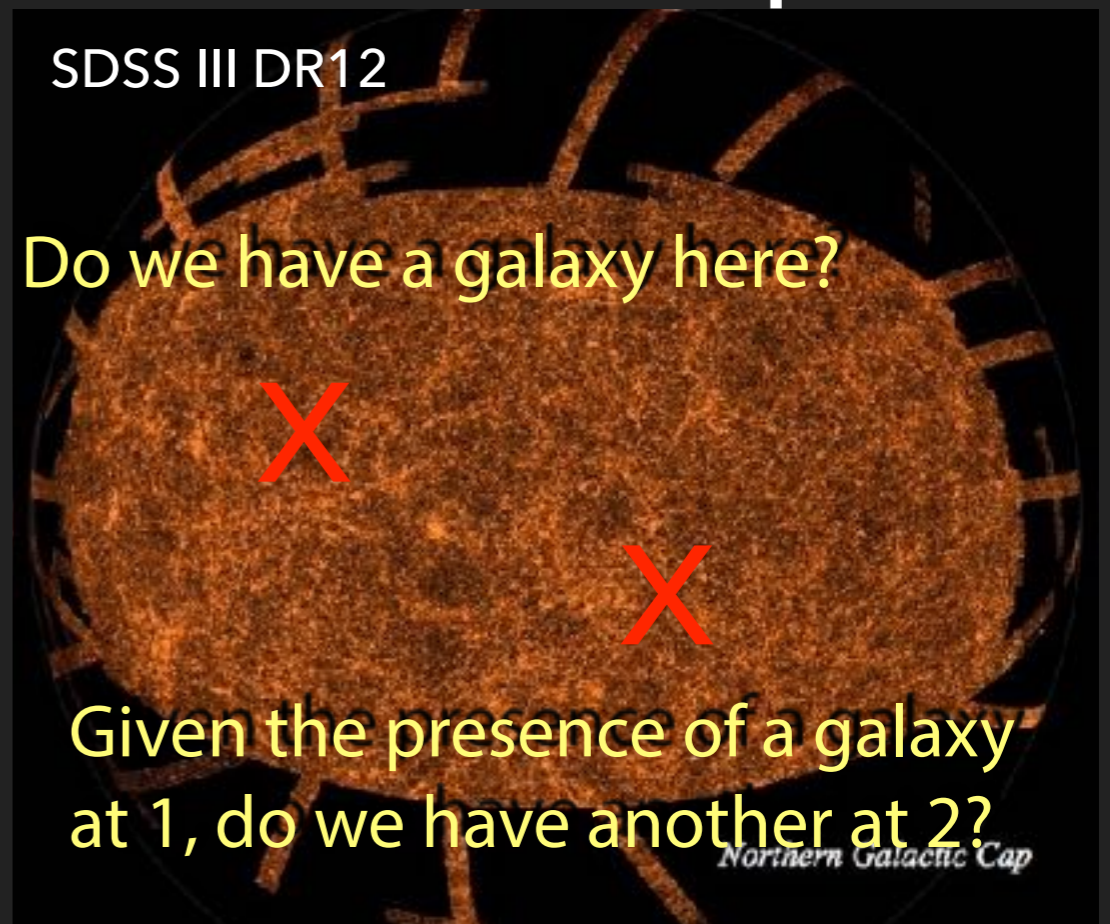
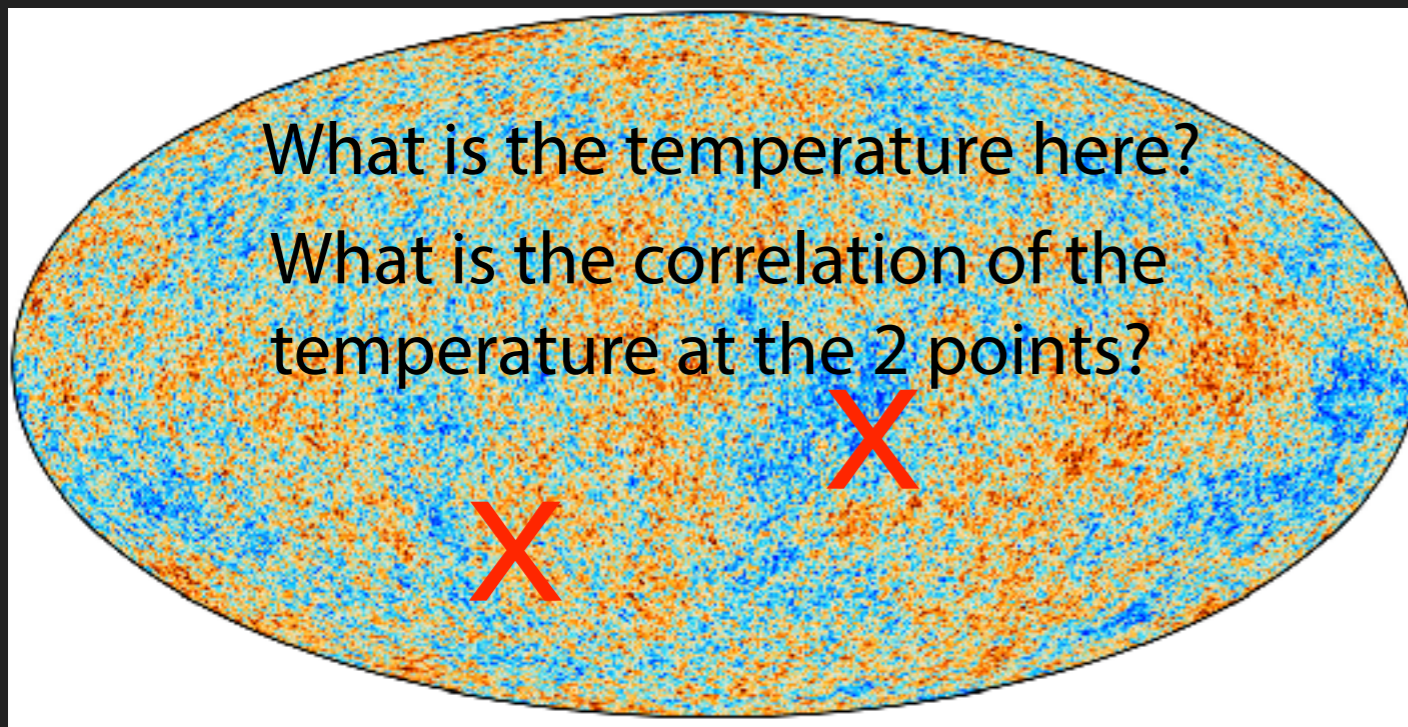
- ▶  $P[\delta_A(x_1)] = P[\delta_A(x_2)] = \dots = P[\delta_A(x_N)]$
- ▶  $P[\delta_A(x_1), \delta_A(x_2)] \neq P[\delta_A(x_1)] P[\delta_A(x_2)]$

position      time

$$\langle A(\mathbf{x}, t) \rangle = A(t)$$

$\langle \dots \rangle$ : ensemble average  
equivalent to spatial average

**correlation between positions !**



# GAUSSIAN RANDOM FIELD AS THE INITIAL CONDITION

## ▶ Gaussianity

- ▶ consider N-point correlators:

$$\langle \delta_A(\mathbf{x}_1) \delta_A(\mathbf{x}_2) \dots \delta_A(\mathbf{x}_N) \rangle_c = 0, \quad \text{for } N \geq 3$$

- ▶ The *2-point correlation function* determines everything:

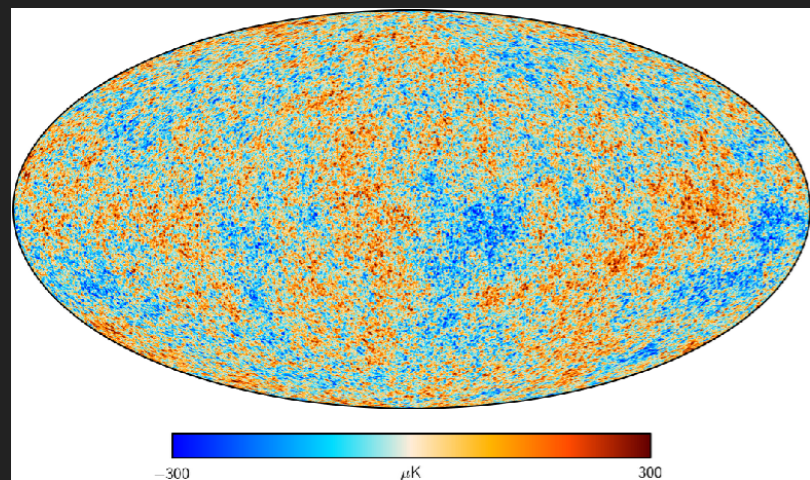
$$\langle \delta_A(\mathbf{x}_1) \delta_A(\mathbf{x}_2) \rangle = \xi_A(\mathbf{x}_1, \mathbf{x}_2) = \xi_A(|\mathbf{x}_1 - \mathbf{x}_2|)$$

↑  
statistical isotropy

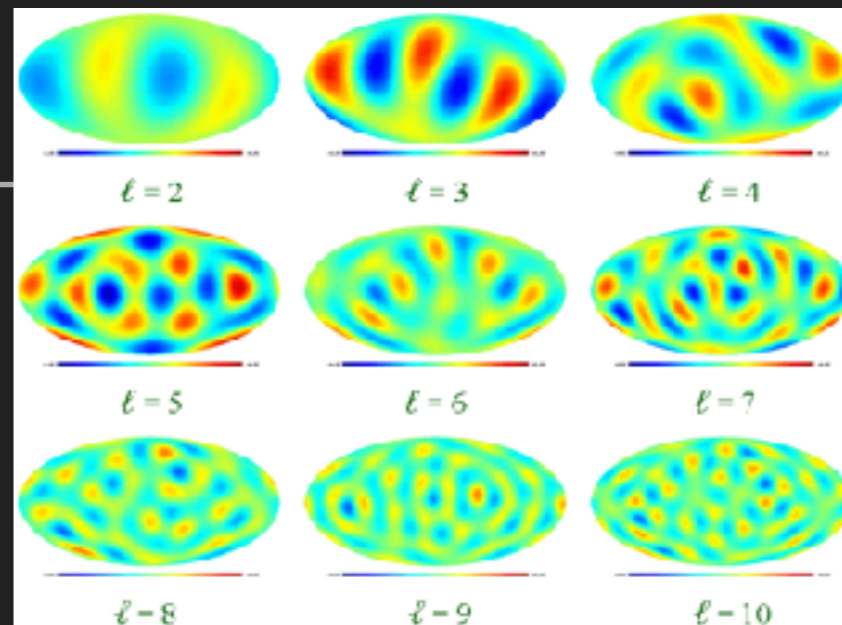
- ▶ or equivalently, the *power spectrum* in Fourier space or in harmonic space
- ▶ In terms of joint probability density functional, this gives

$$P[\delta_A] \propto \exp \left[ -\frac{1}{2} \int d^3x \int d^3x' \delta_A(\mathbf{x}) \xi_A^{-1}(\mathbf{x}, \mathbf{x}') \delta_A(\mathbf{x}') \right]$$

# STATISTICS OF CMB



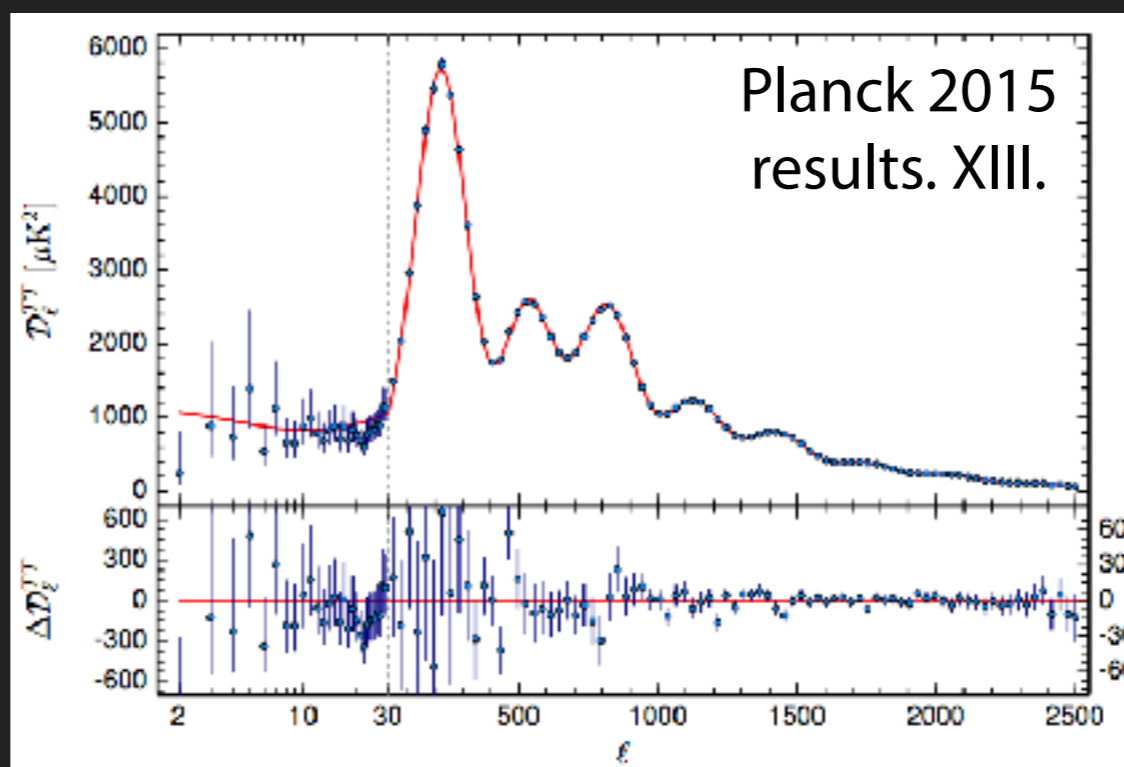
2pt statistics



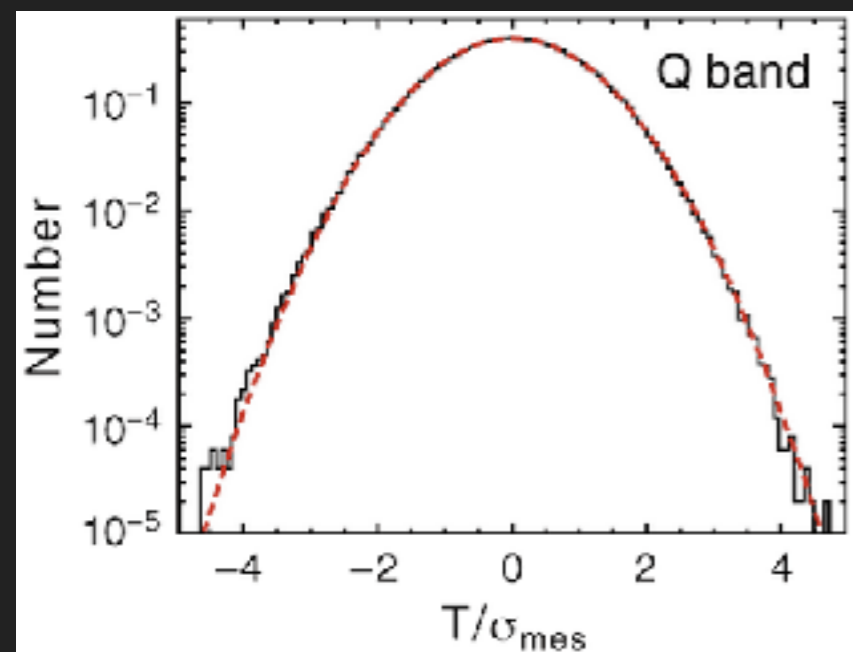
spherical harmonics expansion



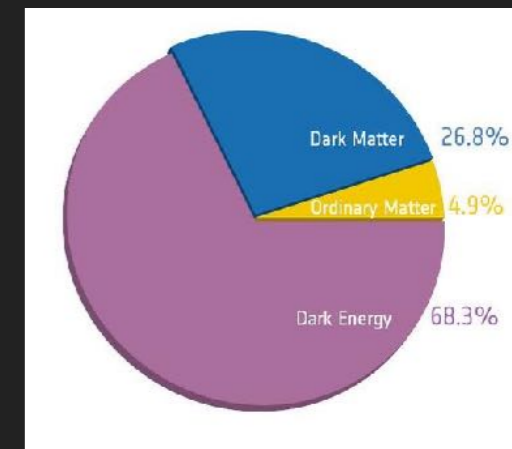
"power spectrum"



1pt probability distribution

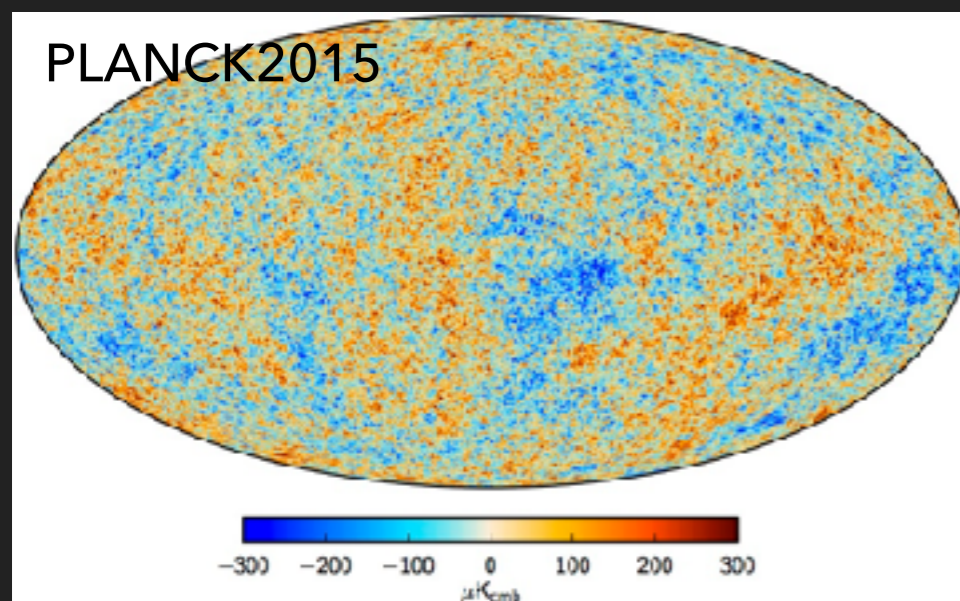
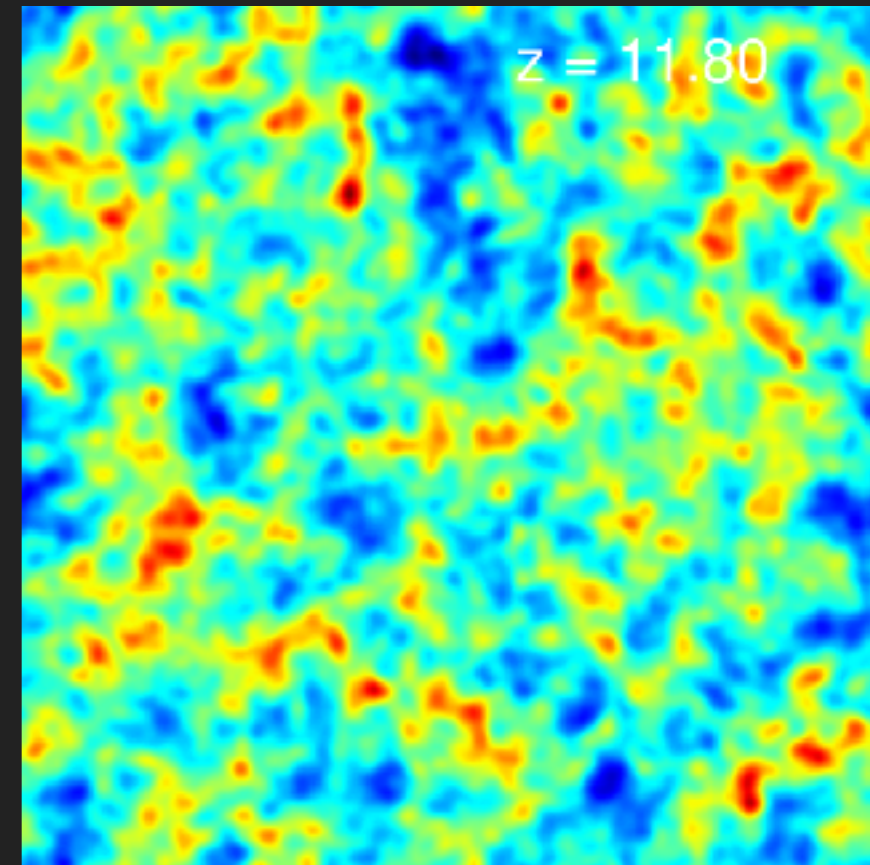


Gaussian Random Field to a very good accuracy (non-Gaussianity < 0.1%)

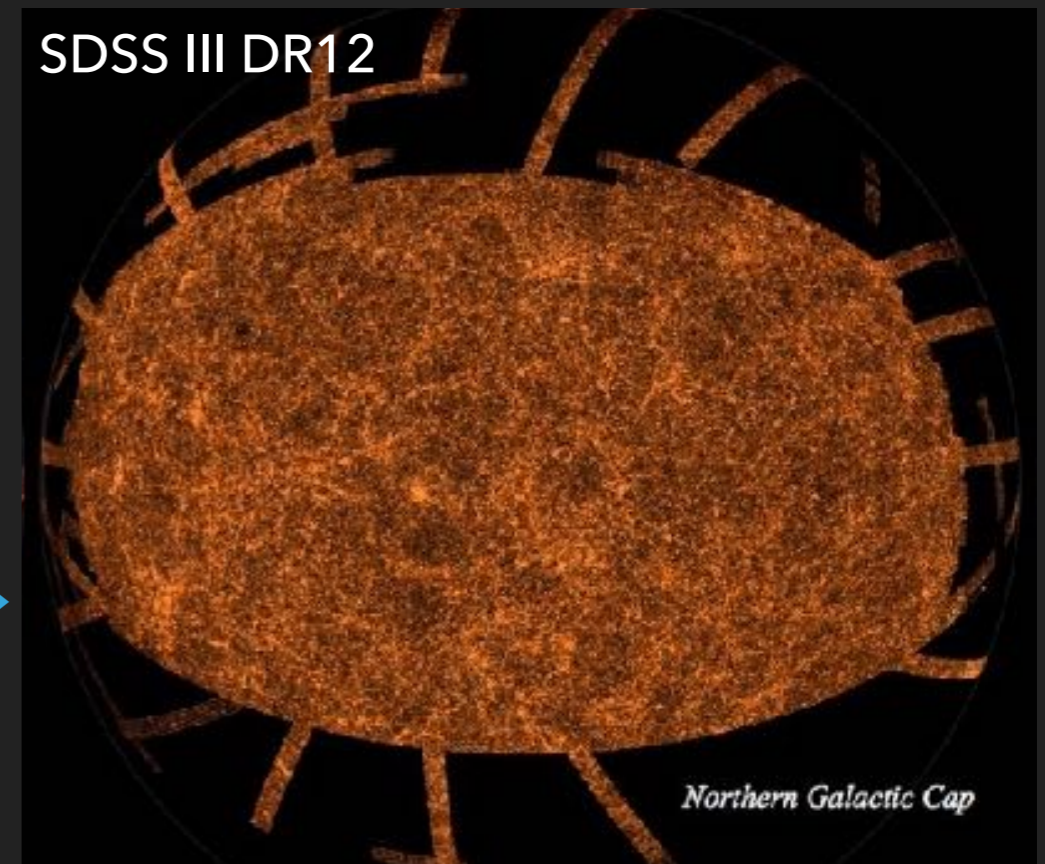
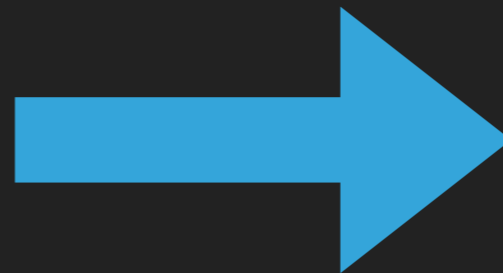


# EVOLUTION OF COSMIC FLUCTUATIONS

- ▶ Gravitational instability is the driver that forms rich cosmic structures
  - ▶ tiny primordial fluctuations seen in the CMB are the seed for the nearby structures
  - ▶ Amplified by gravitational instability over the cosmic time
  - ▶ Any astronomical structures (stars, galaxies, groups, clusters) originated from this!

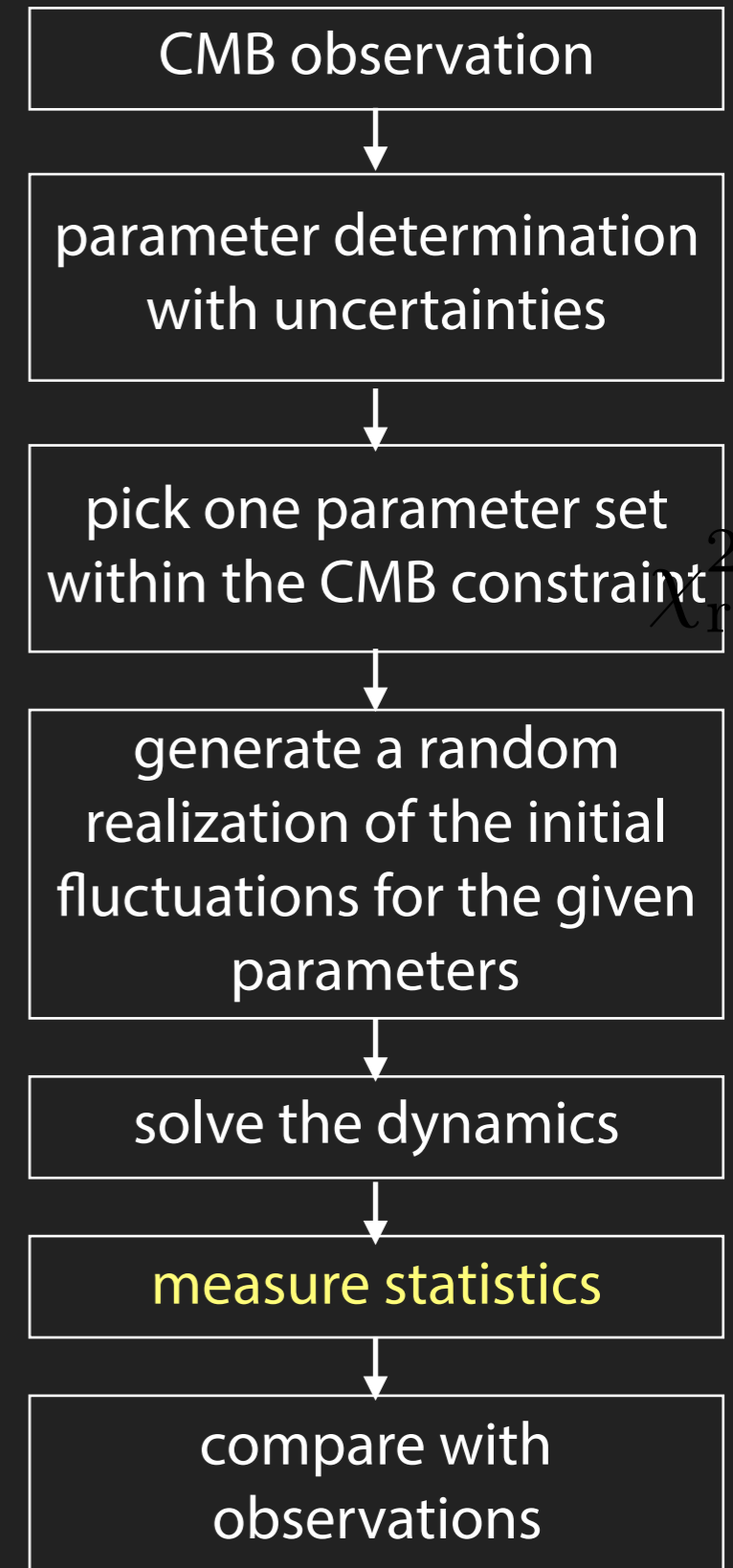
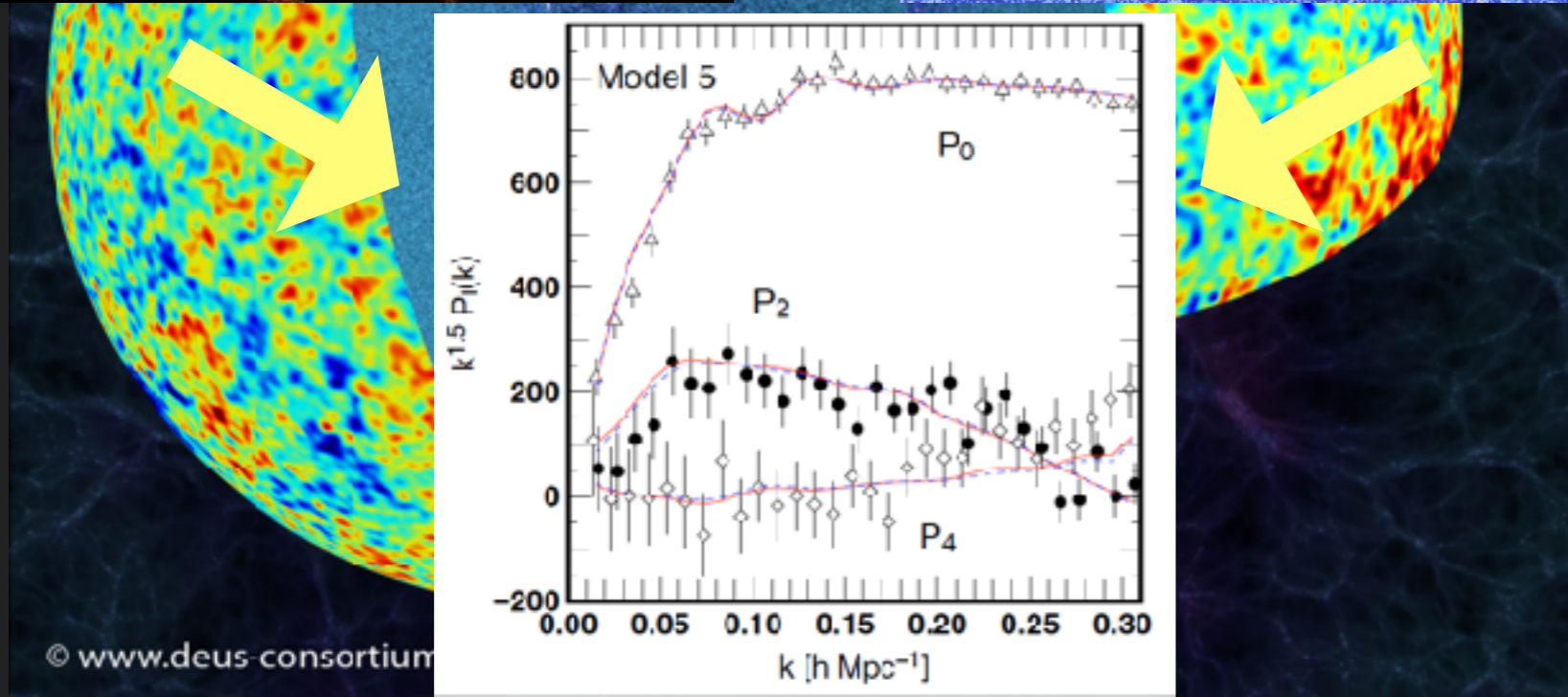
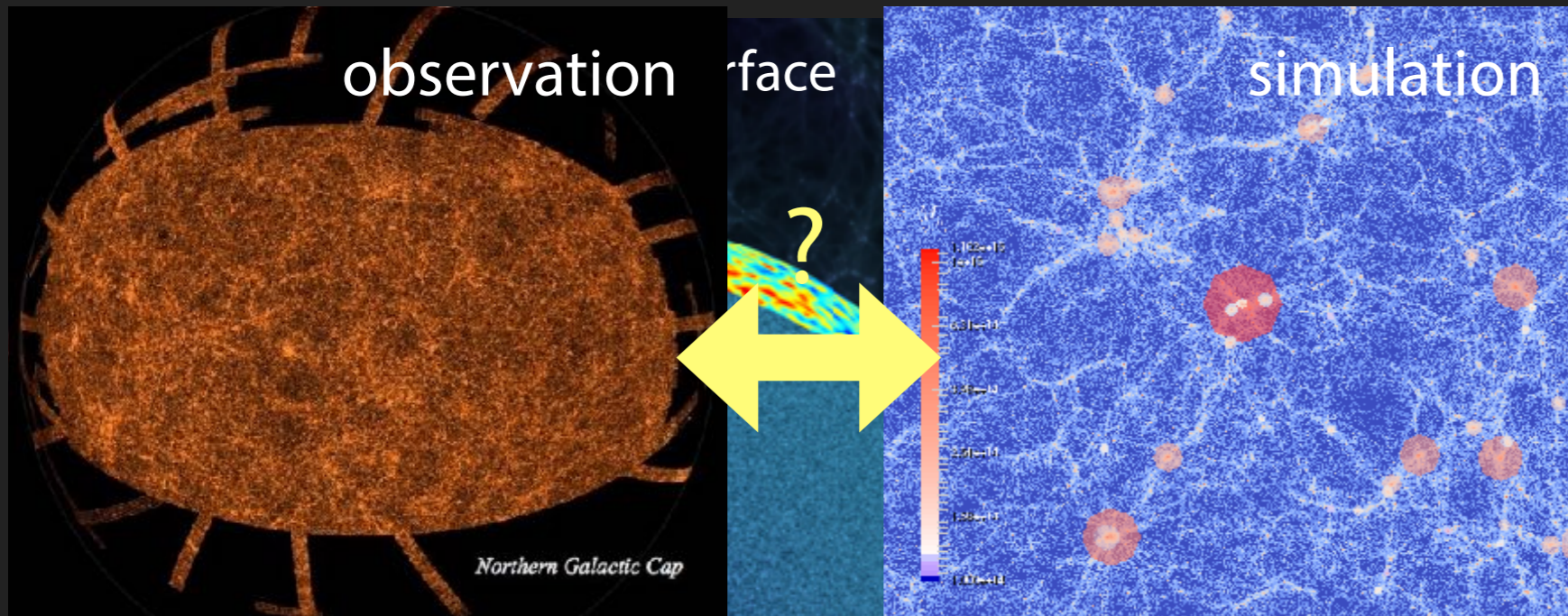


Gravity



# EVOLUTION OF COSMIC FLUCTUATIONS (CONTD)

- ▶ We do not have the information on the initial condition sufficient for full determination of the *particular random realization* in which we live!

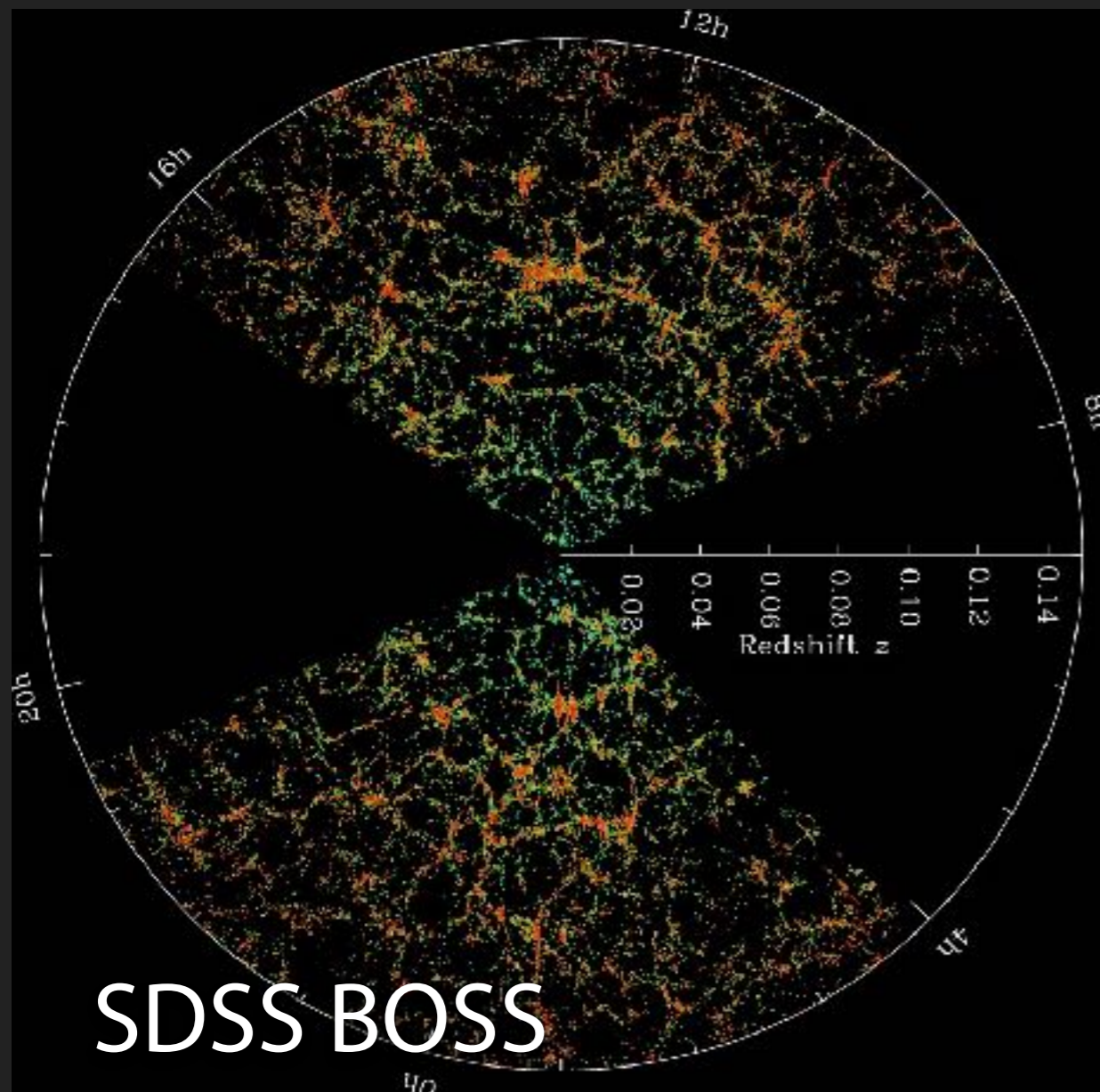


# LATE-TIME OBSERVABLES

# TARGET OBSERVABLES

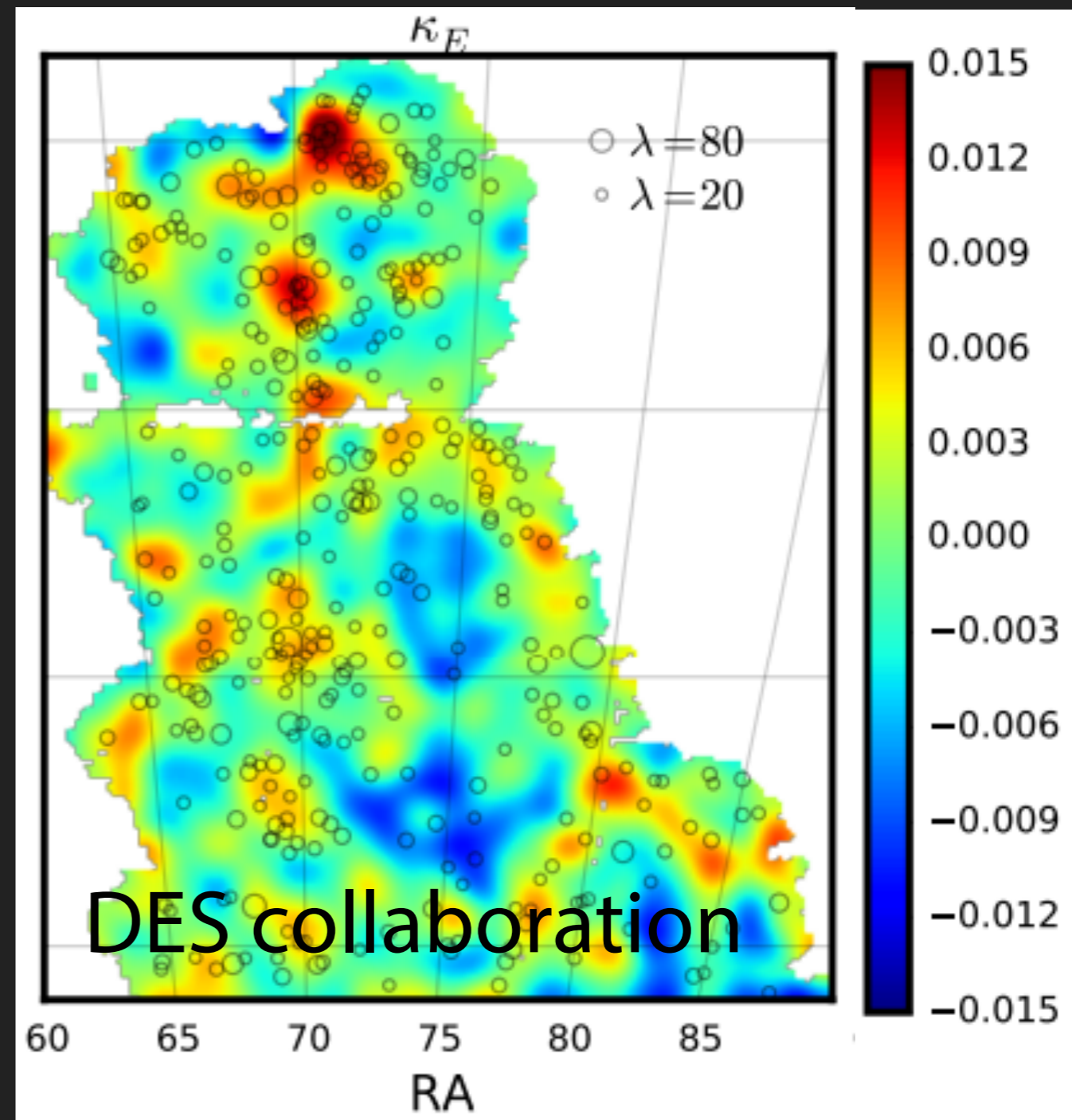
## Galaxy clustering

in point process in 3D space



## weak gravitational lensing

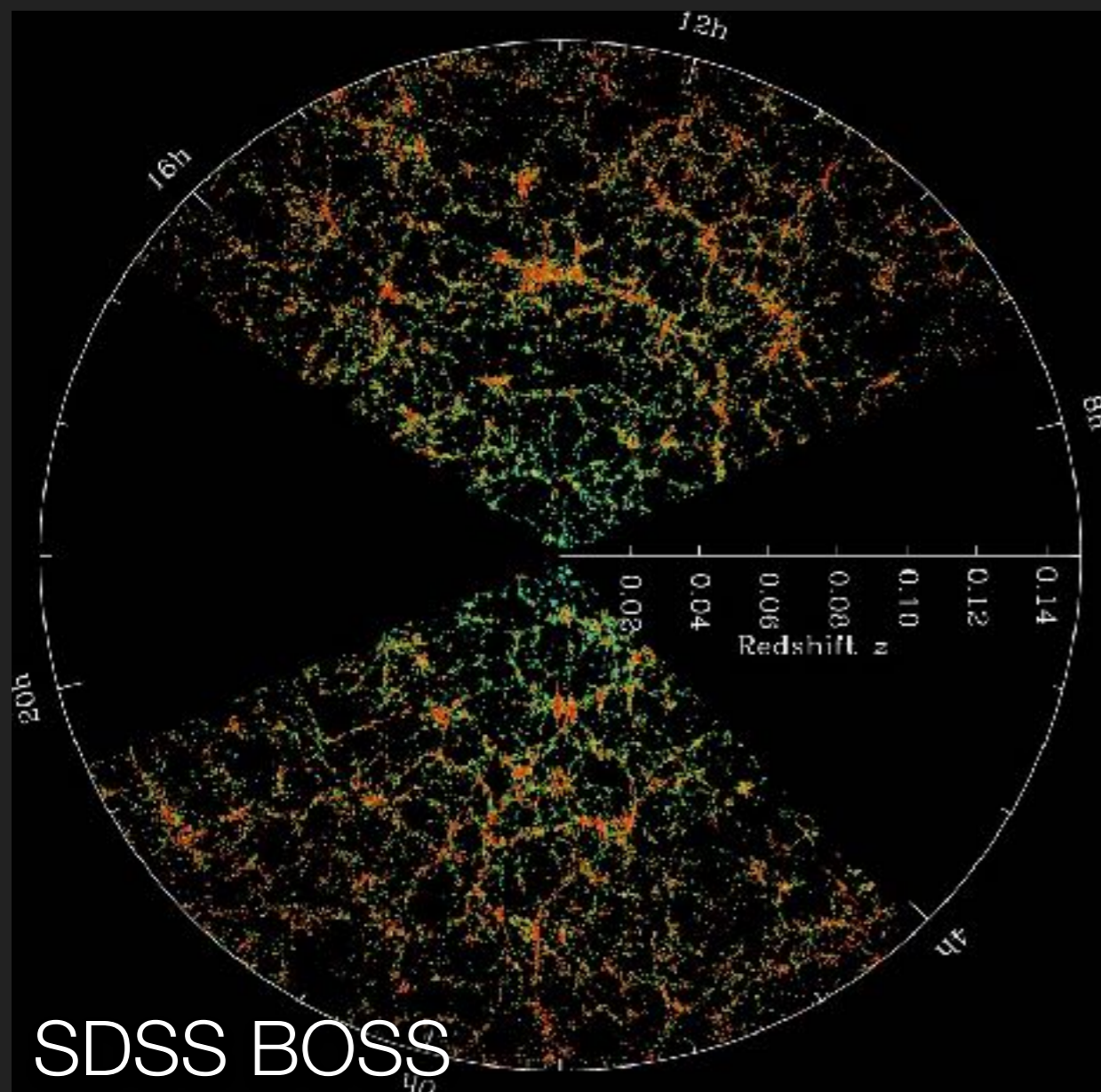
projected mass distribution on 2D plane



# TARGET OBSERVABLES

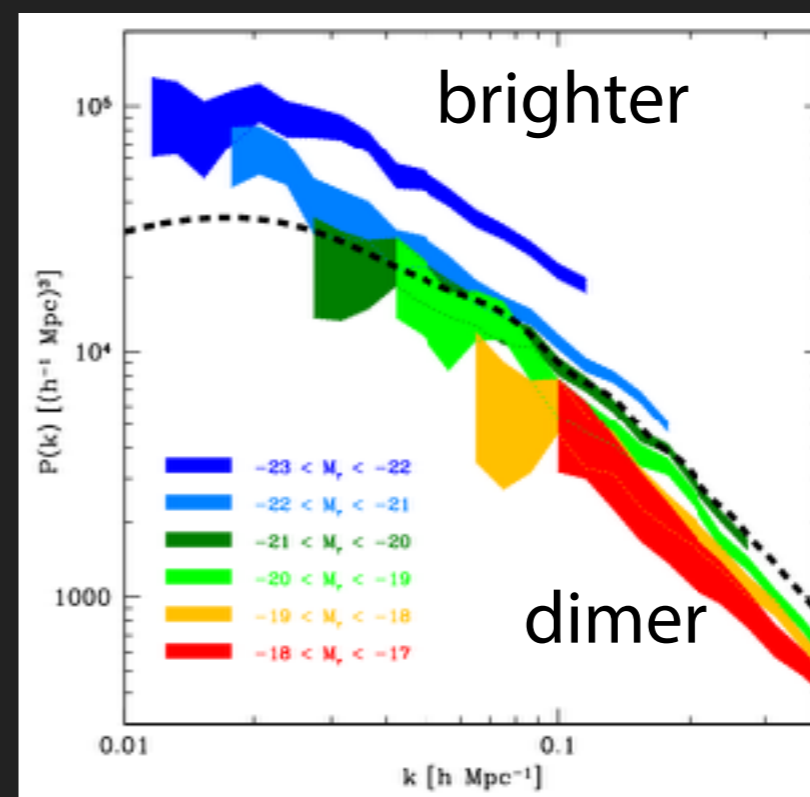
## Galaxy clustering

in point process in 3D space



- ▶ Basic quantity = Positions
- ▶ Additional quantities
  - ▶ characteristic of galaxies
  - ▶ luminosity, color, morphology ...

We do not know the relation between the mass density field and galaxy density field! (galaxy bias uncertainty)

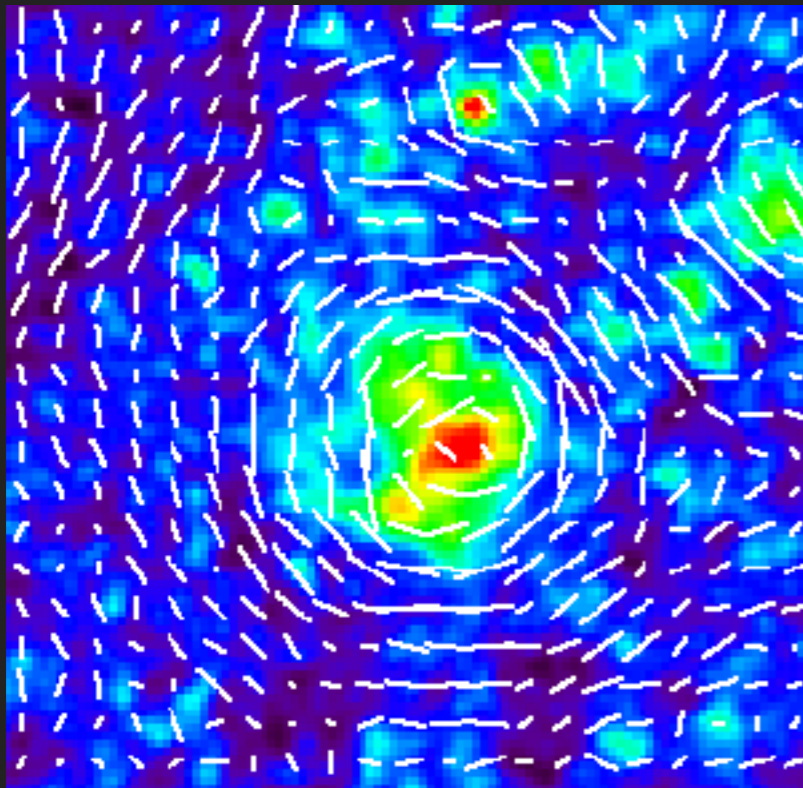


*galaxy power spectra*

Tegmark+'04



# TARGET OBSERVABLES

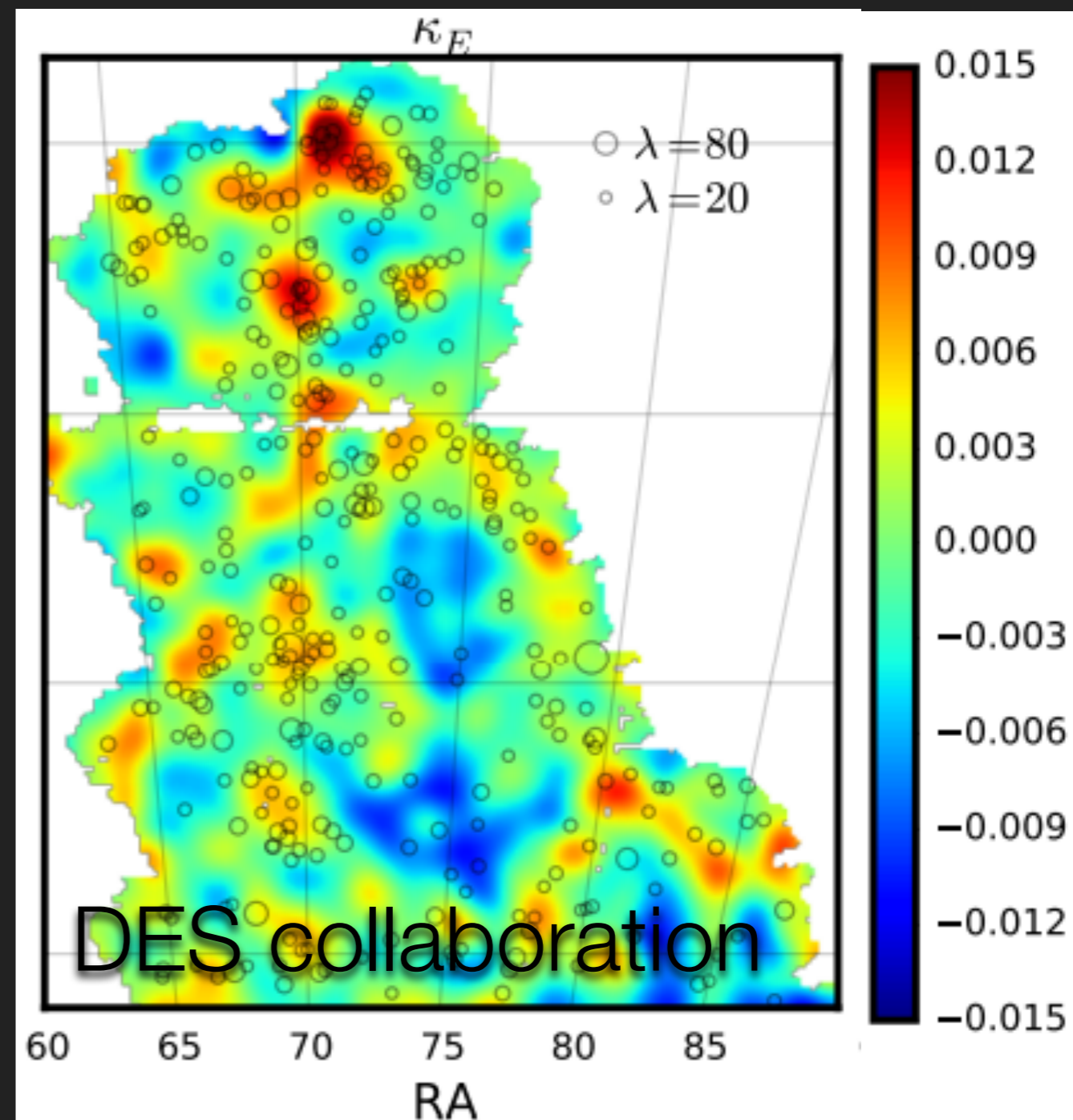


simulation by T. Hamana @ NAOJ

ticks = expected orientation of galaxies

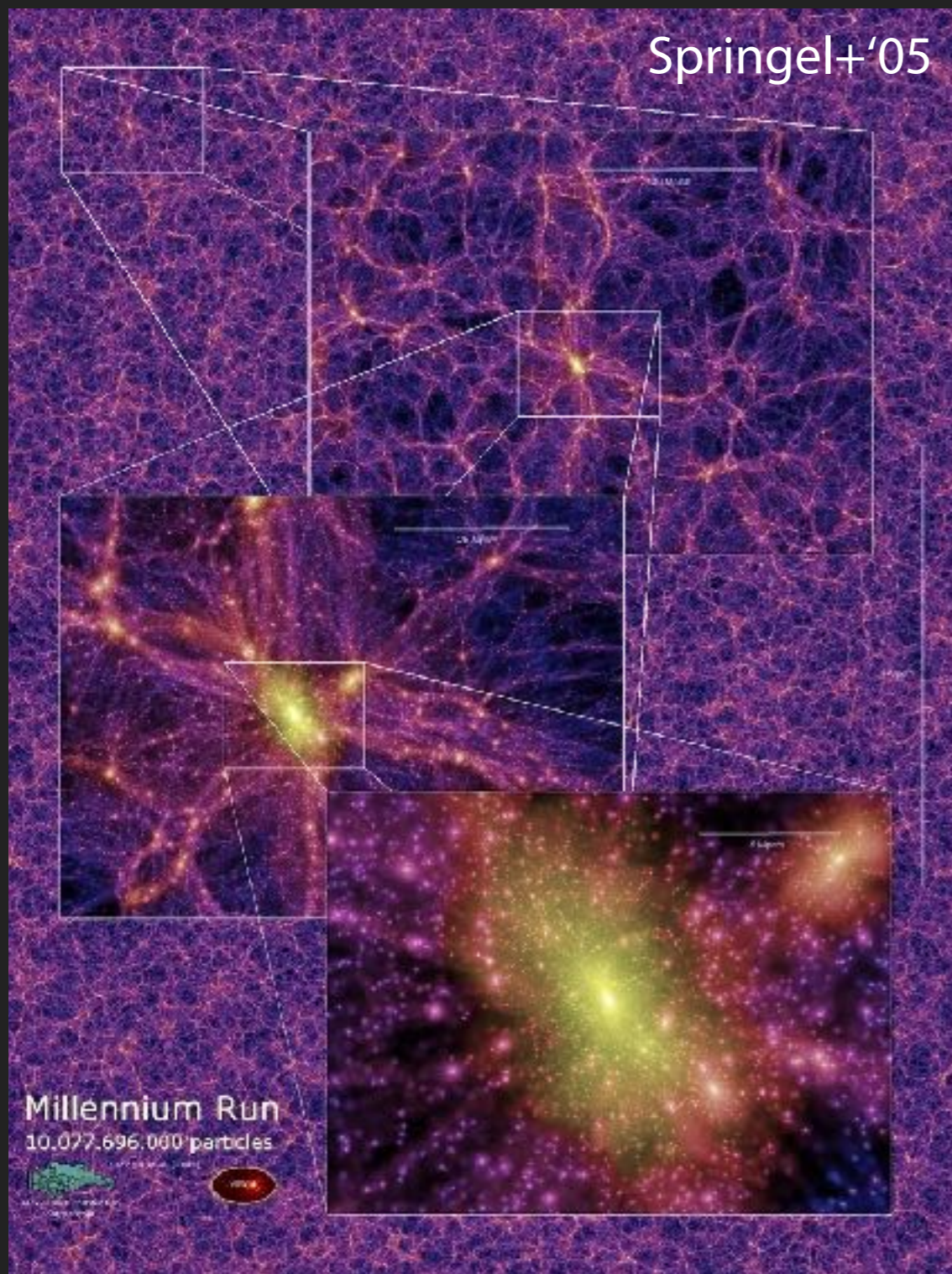
- ▶ **direct observable**
  - ▶ shape of background galaxies
- ▶ **accessible information**
  - ▶ foreground projected mass map
  - ▶ including *dark matter*

weak gravitational lensing  
projected mass distribution on 2D plane

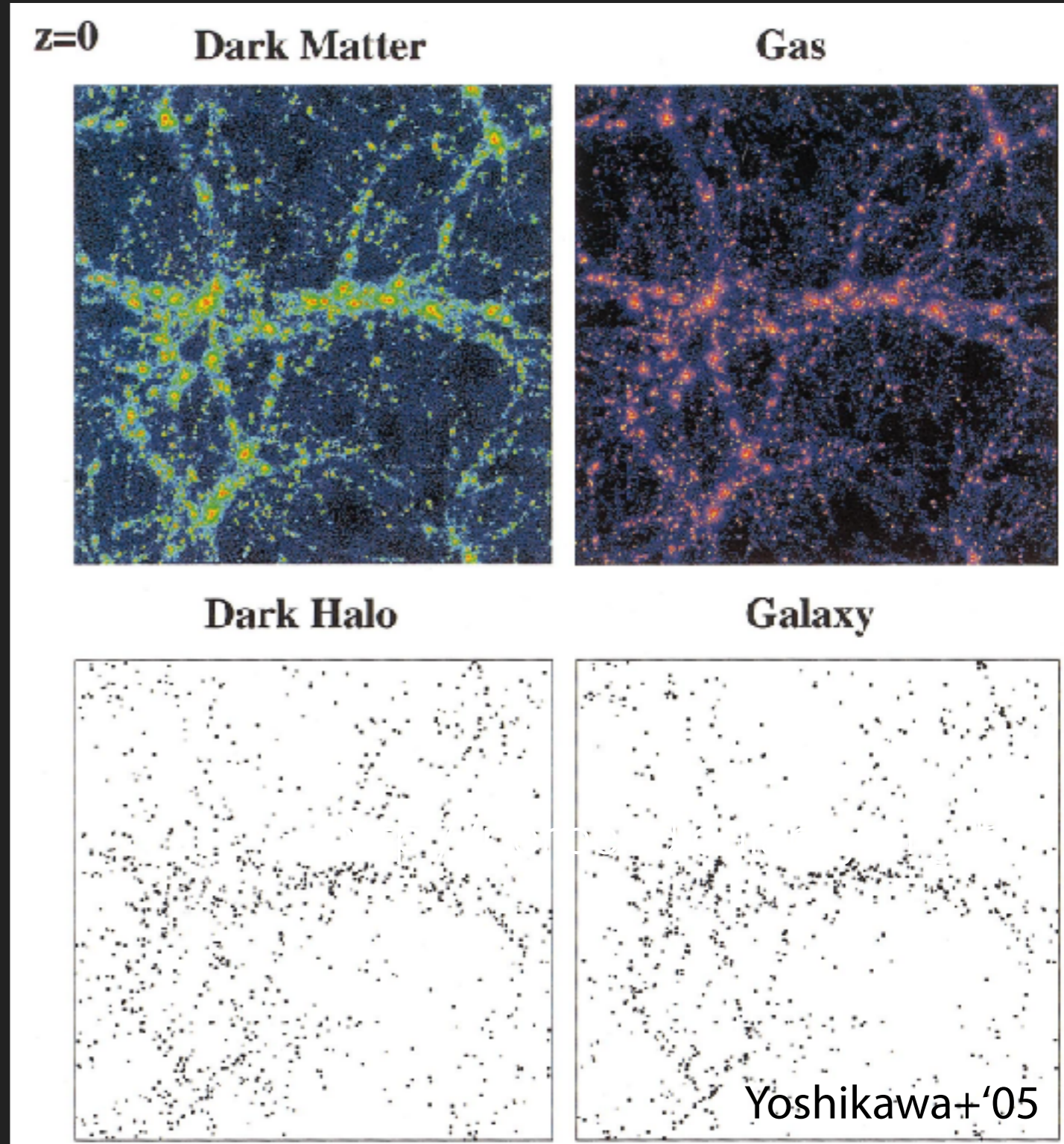


# WHAT WE CAN AND CANNOT PREDICT

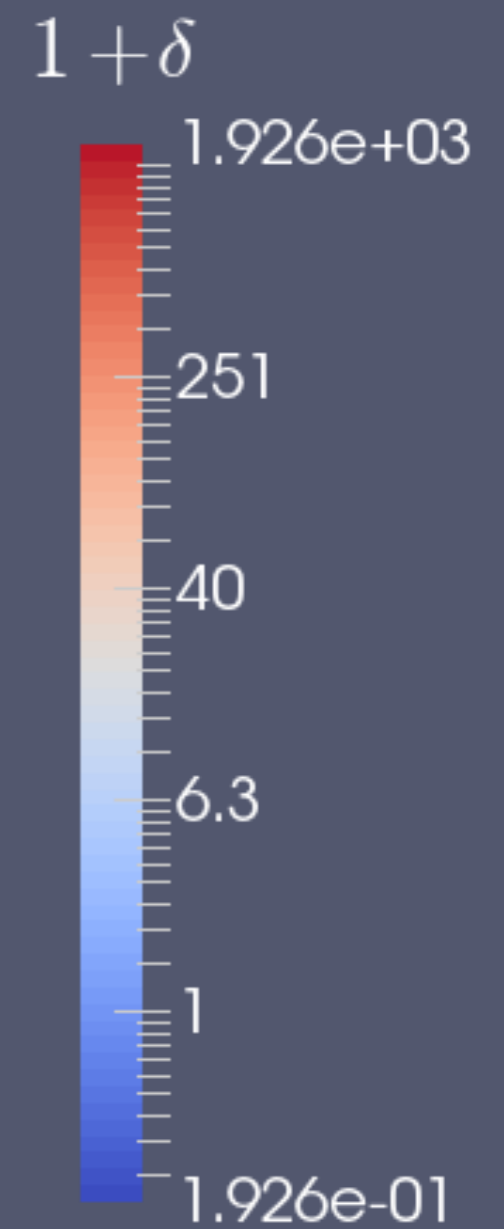
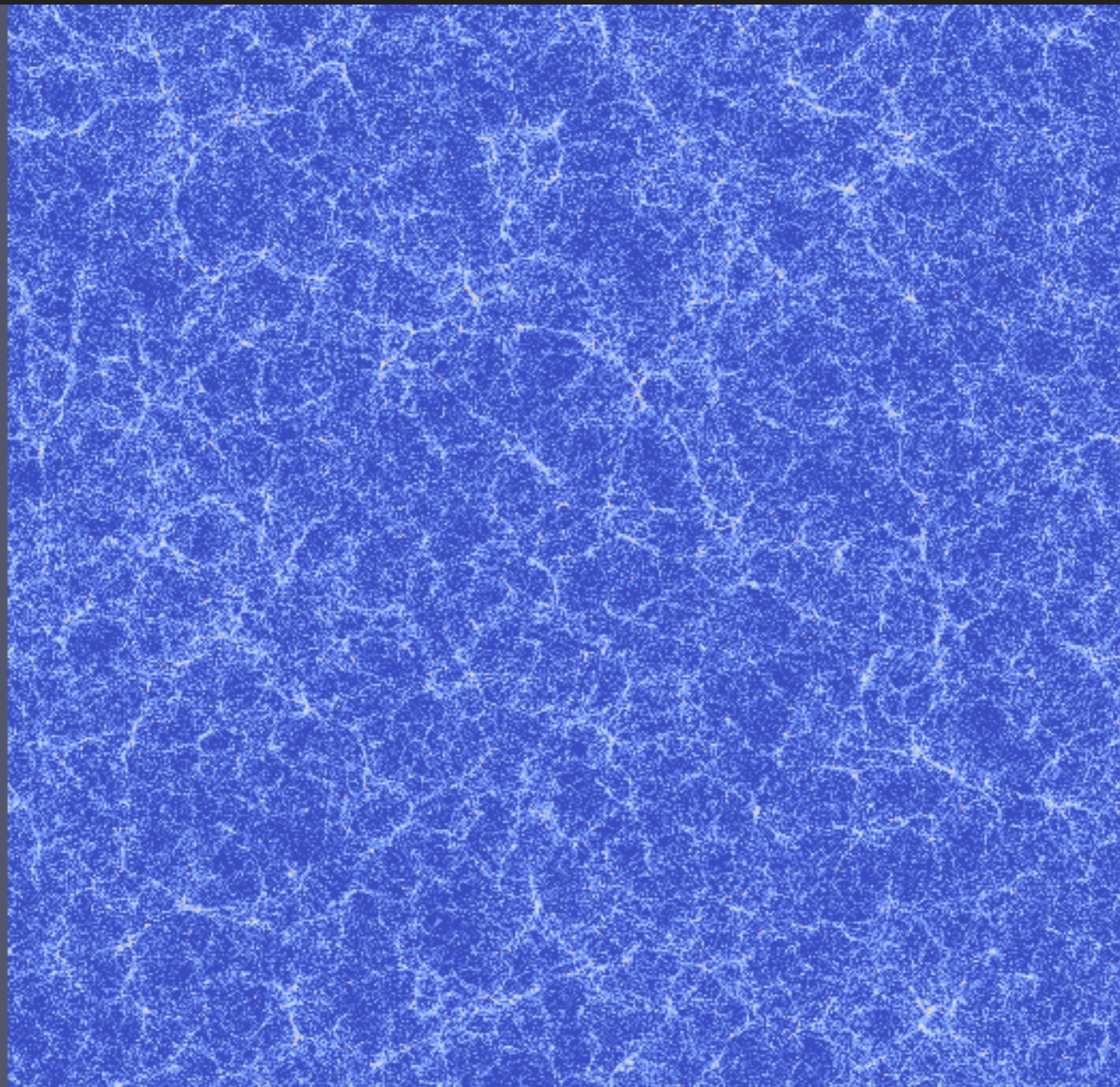
gravity only simulation



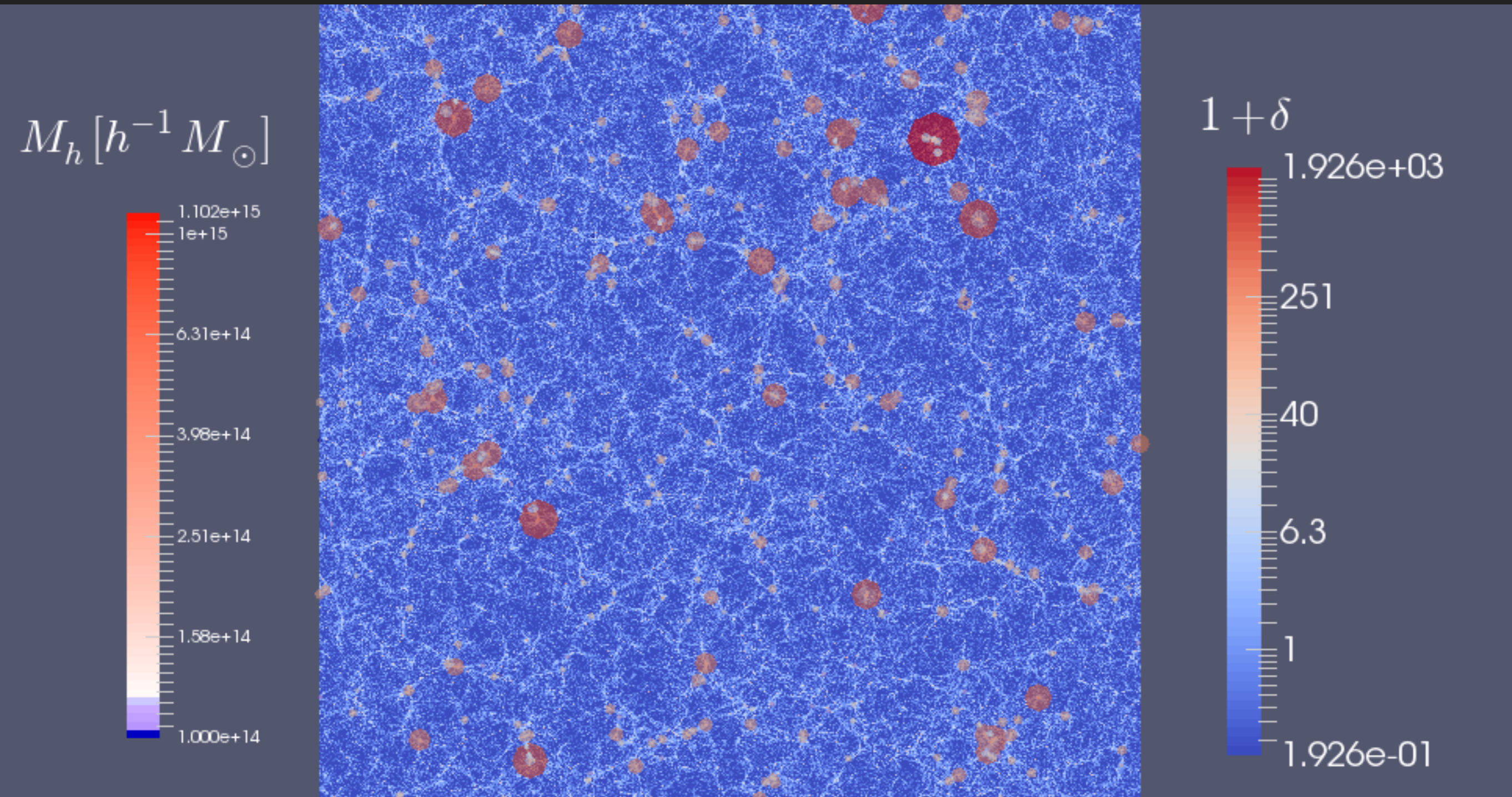
hydrodynamical simulations with various processes



# 2D SLICE OF COSMIC STRUCTURE

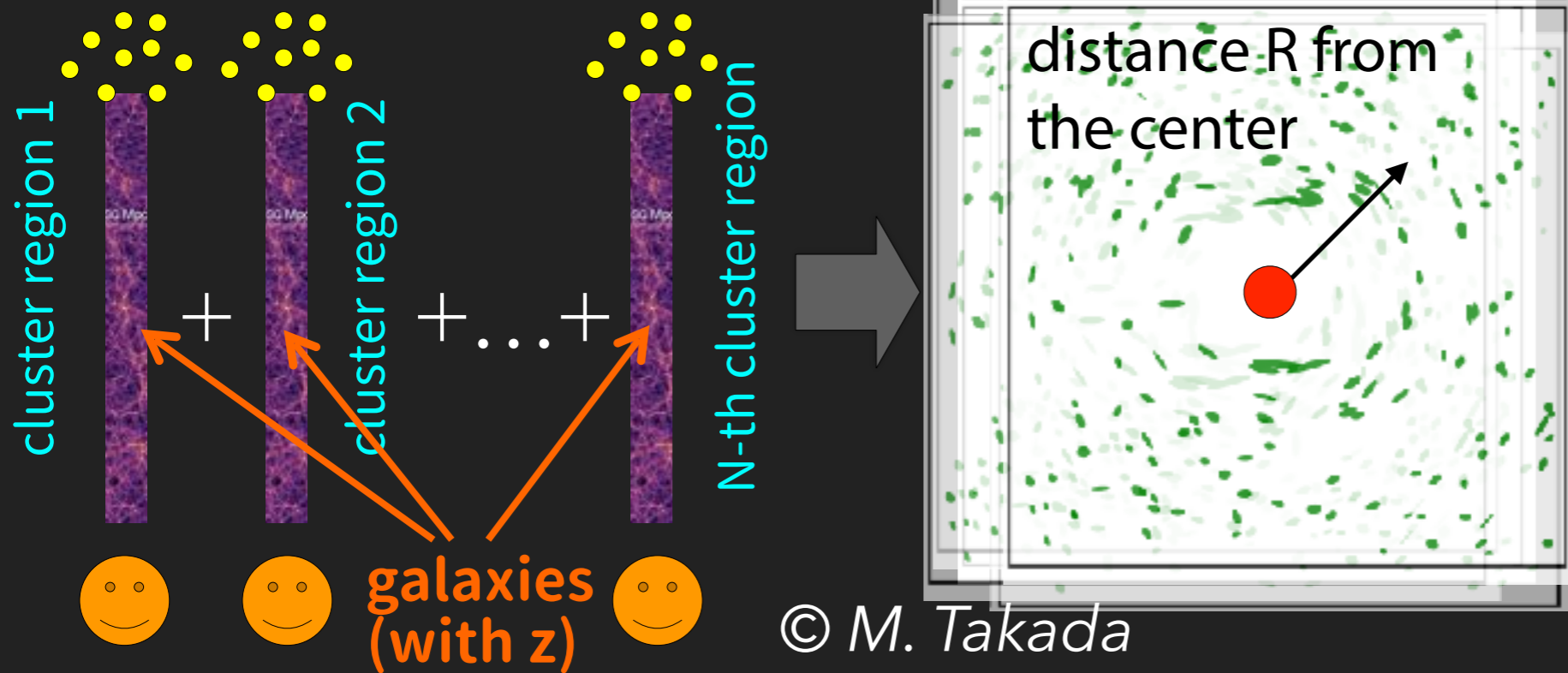


# 2D SLICE OF COSMIC STRUCTURE



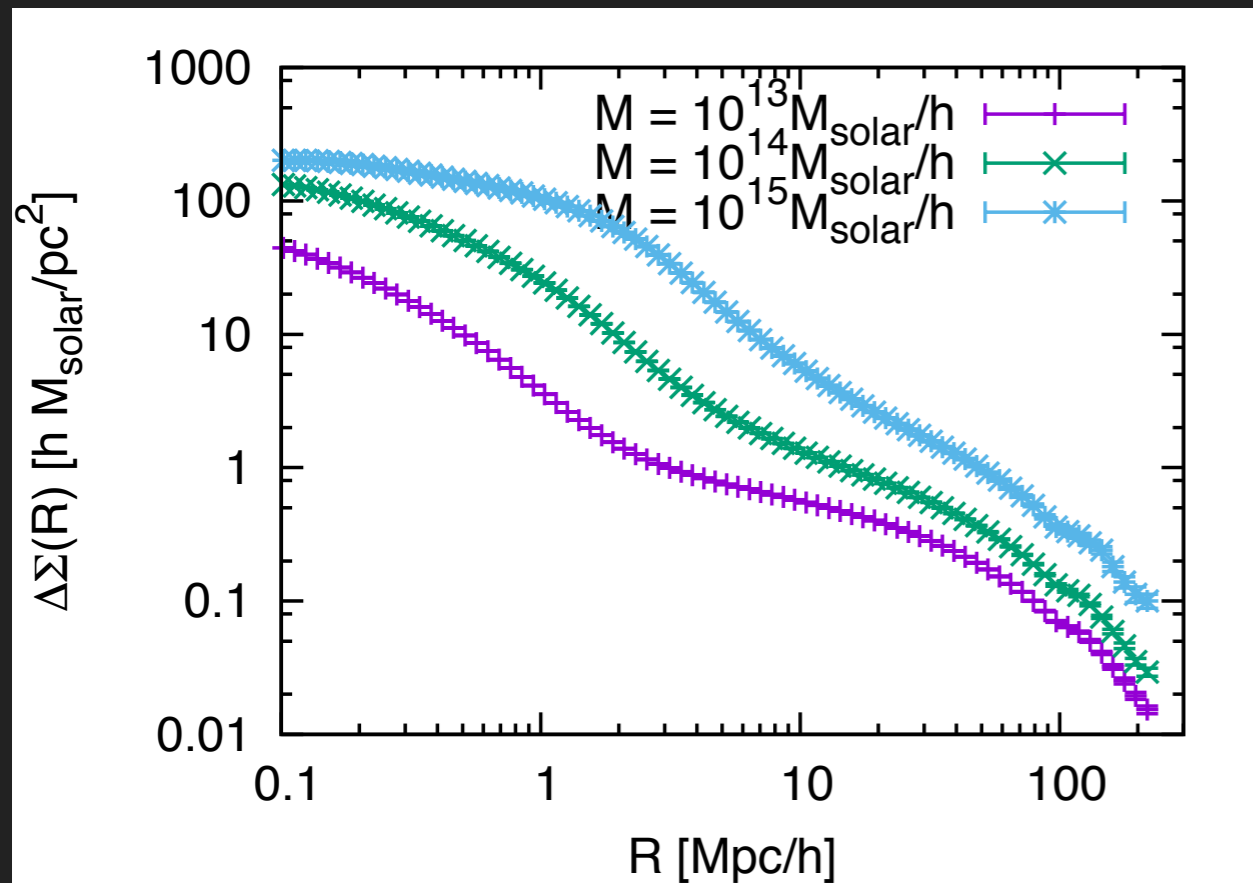
Need an accurate theoretical template as a function of the mass of halos

# GALAXY-GALAXY LENSING



e.g., Oguri & Takada '11

stack the images of background galaxies centered at the foreground cluster positions



The cross-correlation signal of the two observables

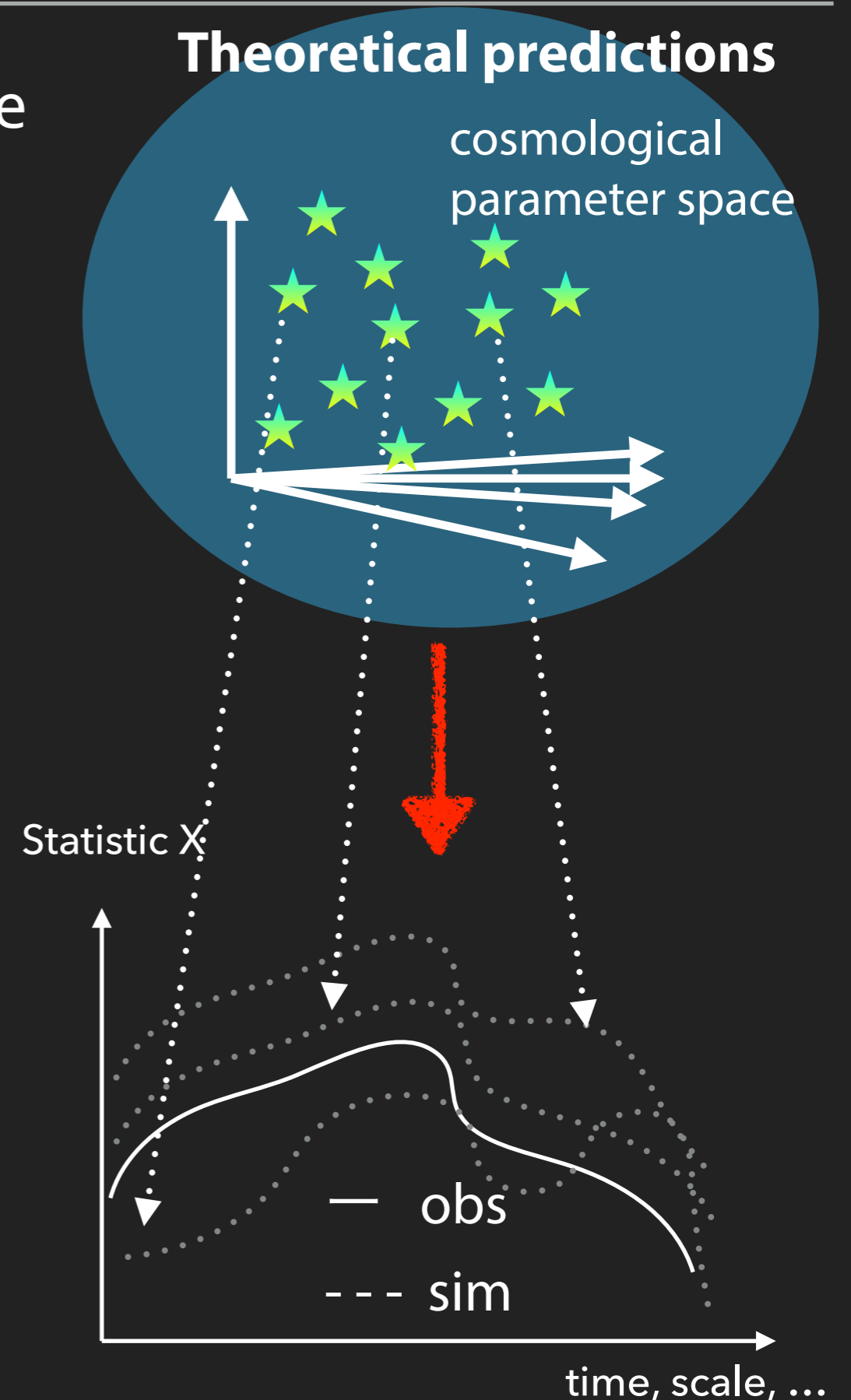
$$\Sigma(R) = \bar{\rho} \int \left[ 1 + \xi_{\text{gm}} \left( \sqrt{R^2 + \Pi^2} \right) \right] d\Pi$$

Break the degeneracy btwn galaxy bias and cosmology!

**DARK EMULATORS**

# OBJECTIVE

- ▶ Numerical cosmology with large-scale structure data
  - ▶ direct confrontation of simulations to observations for model/parameter estimation
- ▶ Accurate determination of basic statistical quantities with N-body simulations
  - ▶ cosmology dependence
  - ▶ machine-learning based approach
- ▶ handy numerical codes for statistical analyses
  - ▶ rapid emulator written in python



# THE SIMULATION DESIGN IN HIGH DIMENSION SPACE

sampling: 21, 22, 12

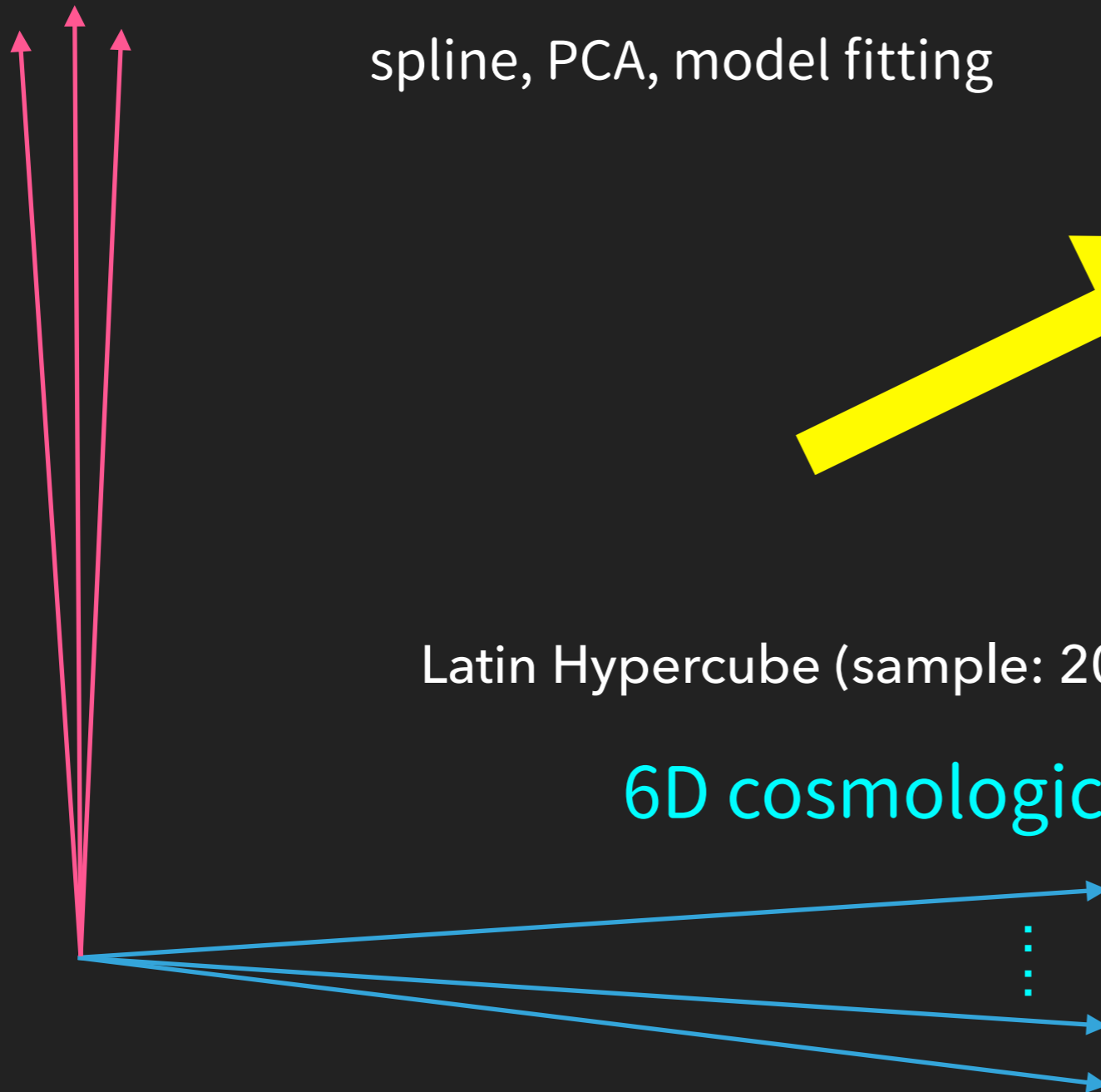
other dependence (time, distance, mass, ...)

spline, PCA, model fitting

Rapid prediction of the statistics in multi-dimensional parameter space for MCMC analyses

Latin Hypercube (sample:  $20+20+1+\alpha$ ) + Gaussian process

6D cosmological parameter space





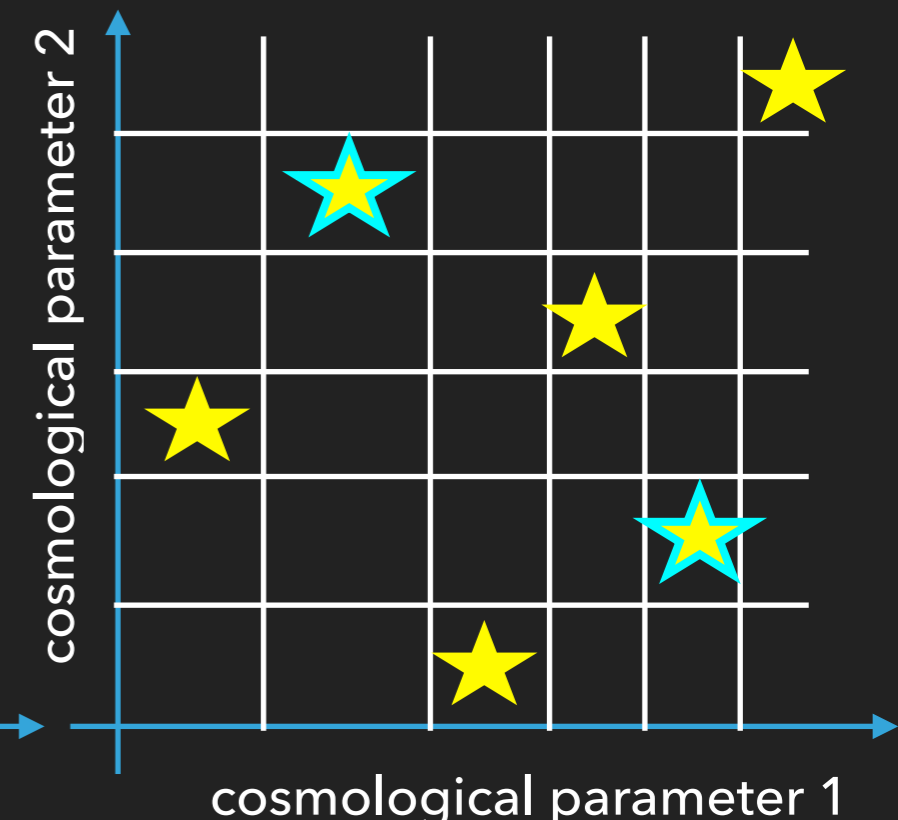
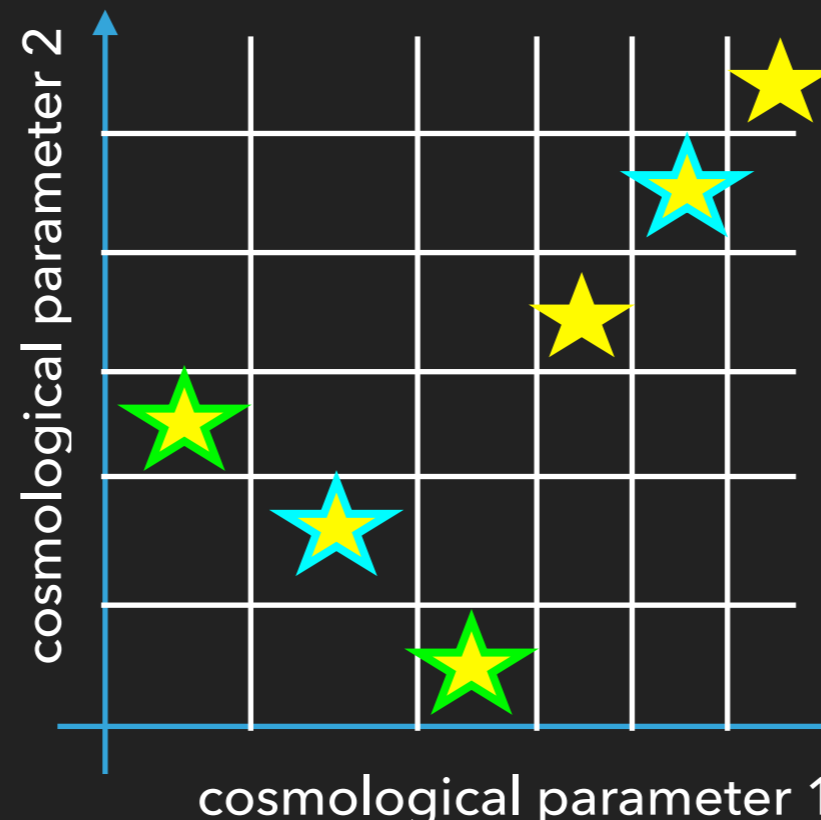
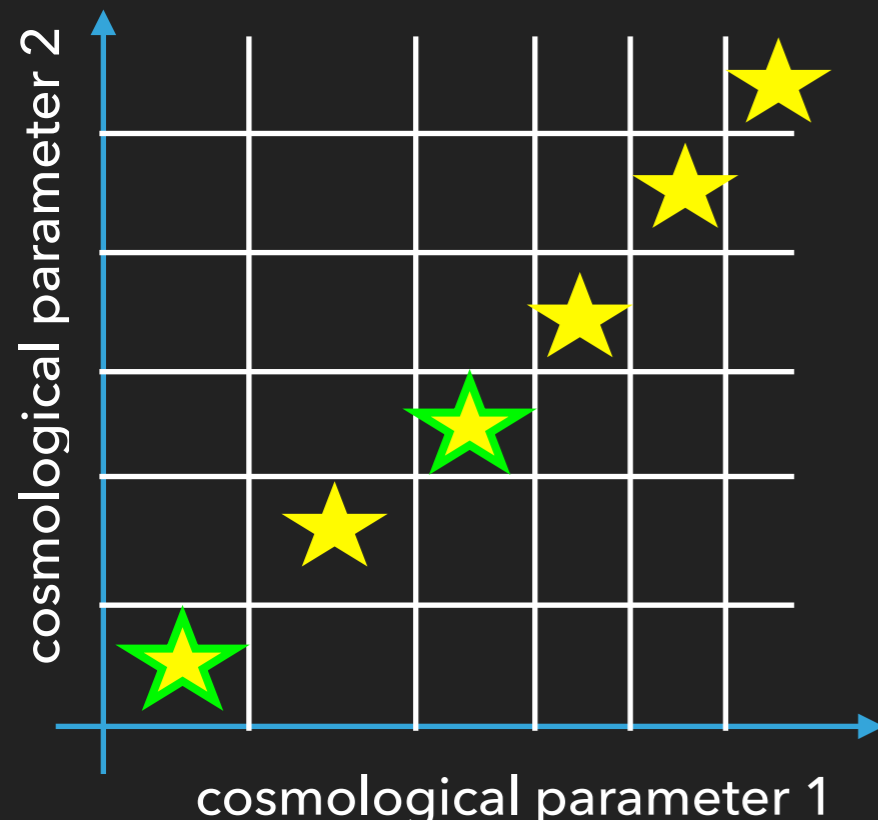
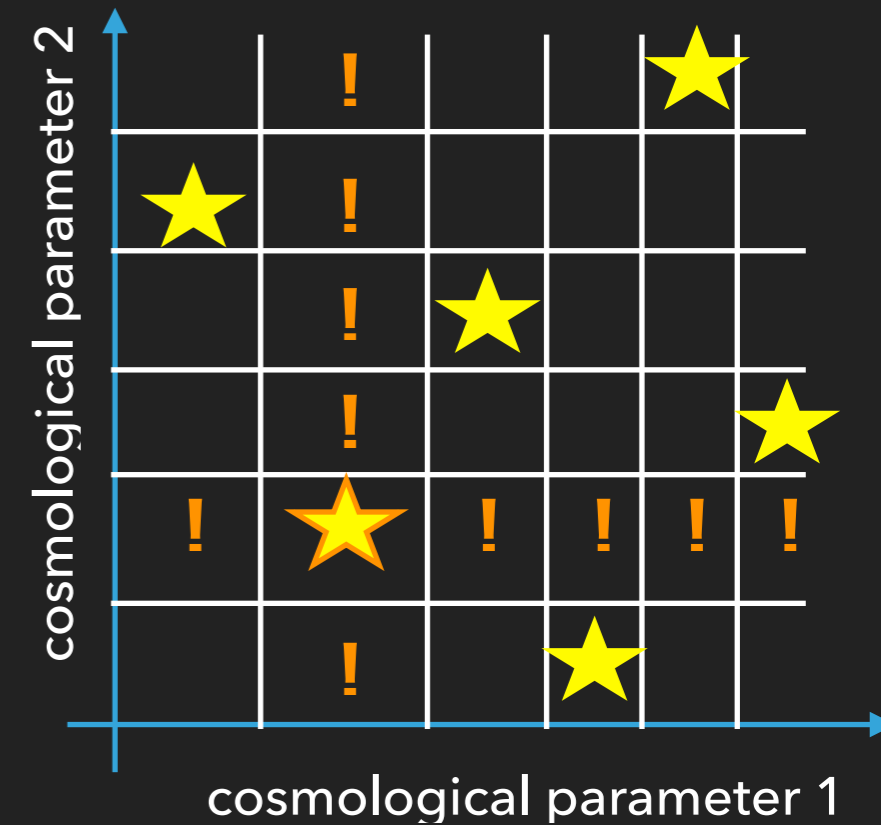
# EFFICIENT SAMPLING SCHEME IN MULTI-DIMENSIONAL SPACE

## ▶ Latin hypercube designs

- ▶ each sample point is the only one in both the row and the column
- ▶ Such a design is not unique (ex. diagonal design)

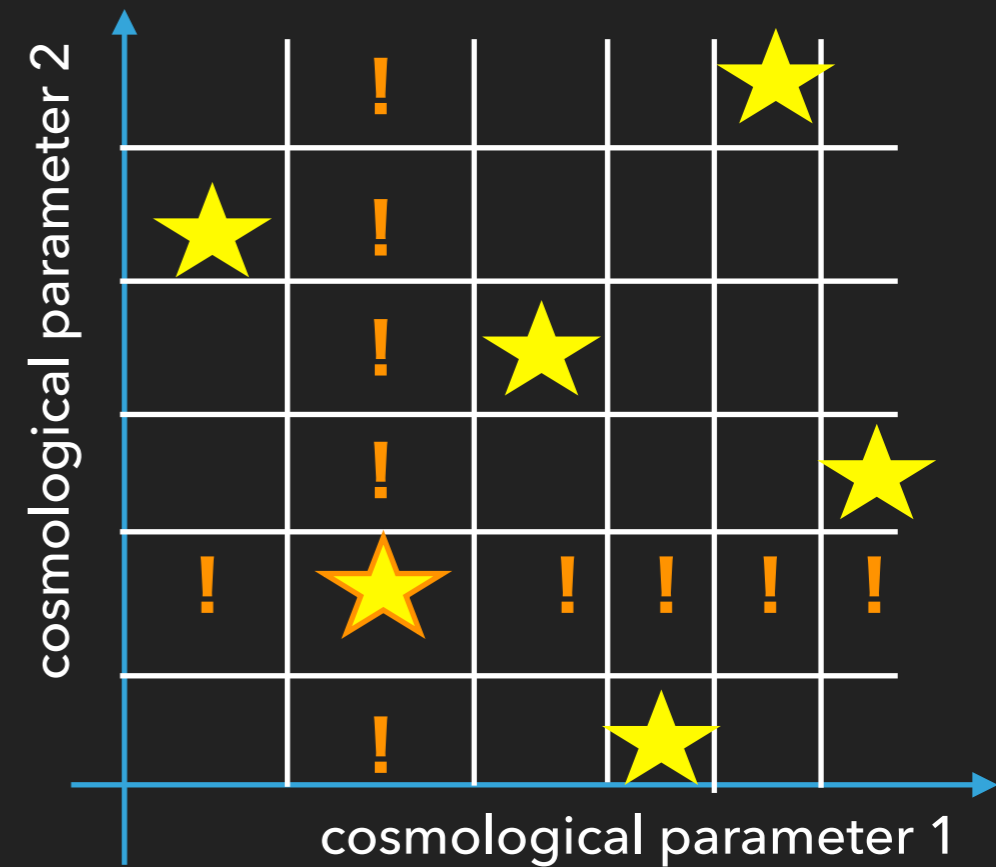
## ▶ Additional constraint: *maxi-min distance design*

- ▶ maximize the sum of the distances of nearest neighbors

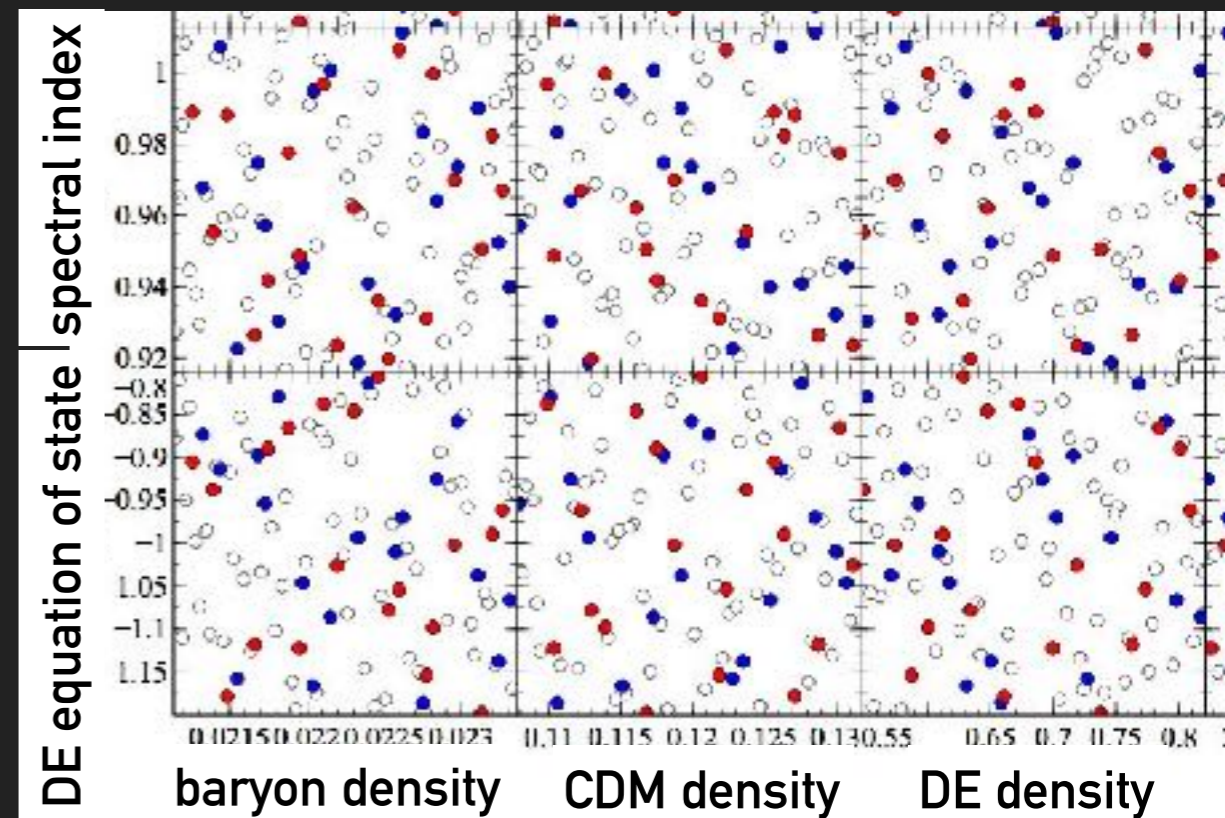


# EFFICIENT SAMPLING SCHEME (CONTD)

- ▶ “Sliced” LHDs
  - ▶ a hierarchical design proposed by Ba, Brenneman&Myers’15
  - ▶ 100 sampling points in total in a LHD
  - ▶ Each of the 20 points are LHDs (e.g., red/blue points)
  - ▶ **Multiple purpose for different slices**
    - ▶ for instance
    - ▶ 20 training set
    - ▶ 20 validation set



$\omega_b = \Omega_b h^2: \pm 5\%$	$\ln(10^{10} A_s): \pm 20\%$
$\omega_c = \Omega_c h^2: \pm 10\%$	$n_s: \pm 5\%$
$\Omega_\Lambda: \pm 20\%$	$w: \pm 20\%$

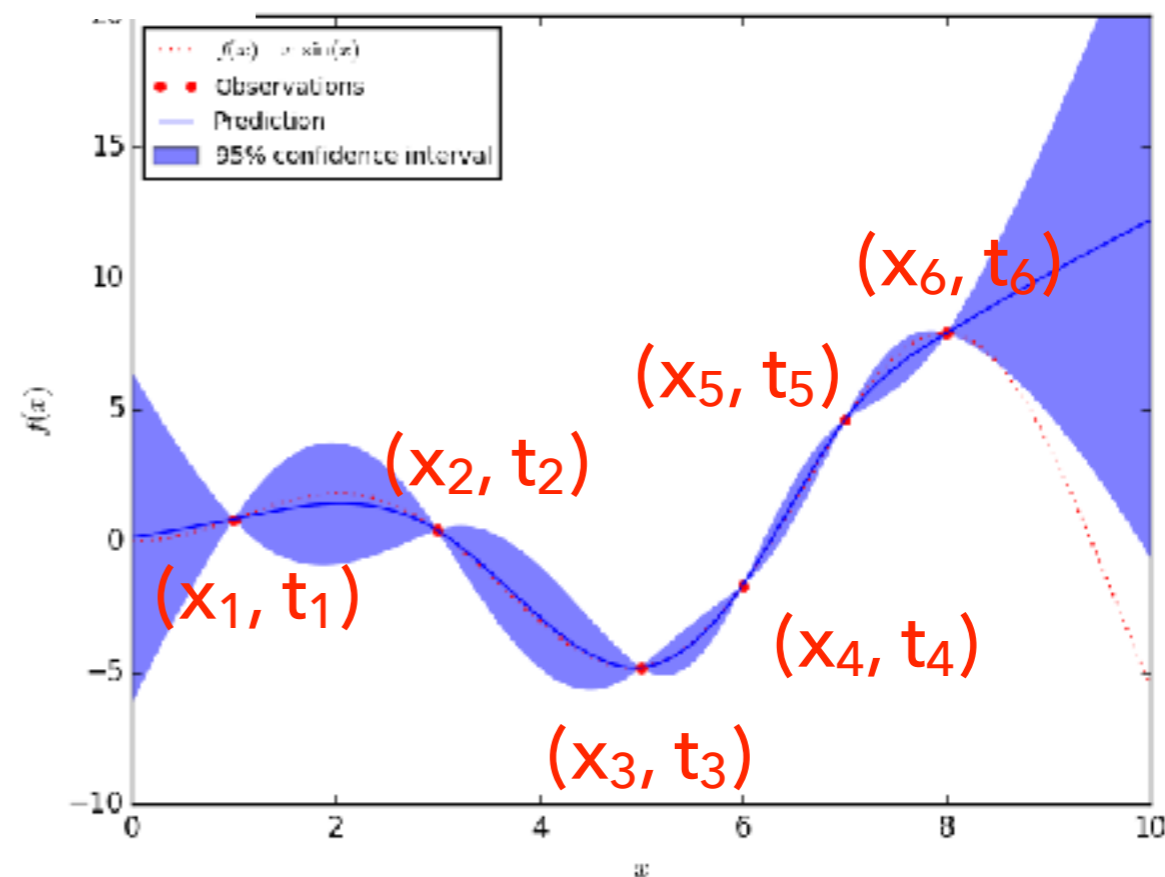


# GAUSSIAN PROCESS

- ✓ A machine-learning technique that interpolates in functional space
  - ✓ non-parametric bayesian inference
  - ✓ good scaling in multi-D space
- ✓ Learn unknown "complexity" of the function from the data themselves
  - ✓ Characterization by the covariance function with a small number of hyper parameters  $\theta$
  - ✓ Estimate  $\theta$  from data  $(x_i, t_i)$

ex. 
$$C(\mathbf{x}, \mathbf{x}'; \theta) = \theta_1 \exp \left[ -\frac{1}{2} \sum_{i=1}^I \frac{(x_i - x'_i)^2}{r_i^2} \right] + \theta_2.$$

output



input

- ✓ Given new  $x_{N+1}$  predict  $t_{N+1}$ 
  - ✓ Use  $(x_i, t_i)$  and  $\theta$  and solve another bayesian inference problem

$$P(t_{N+1} | \mathbf{t}_N) \propto \exp \left[ -\frac{1}{2} [\mathbf{t}_N \ t_{N+1}] \mathbf{C}_{N+1}^{-1} \begin{bmatrix} \mathbf{t}_N \\ t_{N+1} \end{bmatrix} \right]$$

answer:

$$\begin{aligned} \hat{t}_{N+1} &= \mathbf{k}^T \mathbf{C}_N^{-1} \mathbf{t}_N \\ \sigma_{\hat{t}_{N+1}}^2 &= \kappa - \mathbf{k}^T \mathbf{C}_N^{-1} \mathbf{k}. \end{aligned}$$

# SIMULATION SPEC

---

✓ N of particles:  $2048^3$

✓ box size: 1, 2 and  $4 h^{-1}\text{Gpc}$

resolve a  $10^{12} h^{-1} M_{\text{solar}}$  halo with  $\sim 100$  particles in the high resolution runs

✓ 2nd-order Lagrangian PT  
initial condition @  $z_{\text{in}}=59$

(vary slightly for different cosmologies to keep the RMS displacement about 25% of the inter-particle separation)

✓ Tree-PM force by L-Gadget2  
(w/  $4096^3$  PM mesh)

✓ 21 outputs in  $0 \leq z \leq 1.5$

(equispaced in linear growth factor)

✓ Data compression (256GB  $\rightarrow$  48GB per snapshot)

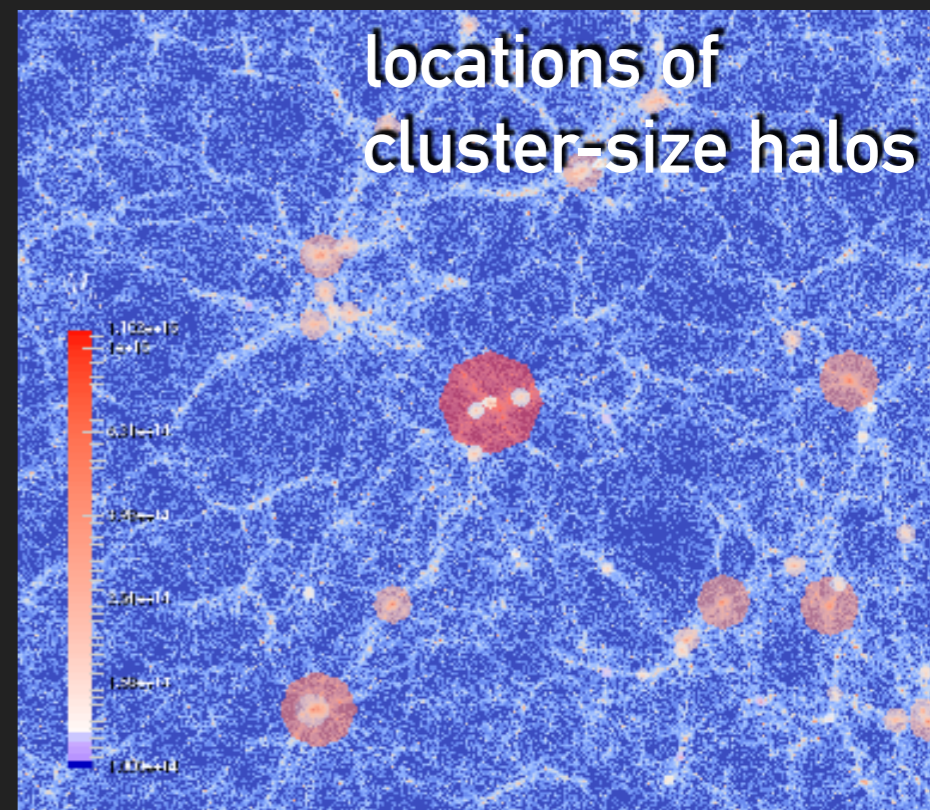
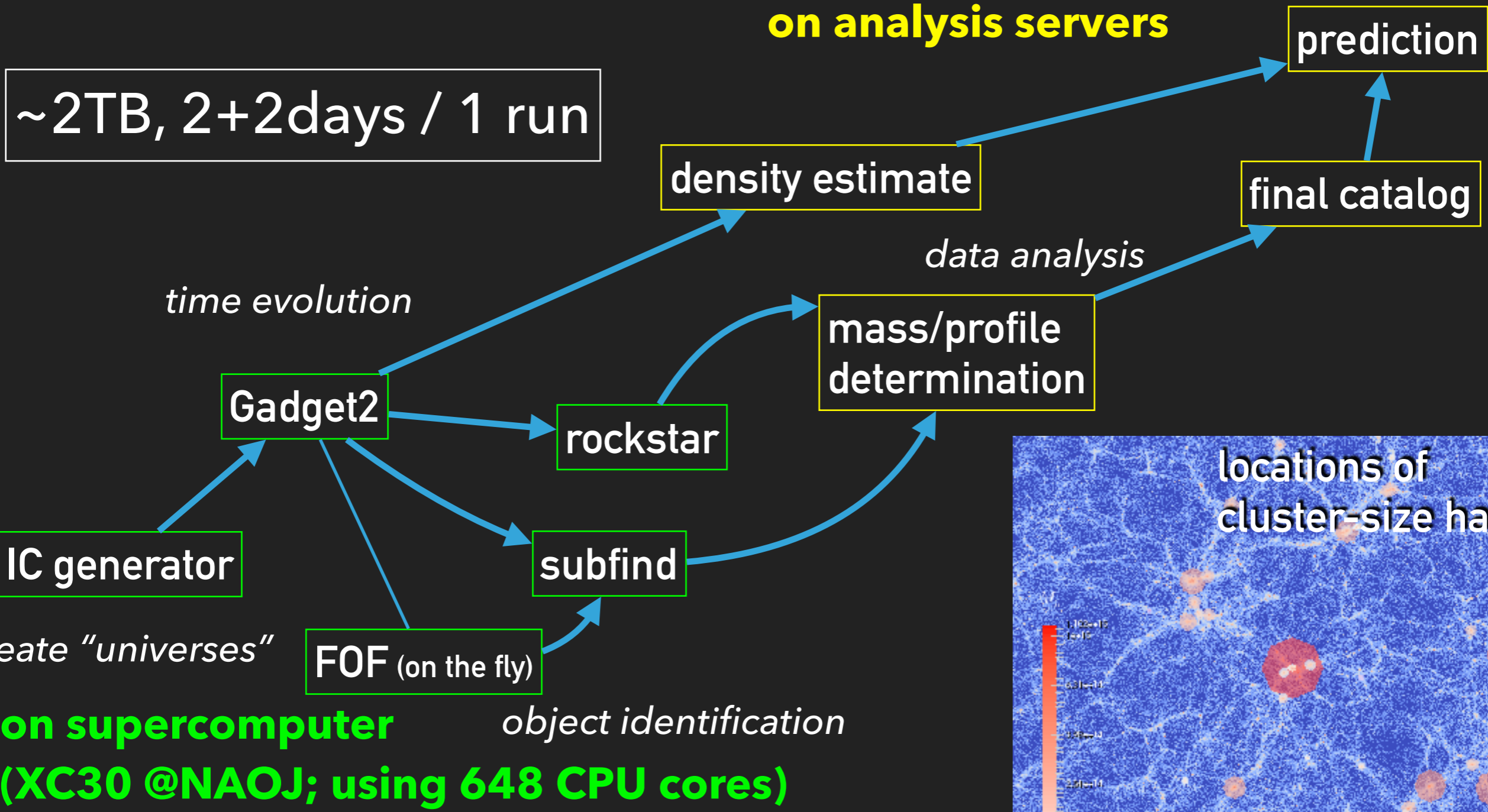
✓ positions  $\rightarrow$  displacement (16 bits per dimension; accuracy  $\sim 1 h^{-1} \text{kpc}$ )

✓ velocity: discard after halo identification

✓ ID: rearrange the order of particles by ID and then discard

✓ consuming  $\sim 200\text{TB}$  ( $\sim$ observational data)

# SIMULATION PIPELINE



► identify and store more than **10 billion** halos in total

# SIMULATION STATUS

122 sims are available in total

## fiducial model

- ▶ PLANCK<sub>15</sub> flat  $\Lambda$ CDM
- ▶ 24+1 realizations done
- ▶ test of statistical error
- ▶ tests/development of analysis codes

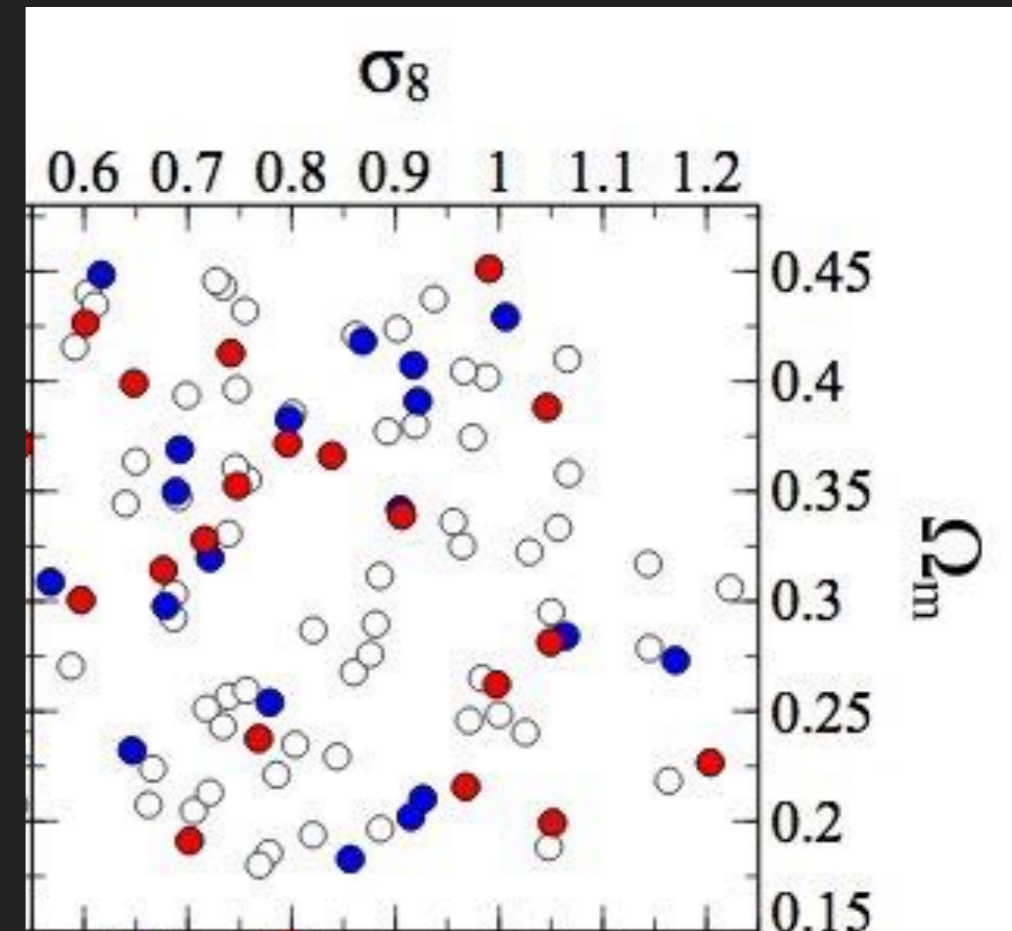
## varied cosmology

### high resolution runs

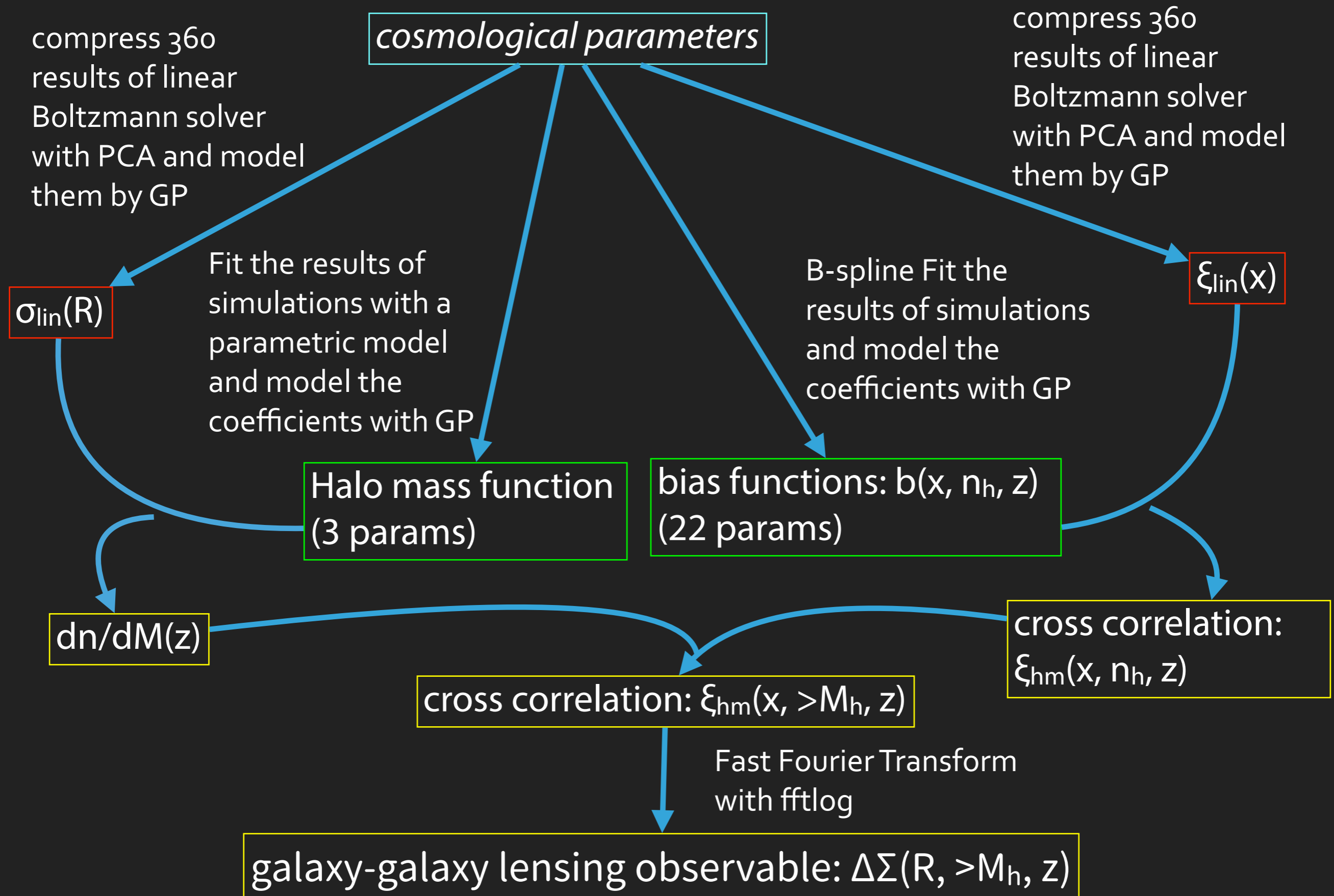
- ▶ g-g lensing
- ▶ 2 initial conditions
  - ▶ fixed random phase (20 done **red**)
  - ▶ varied random phase (40 done **red+blue**)

### low resolution runs

- ▶ calibration of largest scales
- ▶ 37 realizations done
- ▶ in progress (60 white points)



# EMULATOR DESIGN



# Read out pre-computed PCA basis function + GP

```
In [3]: basis = [[joblib.load('basis/S%03d_dens%02d_basis.pkl' % (snap,ndens)) for ndens in range(0,10)] for snap in range(0,21)]
dsig_gp = [[joblib.load('gp/S%03d_dens%02d_gp.pkl' % (snap,ndens)) for ndens in range(0,10)] for snap in range(0,21)]
```

```
In [96]: def prep_dsigma_template(params):
global d_gp
d_gp = np.zeros((21,10,81))
for snap in range(0,21):
for ndens in range(0,10):
d_gp_pca=dsig_gp[snap][ndens].predict(params)
d_gp[snap,ndens,] = basis[snap][ndens].inverse_transform(d_gp_pca)[0,]
```

## Prepare a table for 3D spline

### Inputs:

- ▶ scale factor (time)
- ▶ number density (or halo mass)
- ▶ projected distance

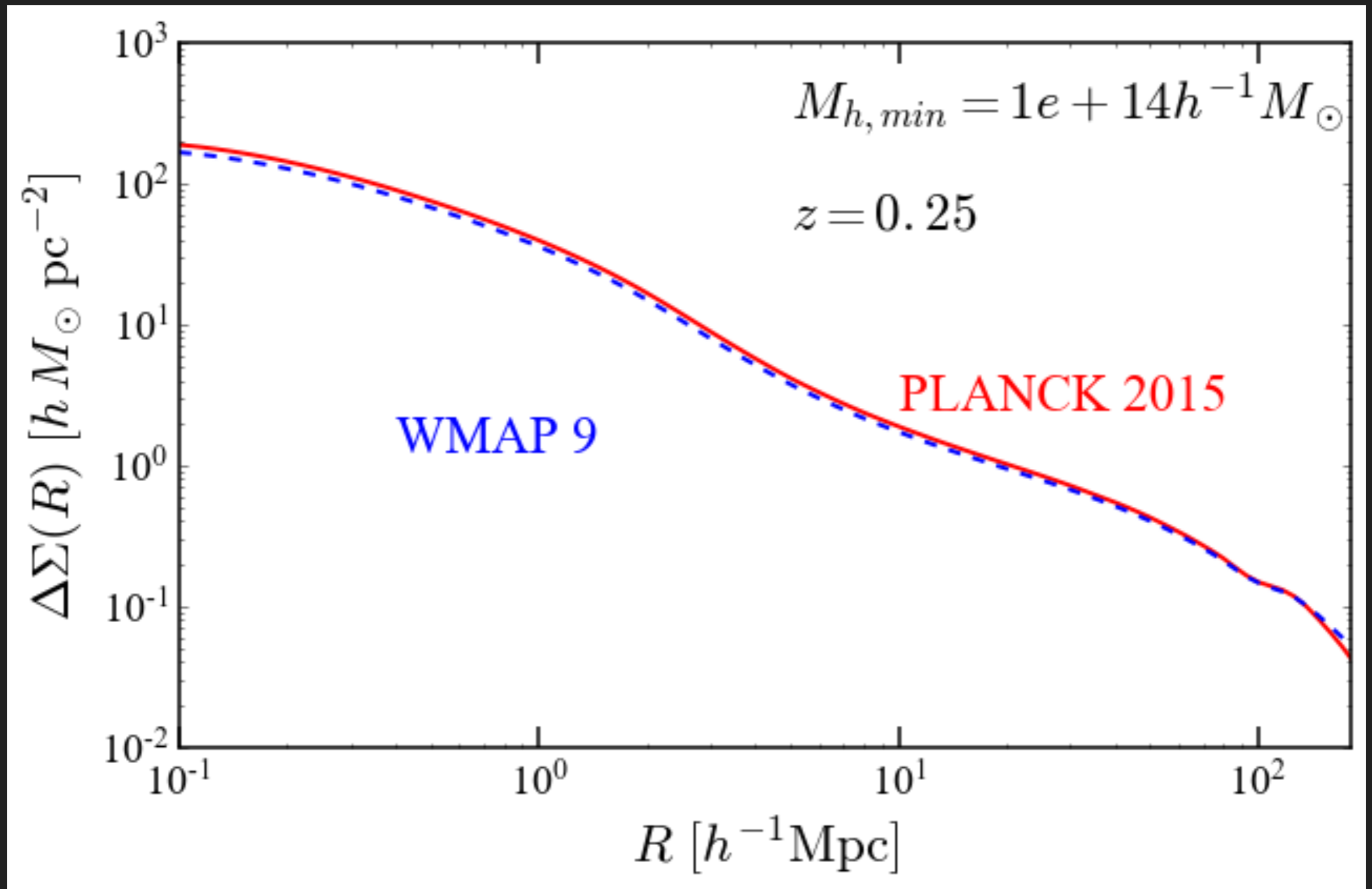
```
In [59]: z=0.25
ascale = 1./(1+z)
Rplot = np.logspace(-1,2.3,100) # in h^{-1}Mpc
Mmin = 1e14 # in h^{-1}M_sun
```

```
# PLANCK 2015
cparam = np.array([[0.02225,0.1198,0.6844,3.094,0.9645,-1]])
set_cosmo(cparam) give your cosmological params ~5s
set_redshift(z) and redshifts ~600ms; HMF GP called inside
lognh = mh_to_logdens(Mmin) convert M_min to n_h ~50μs
plt.loglog(Rplot,get_dsigma(ascale, lognh, Rplot),lw=2,color='red')
```

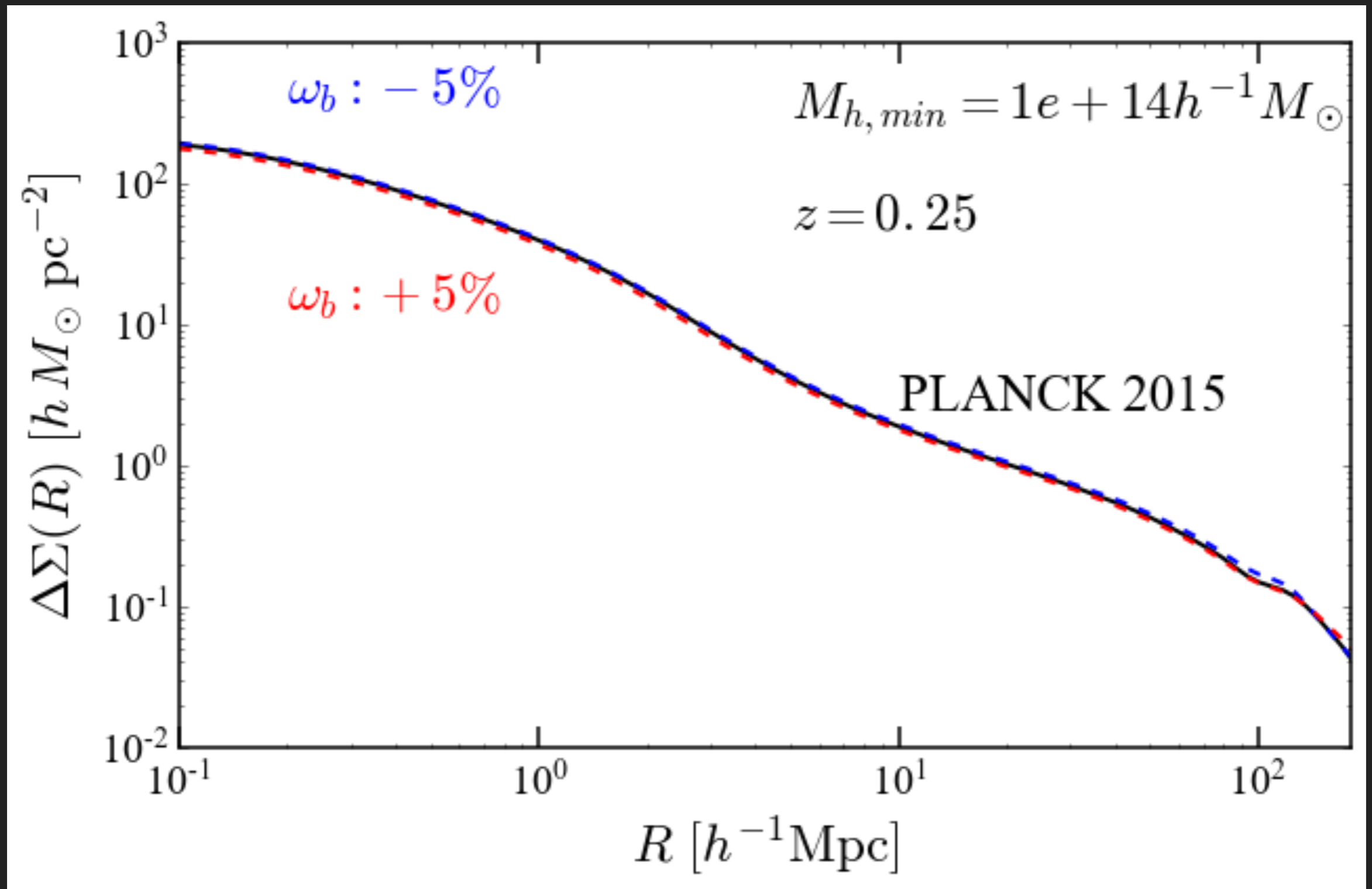
Evaluate !! ~1ms



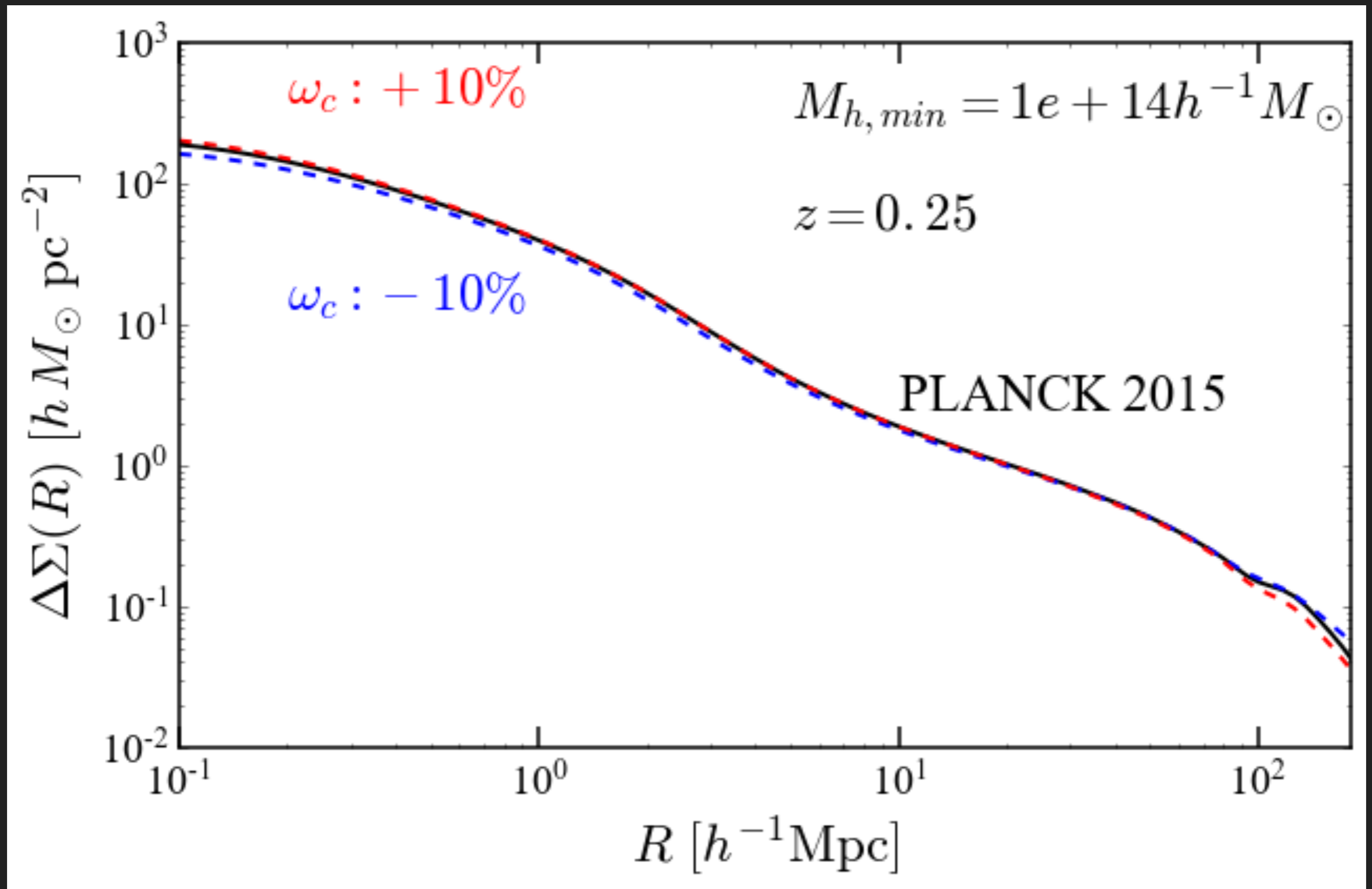
# OUR $\Delta\Sigma$ EMULATOR DEMONSTRATIONS



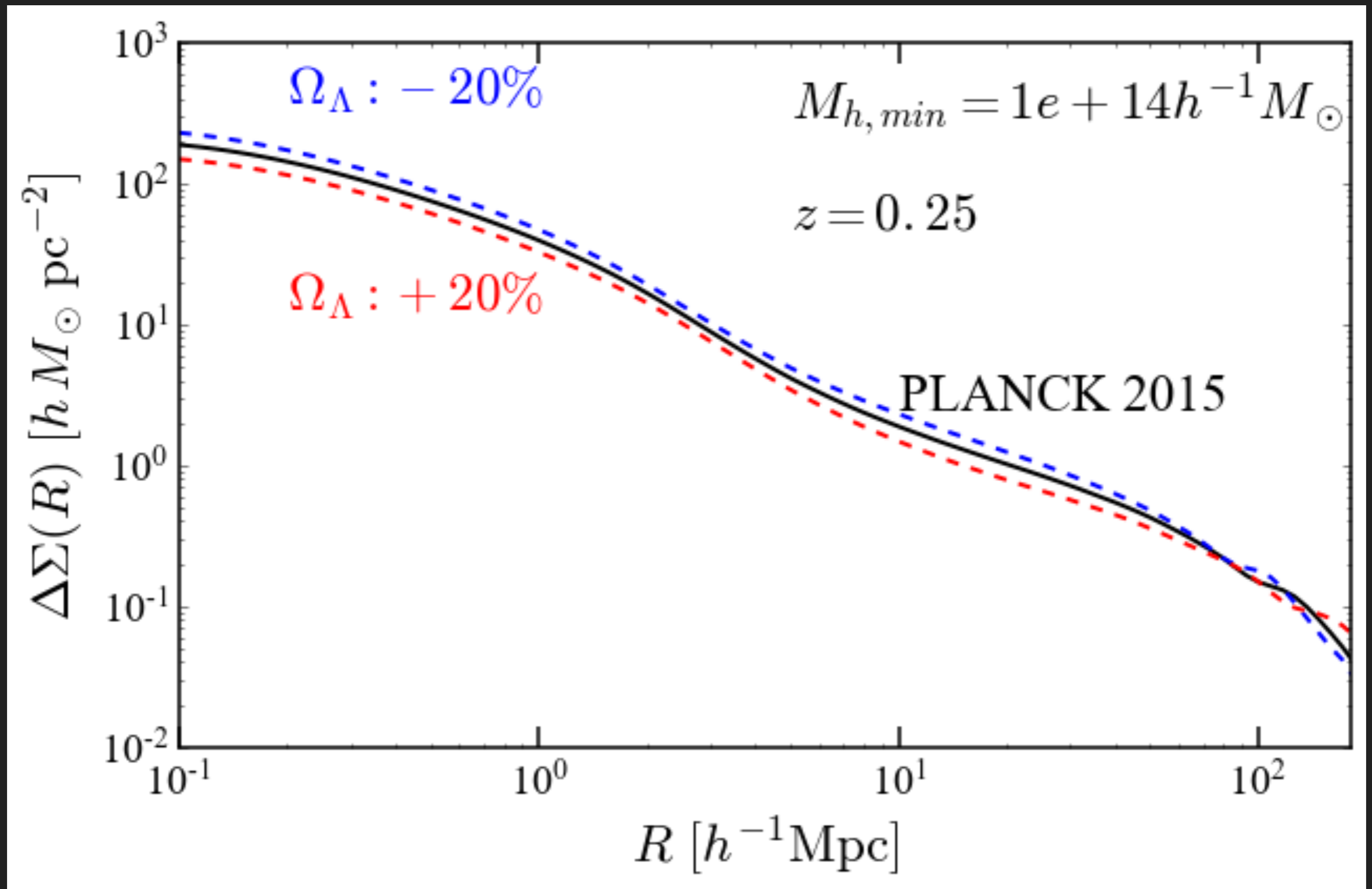
# OUR $\Delta\Sigma$ EMULATOR DEMONSTRATIONS



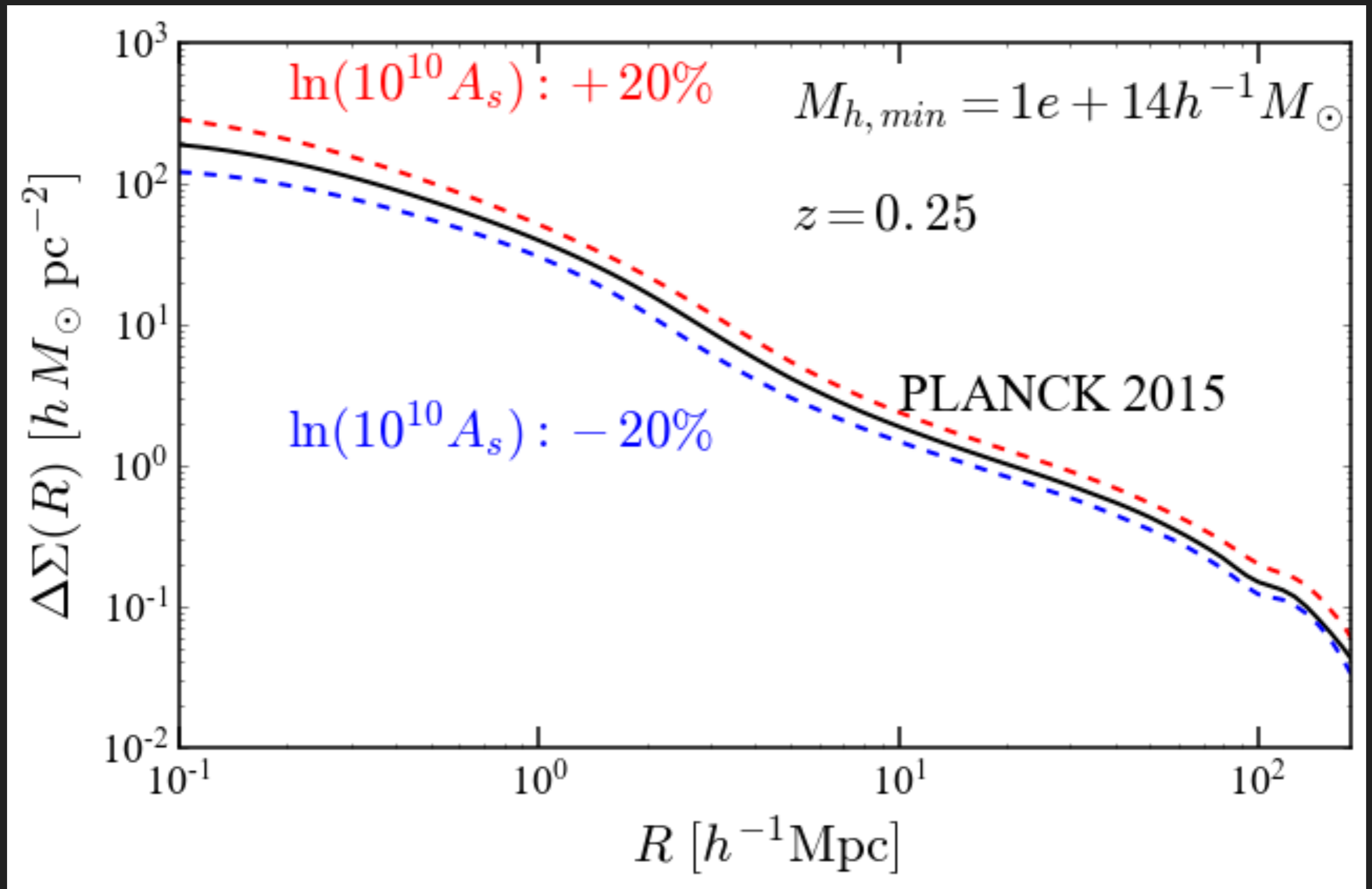
# OUR $\Delta\Sigma$ EMULATOR DEMONSTRATIONS



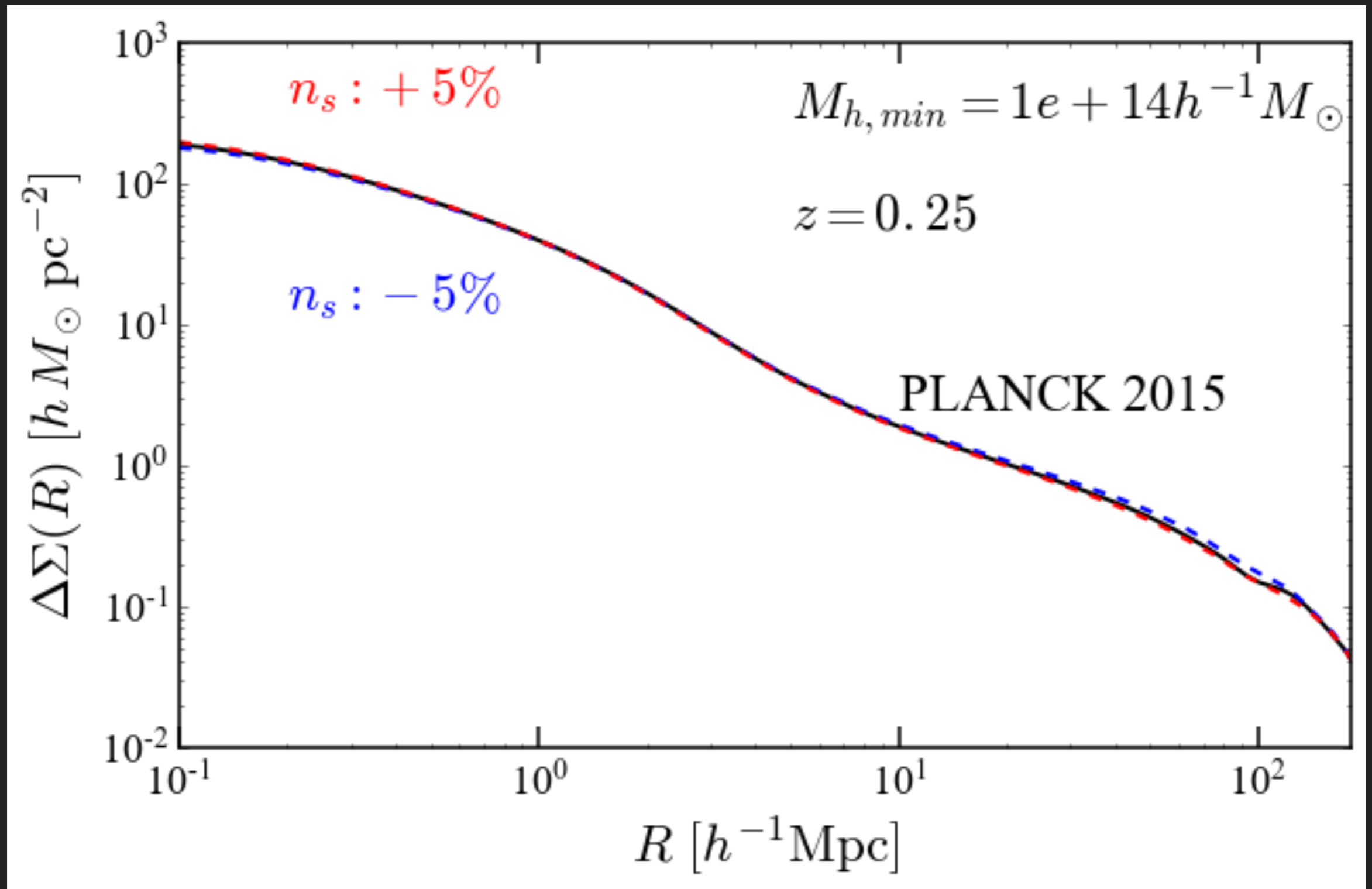
# OUR $\Delta\Sigma$ EMULATOR DEMONSTRATIONS



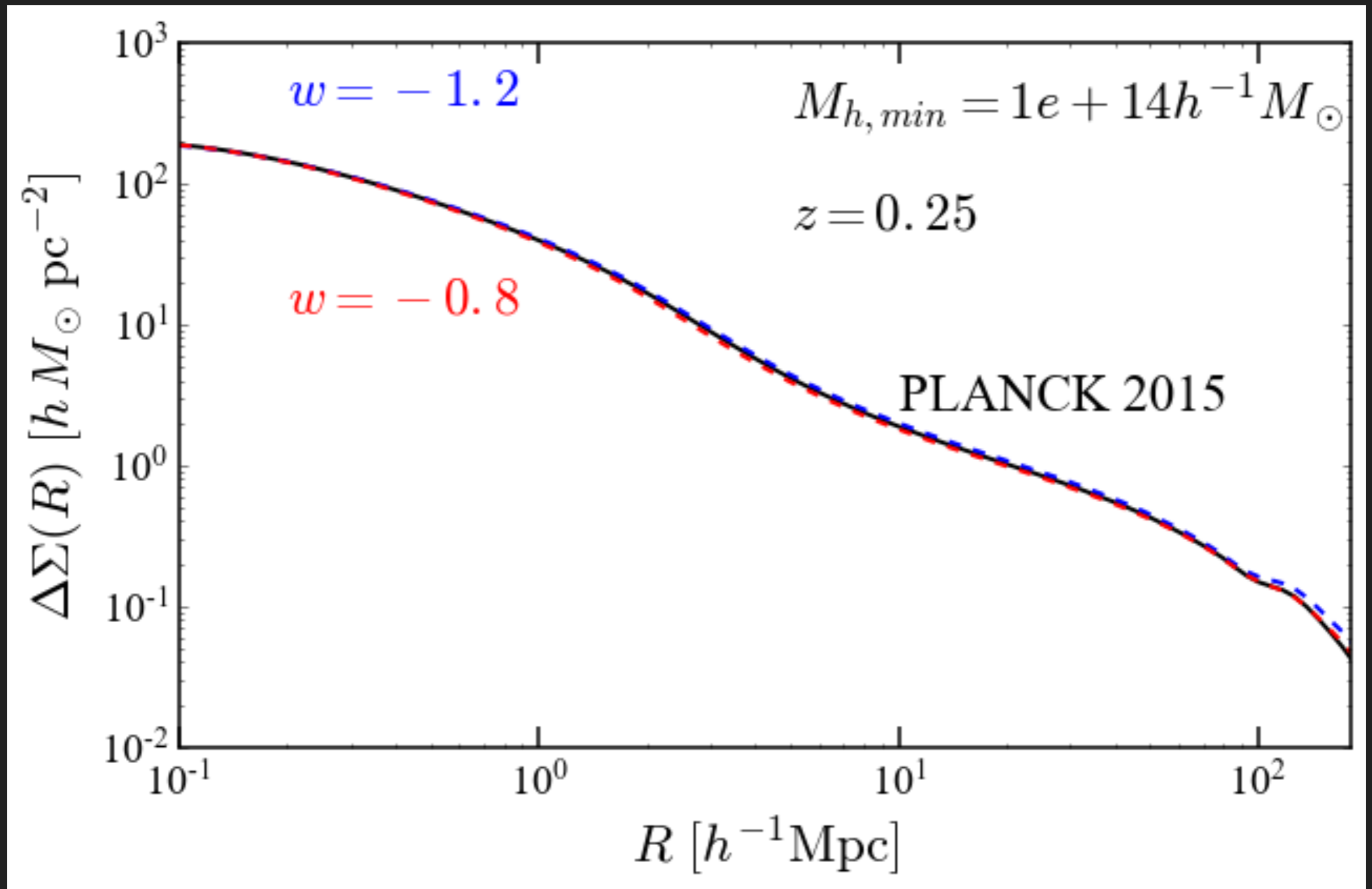
# OUR $\Delta\Sigma$ EMULATOR DEMONSTRATIONS



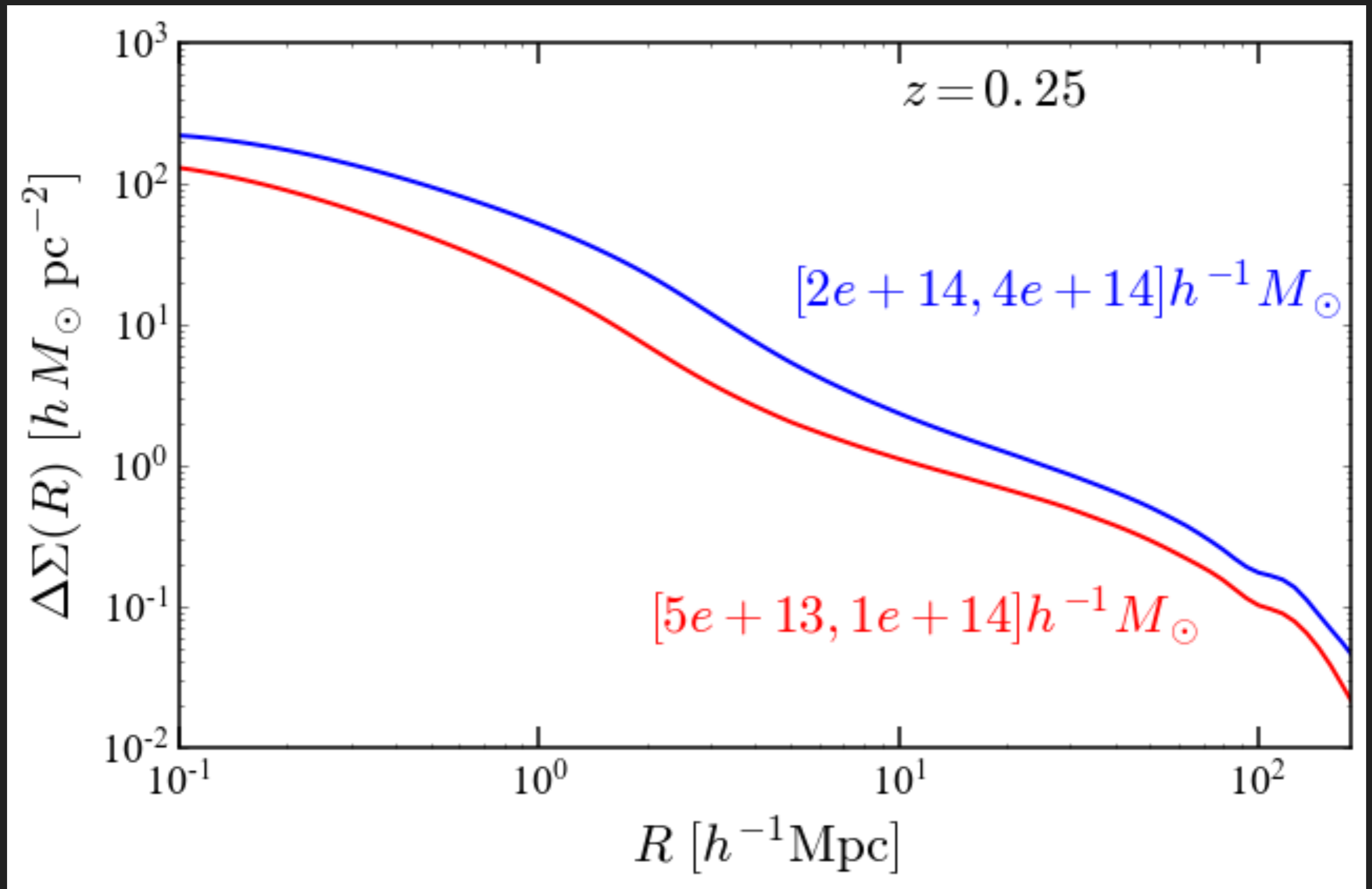
# OUR $\Delta\Sigma$ EMULATOR DEMONSTRATIONS



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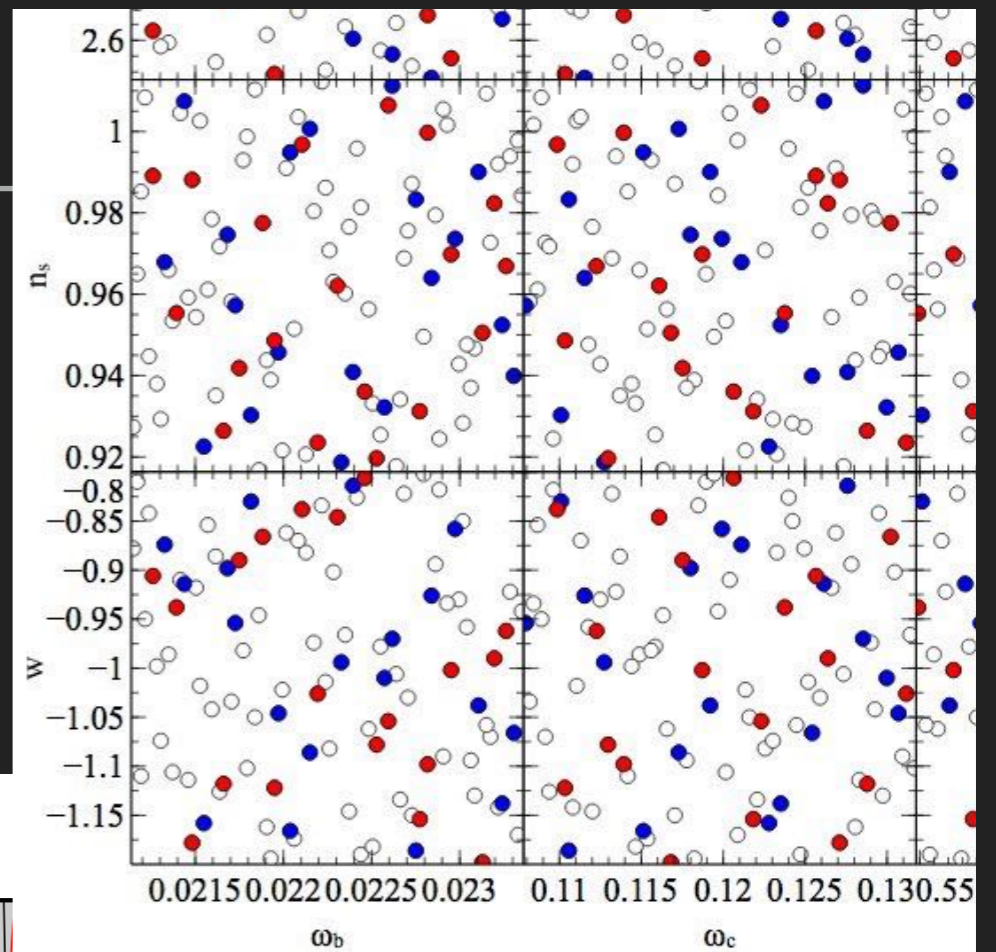


エミュレータ

# GAUSSIAN PROCESS ACCURACY

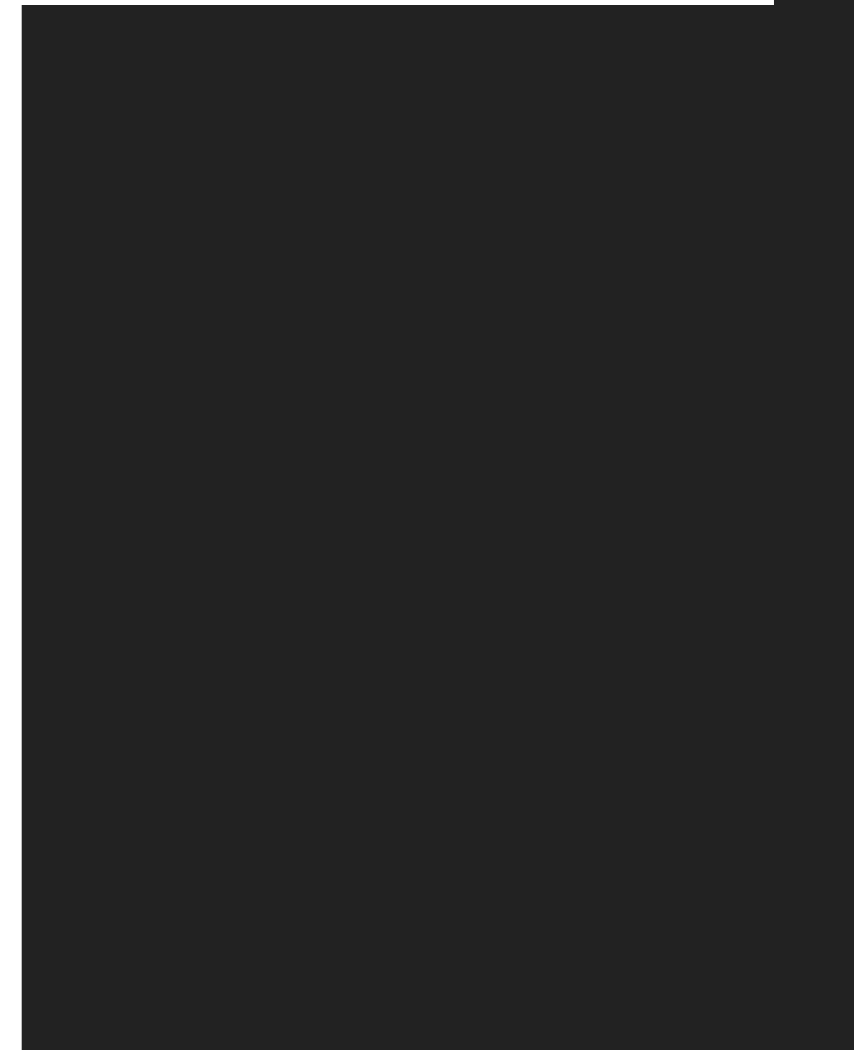
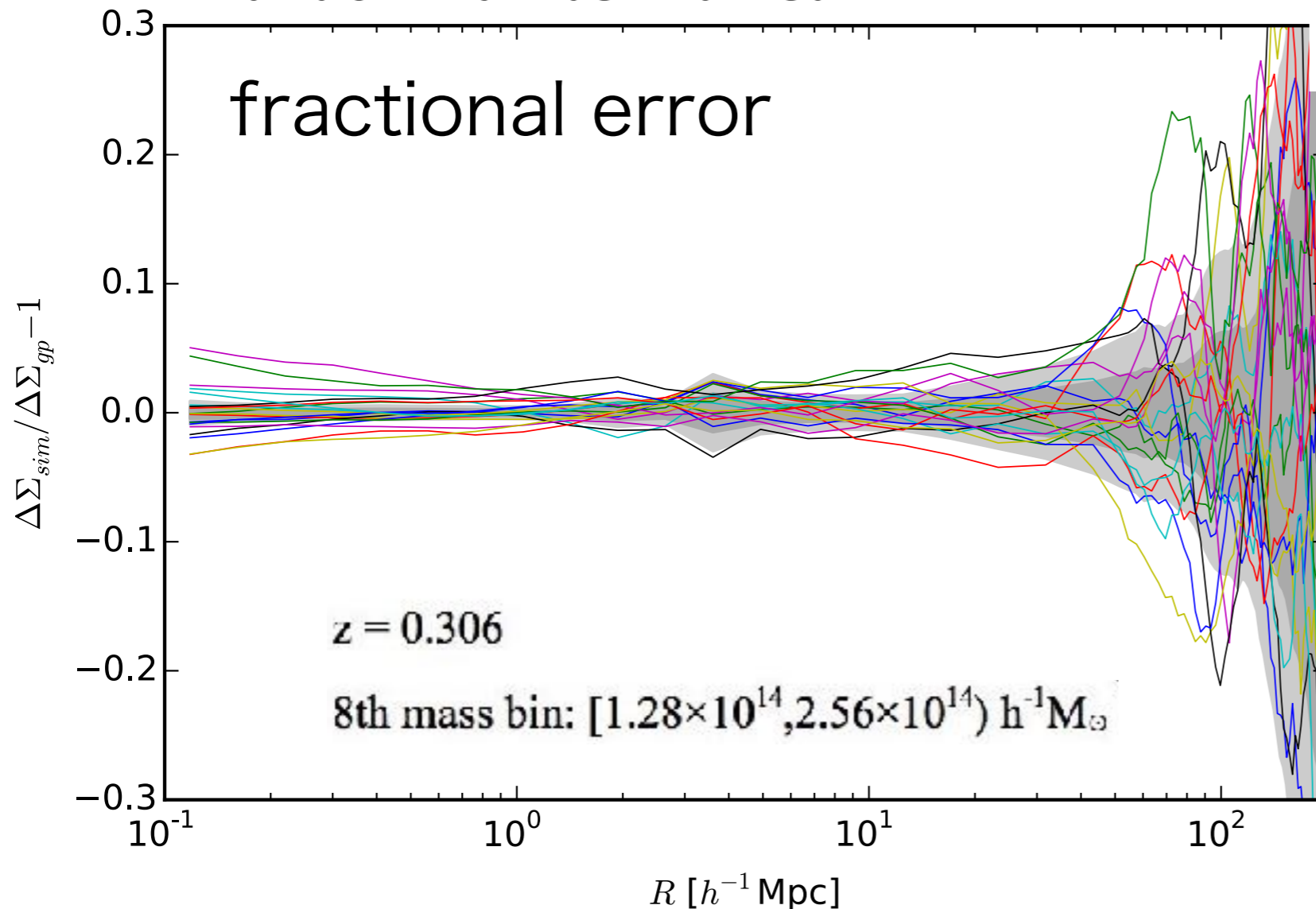
**training** with 20 models (red)

**validation** with 20 other models (blue)



random number varied

fractional error



# SUMMARY

- ▶ Modeling the halo mass function and galaxy-galaxy lensing signal
  - ▶ Latin hypercube design + fitting/GP/spline
  - ▶ handy emulator in python almost ready
  - ▶ accuracy test undergoing, roughly 2-3% accuracy
- ▶ To come
  - ▶ Apply to real data and extract cosmological information
  - ▶ RSD emulator to combine g-g lensing and 3D clustering
  - ▶ further extension under discussion
    - ▶ e.g., non-flat,  $w_0$ - $w_a$  cosmologies

# MCMC cosmology with N-body emulators R. Murata

## Average DM distribution around massive clusters

